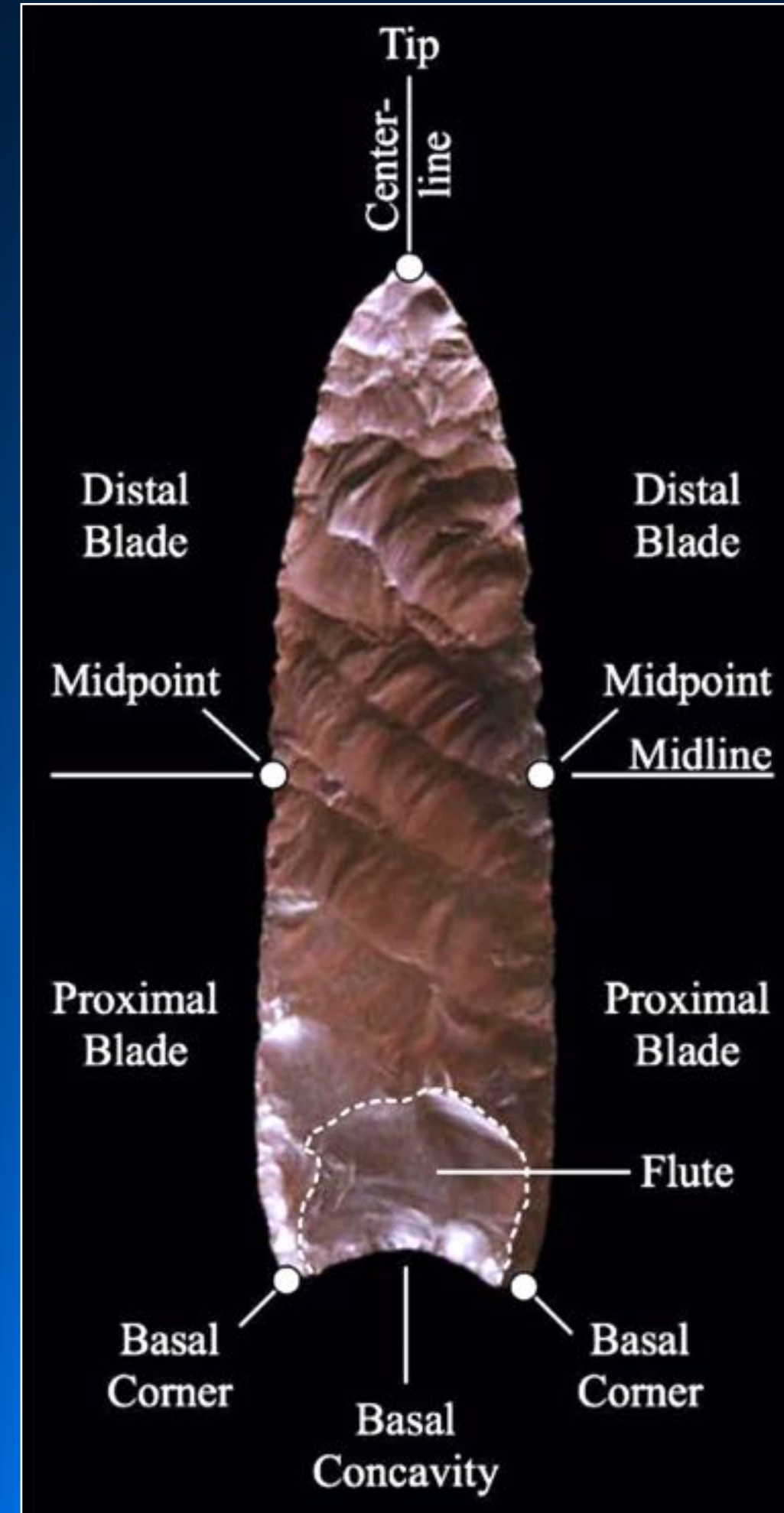


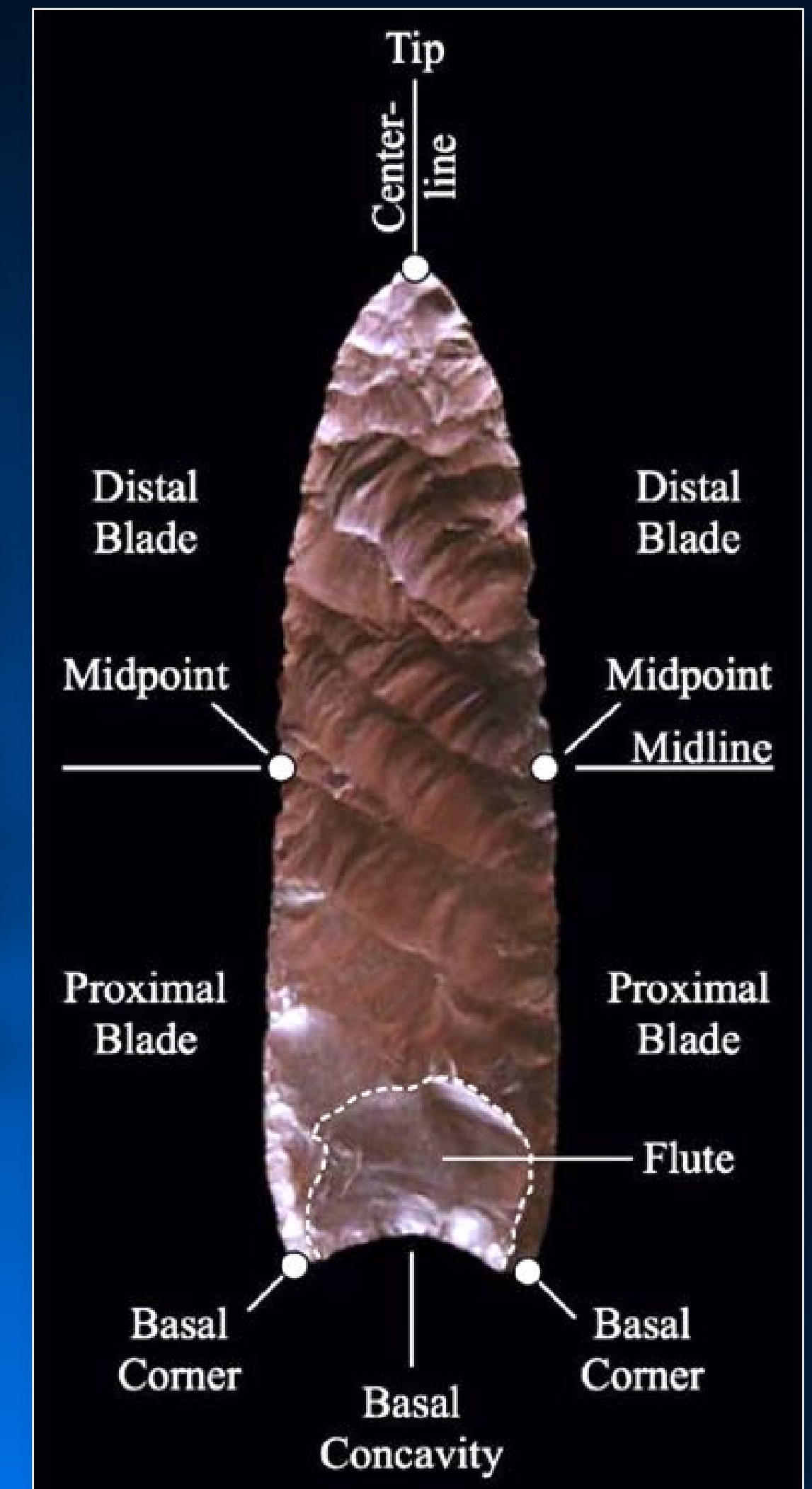
# Lab Practical Assignment V

## Morphometrics & Spatial Data Analysis



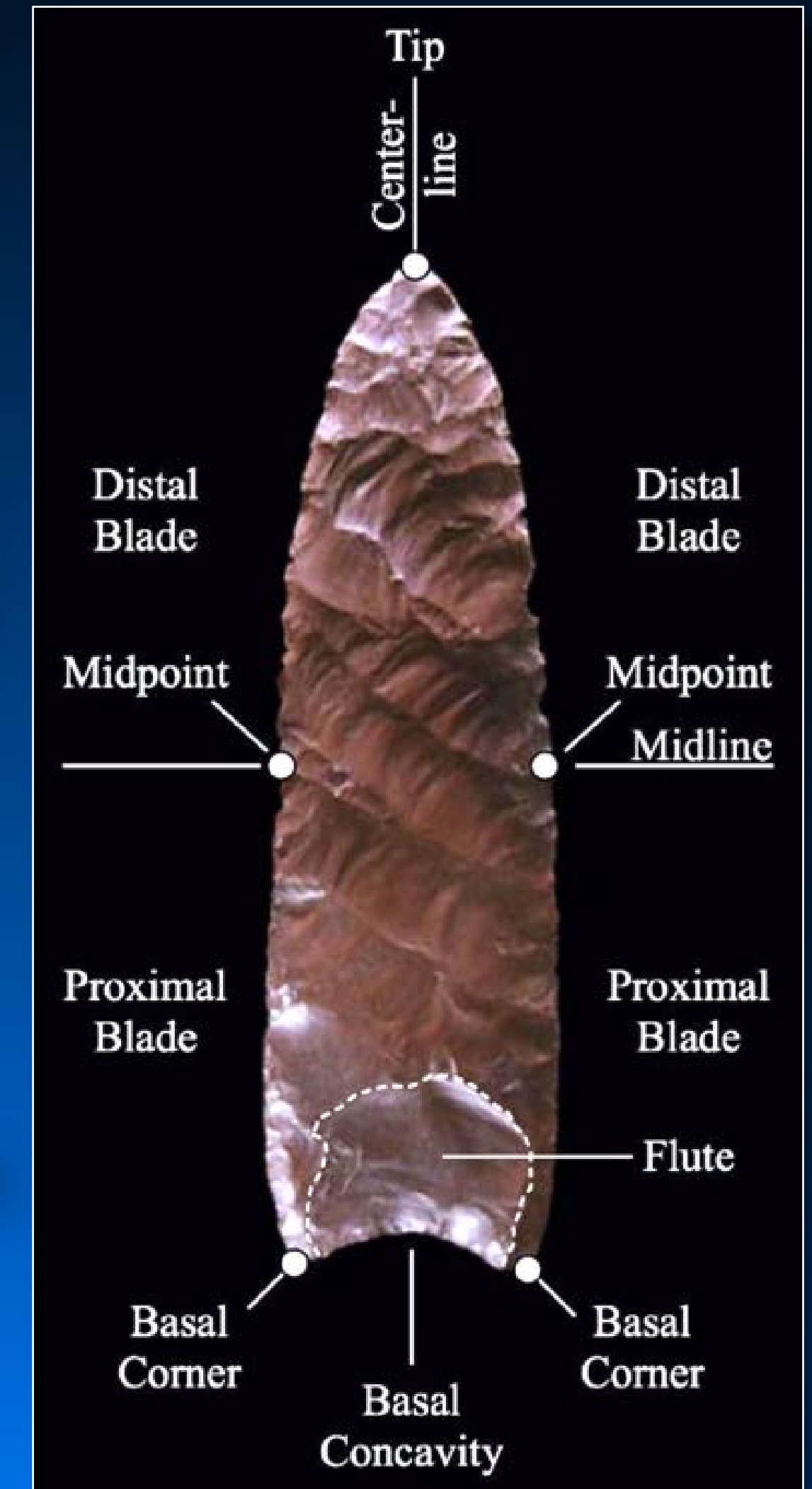
# Lab Practical Assignment V

1. The Clovis dataset (Clovis.csv, Clovis.dat) contains a set of outline semilandmarks for 148 Clovis archeological points collected from four regions in the continental United States. In order to understand human cultural development archaeologists often wish to quantify and compare the forms of artifacts fashioned by craftsmen in different geographic regions, especially in those cases where written records are not available. Analysis of the nominal artifacts that define fluted projectile points, such as those characteristic of the North American Clovis culture (ca. 11,600 – 10,800 radiocarbon yrs BP, 13,550 –12,850 calibrated yrs B.P.), represents an interesting case in point. Identified primarily by their production of a distinctively shaped bladed tool, the PaleoIndian cultures that created these artifacts spread across North America in the interval between the retreat of the northern glaciers at the end of the Pleistocene and the start of the Younger Dryas cold interval. Regional variation in the forms and/or shapes of these artifacts (Fig. 2) has been cited as evidence that Clovis people did, and did not vary their design in response to local environmental conditions or situations, including fabrication material availability, prey types, cultural differences, use in ceremonial activities, etc. Analyse the shapes of these Clovis point outlines and address the following questions. (100 points)



# Lab Practical Assignment V

1. The Clovis dataset (Clovis.csv, Clovis.dat) contained set of outline semilandmarks for 148 Clovis archeological points collected from four regions in the continental United States. ... (100 points)
  - a. Do these data need to be transformed prior to analysis? (10 points)
  - b. Can the dimensionality of these data be reduced without losing potentially important information content? If so, by what means and by how much? Describe the methods and how the data-analysis results that support your (written) interpretation. (20 points)
  - c. What are the major directions of shape variation across the pooled sample? Describe the methods and how the data-analysis results that support your (written) interpretation. (20 points)
  - d. Do distinctions, in terms of Clovis-point shape variation, exist between the regions from which the samples were collected? Describe the methods and how the data-analysis results that support your (written) interpretation. (30 points)
  - e. If any regional distinctions exist, are they significant statistically? Describe the methods and how the data-analysis results that support your (written) interpretation. (20 points)



# Lab Practical Assignment V

## Clovis Point Outlines

n	Group	x1	y1	x2	y2	x3	y3	x4	y4	x5	y5
1	Southwest	0.3171	0.0089	0.2705	0.0527	0.2150	0.0845	0.1562	0.1097	0.0936	0.1229
2	Southwest	0.3273	0.0070	0.2846	0.0550	0.2264	0.0827	0.1630	0.0946	0.0992	0.1038
3	Southwest	0.3251	0.0126	0.2768	0.0518	0.2230	0.0831	0.1648	0.1050	0.1028	0.1099
4	Southwest	0.3405	0.0042	0.2864	0.0436	0.2237	0.0675	0.1586	0.0835	0.0931	0.0980
5	Southwest	0.3170	0.0036	0.2779	0.0552	0.2213	0.0866	0.1585	0.1025	0.0952	0.1160
6	Southwest	0.3145	0.0131	0.2666	0.0548	0.2080	0.0790	0.1531	0.1105	0.0910	0.1240
7	Southwest	0.3107	0.0110	0.2691	0.0568	0.2144	0.0859	0.1548	0.1028	0.0940	0.1145
8	Southwest	0.3430	0.0039	0.2886	0.0433	0.2301	0.0762	0.1640	0.0885	0.0979	0.1001
9	Southwest	0.3313	0.0054	0.2844	0.0517	0.2248	0.0799	0.1601	0.0928	0.0954	0.1055
10	Southwest	0.0061	0.2966	0.0417	0.2314	0.0601	0.0601	0.1643	0.0697	0.0969	0.0767

# Lab Practical Assignment V

1. Calibrating airborne and satellite remote sensing systems requires extensive “ground truthing” via comparison with features whose local and/or regional distributions are known. As part of a calibration exercise a high-angle arial photograph was taken of a test area in southern Arizona in which the taxonomic identification of each individual plant was known. These plants were classified into two types based on their ecologies: extremely drought-tolerant creosote-type plants (e.g., *Larrea tridentata*, left) and moderately drought-tolerant brittlebush-type plants (e.g., *Encelia fairnosa*, right). The locations of these plants in the test area are given in the Arizona datasets (Arizona.csv, Arizona.dat). Use quadrature analysis to quantify and compare the distributions of these plant types in answering the following questions. (90 points)



- a. Do these data need to be transformed prior to analysis? (10 points)
- b. Use the combined distributions of both plants to define 9 cell, 16 cell and 25 cell quadrature sampling schemes. Show your cell counts. (10 points)

# Lab Practical Assignment V

1. Calibrating airborne and satellite remote sensing systems requires extensive “ground truthing” ...  
(90 points)

c. Test for distributional uniformity for the drought-tolerant creosote-type plants and the brittle-bush plants using each sampling scheme. Show the data-analysis results that support your (written) interpretation. (20 points)

d. Combine the two datasets and test for distributional randomness and clustering for the drought-tolerant creosote-type plants and the brittlebush plants using a 15 x 15 quadrat sampling scheme. Show the distribution map and data-analysis results that support your (written) interpretation. (20 points)

e. On the basis of the results you obtained in 3c and 3d decide whether the two plant types exhibit similar or different distributions in the test area. Refer to specific data-analysis results that support your (written) interpretation. (30 points)



# Lab Practical Assignment V

## Arizona Test Site Locations

n	Type	X Axis	Y Axis
1	Creosote-Type	21.97	6.56
2	Creosote-Type	25.59	8.41
3	Creosote-Type	36.90	7.79
4	Creosote-Type	42.01	4.10
5	Creosote-Type	17.91	10.05
6	Creosote-Type	16.42	10.87
7	Creosote-Type	12.37	10.66
9	Creosote-Type	15.14	12.71
10	Creosote-Type	18.98	12.10

n	Type	X Axis	Y Axis
8	Brittlebush Type	13.44	12.30
11	Brittlebush Type	22.82	11.69
26	Brittlebush Type	30.92	14.15
29	Brittlebush Type	37.32	19.27
30	Brittlebush Type	38.82	20.71
31	Brittlebush Type	40.31	20.91
34	Brittlebush Type	43.08	23.78
35	Brittlebush Type	48.84	25.63
36	Brittlebush Type	50.55	26.86

# Lab Practical Assignment V

3. At present, over some 190 have been conformed to exist on Earth (see Earth Impact Database). The North American Impact Structures datasets (North American Impact Structures.csv, North American Impact Structures.dat) lists the locations of the 60 impact structures known from North America (the US, Canada and Mexico) along with the 10 suspected structures that remain unconfirmed at this time. Analyze the geographic distribution of these impact known and suspected structures and answer the following questions.

(120 points)



- a. Do these data need to be transformed prior to analysis? (10 points)
- b. Are the confirmed impact structures distributed uniformly across North America? Describe the methods and how the data-analysis results that support your (written) interpretation. (20 points)
- c. Do the confirmed impact structures exhibit unusual clustering or dispersion across North America? If so, what might this arise from? Describe the methods and how the data-analysis results that support your (written) interpretation. (30 points)
- d. Are the unconfirmed impact structure positions distributed uniformly within their own spatial field? Describe the methods and show the data-analysis results that support your (written) interpretation. (20 points)
- e. If positions of the unconfirmed structures are combined with the positions of the confirmed impact structures, would this change your answers to 3b and/or 3c? Show the data-analysis results that support your (written) interpretation. (40 points)

# Lab Practical Assignment V

## North American Impact Database

Name	Location	Diameter (km)	Age (years)	Latitude	Longitude
Brent	Ontario	3.8	396 ± 20	46°5'N	78°29'W
Carswell	Saskatchewan	39	115 ± 10	58°27'N	109°30'W
Charlevoix	Quebec	54	342 ± 15	47°32'N	70°18'W
Couture	Quebec	8	430 ± 25	60°8'N	75°20'W
Deep Bay	Saskatchewan	13	99 ± 4	56°24'N	102°59'W
Eagle Butte	Alberta	10	< 65	49°42'N	110°30'W
Elbow	Saskatchewan	8	395 ± 25	50°59'N	106°43'W
Gow	Saskatchewan	4	< 250	56°27'N	104°29'W
Haughton	Nunavut	23	39	75°23'N	89°40'W

# Lab Practical Assignment V

4. The cuticula of many trilobites display numerous tubercles, which are small raised bumps or granular-like protuberances on a structure's surface. In some trilobites these are thought to house specialized organs that allowed the trilobite to sense its local environment. If this hypothesis is correct it would be interesting to know whether the distribution of these tubercles was random, clustered or dispersed. The Tubercles dataset (Tubercles.csv, Tubercles.dat) contains information on the positions of 136 tubercles collected from the left-hand side of the cranidium from a single *Paradoxides forchhammeri* specimen. Use nearest-neighbor analysis to answer the following questions. (100 points)
- Do these data need to be transformed prior to analysis? (10 points)
  - What is the expected mean nearest neighbor distance for these data based on the naïve estimate and Donnelly's (1978) correction for edge effects? In this calculation use the area and perimeter of the distribution's convex hull as the area estimate. (20 points)
  - What is the mean nearest neighbor distance for these data? (20 points)
  - Based on the results you obtained in 4b and 4c, decide whether the tubercles in this specimen display a random, clustered or dispersed distribution. Show the data-analysis results that support your (written) interpretation. (30 points)
  - Based on the results you obtained in 4d offer explanations for the distribution, and the function, of tubercles under the assumption that they housed some sort of sensory organ. (20 points)



# Lab Practical Assignment V

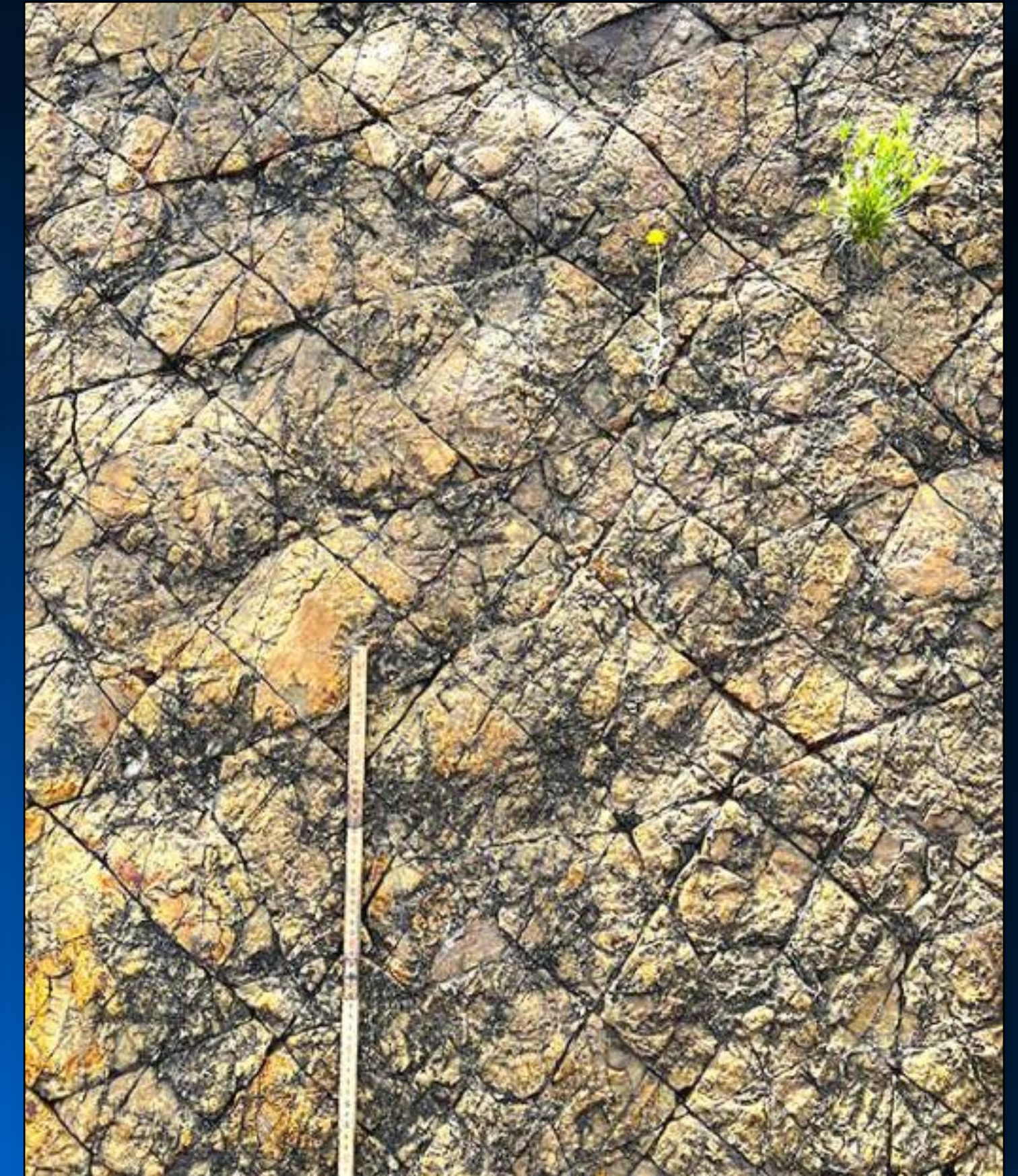
## Trilobite Glabellar Tubercles

n	Group	x-Axis (cm)	y-Axis (cm)
1	Paradoxides forchhammeri	0.306	1.932
2	Paradoxides forchhammeri	0.240	1.825
3	Paradoxides forchhammeri	0.404	1.935
4	Paradoxides forchhammeri	0.357	1.798
5	Paradoxides forchhammeri	0.460	1.872
6	Paradoxides forchhammeri	0.568	1.874
7	Paradoxides forchhammeri	0.574	1.754
8	Paradoxides forchhammeri	0.724	1.847
9	Paradoxides forchhammeri	0.808	1.839
10	Paradoxides forchhammeri	0.788	1.681

n	Group	x-Axis (cm)	y-Axis (cm)
11	Paradoxides forchhammeri	0.916	1.694
12	Paradoxides forchhammeri	0.922	1.823
13	Paradoxides forchhammeri	1.061	1.834
14	Paradoxides forchhammeri	1.081	1.632
15	Paradoxides forchhammeri	1.128	1.651
16	Paradoxides forchhammeri	1.148	1.782
17	Paradoxides forchhammeri	1.234	1.842
18	Paradoxides forchhammeri	1.454	1.763
19	Paradoxides forchhammeri	1.348	1.670
20	Paradoxides forchhammeri	1.357	1.593

# Lab Practical Assignment V

3. In the development of petroleum reservoirs it is important to understand the direction(s) petroleum resources can be expected to flow. In this context it would be useful to know whether lineaments exposed on the surfaces of reservoir-rock outcrops are indicative of fractures at depth. The three Odessa datasets (Odessa North, Odessa Northwest, Odessa West) contain surface lineament direction measurements for two reservoir rock formations. In the Odessa North field independent assessments of the reservoir fracture pattern characterizing the Grayburg Dolomite at depth suggest its fractures exhibit a trend of approx. N 75° E. In the Odessa Northwest field (also the Grayburg Dolomite) at-depth studies suggest fracture trends of N 35° E and N 55° W. The Odessa West field drawn petroleum from the San Andrews Limestone where water flood breakthrough data suggest a channeling trend of N 75° E. The Odessa North, Odessa Northwest and Odessa West datasets each contain surface lineament measurements for outcrops of the reservoir rocks in question. Use these data to perform the following analyses and answer their associated questions. (120 points)

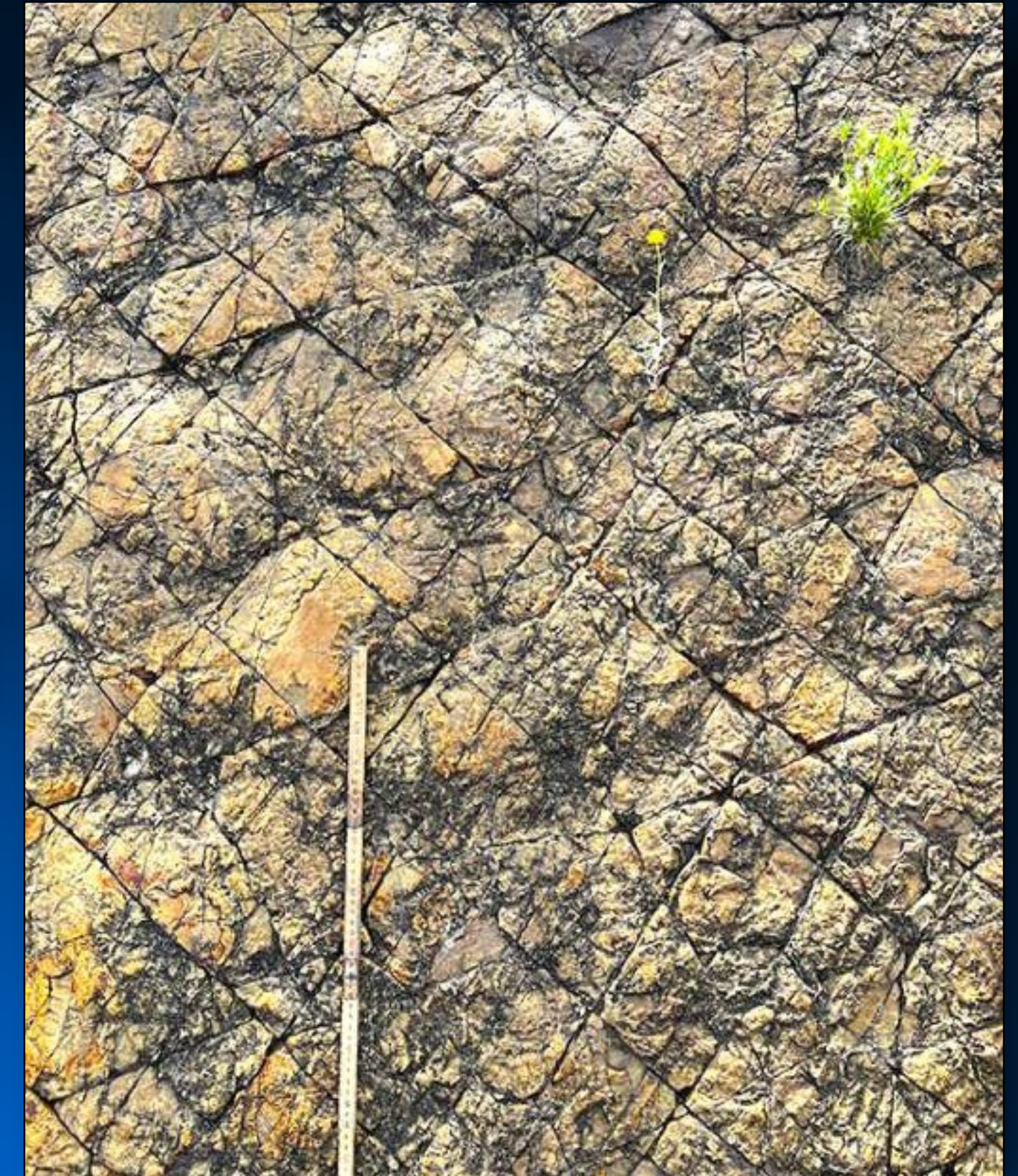


a. Do these data need to be transformed prior to analysis? (10 points)

b. Display direction rose charts for the Odessa North, Odessa Northwest and Odessa West datasets. Use these to estimate the mean lineament directions and their associated 95 percent confidence angles. (30 points)

# Lab Practical Assignment V

3. In the development of petroleum reservoirs it is important to understand the direction(s) petroleum resources can be expected to flow. ... (120 points)
- On a pairwise basis, do these lineament data all exhibit the same trend directions? Show the data-analysis results that support your (written) interpretation. (30 points)
  - Are each of the lineament datasets consistent with the estimates of at-depth fracture trends for their respective petroleum production fields? Show the data-analysis results that support your (written) interpretation. (30 points)
  - How might any discrepancies between surface lineament trends and at-depth direction flow trends be accounted for? (20 points)



# Lab Practical Assignment V

## Odessa Direction Data

n	Group	Azimuth
1	Odessa North	49.3
2	Odessa North	43.3
3	Odessa North	47.4
4	Odessa North	129.0
5	Odessa North	128.5
6	Odessa North	126.3
7	Odessa North	127.8
8	Odessa North	125.0
9	Odessa North	47.5
10	Odessa North	47.8

n	Group	Azimuth
1	Odessa Northwest	35.3
2	Odessa Northwest	105.9
3	Odessa Northwest	33.2
4	Odessa Northwest	249.4
5	Odessa Northwest	78.5
6	Odessa Northwest	34.7
7	Odessa Northwest	76.0
8	Odessa Northwest	31.0
9	Odessa Northwest	32.5
10	Odessa Northwest	241.9

n	Group	Azimuth
1	Odessa West	27.8
2	Odessa West	181.4
3	Odessa West	47.5
4	Odessa West	12.2
5	Odessa West	242.7
6	Odessa West	68.0
7	Odessa West	48.8
8	Odessa West	180.5
9	Odessa West	77.5
10	Odessa West	246.2

# Lab Practical Assignment IV

## Multivariate Data Analysis, Morphometrics & Diversity

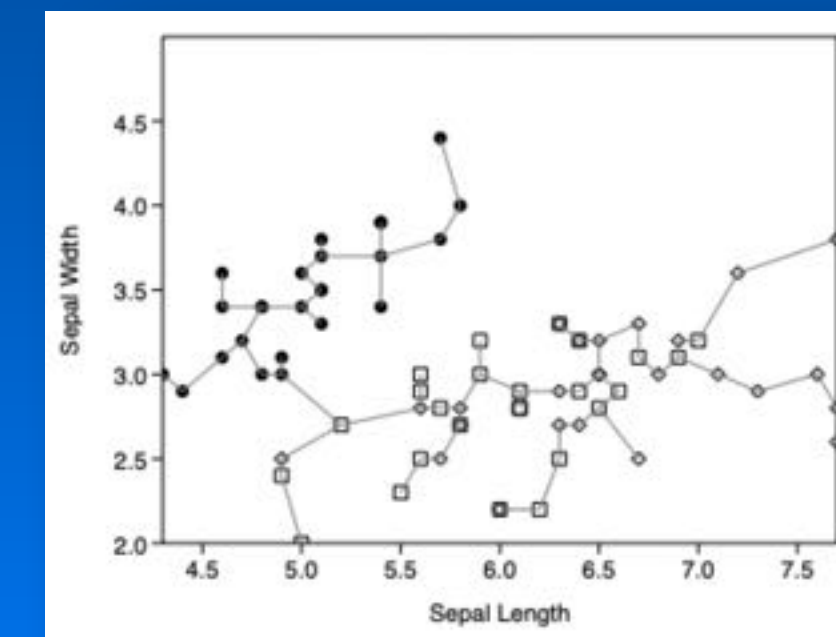
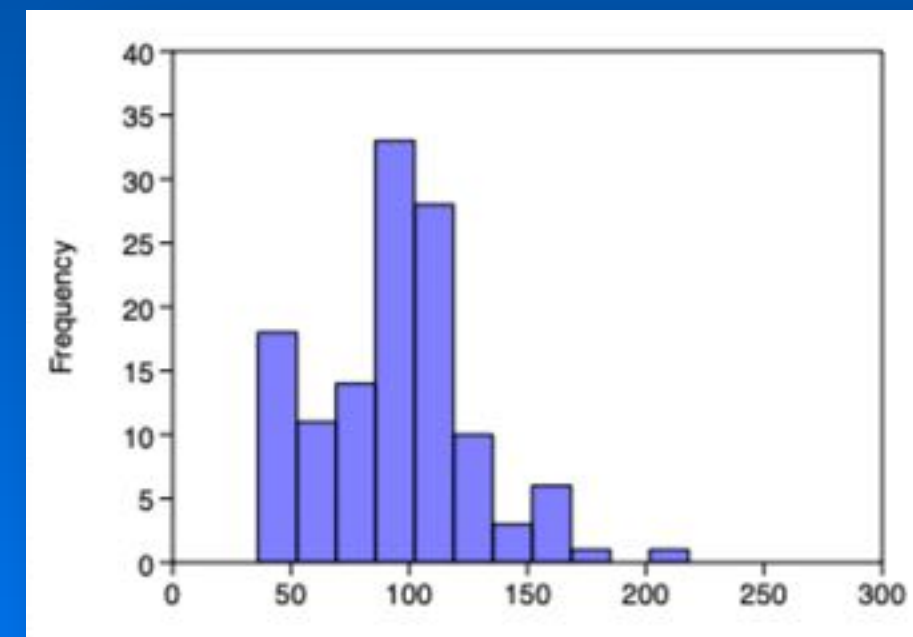
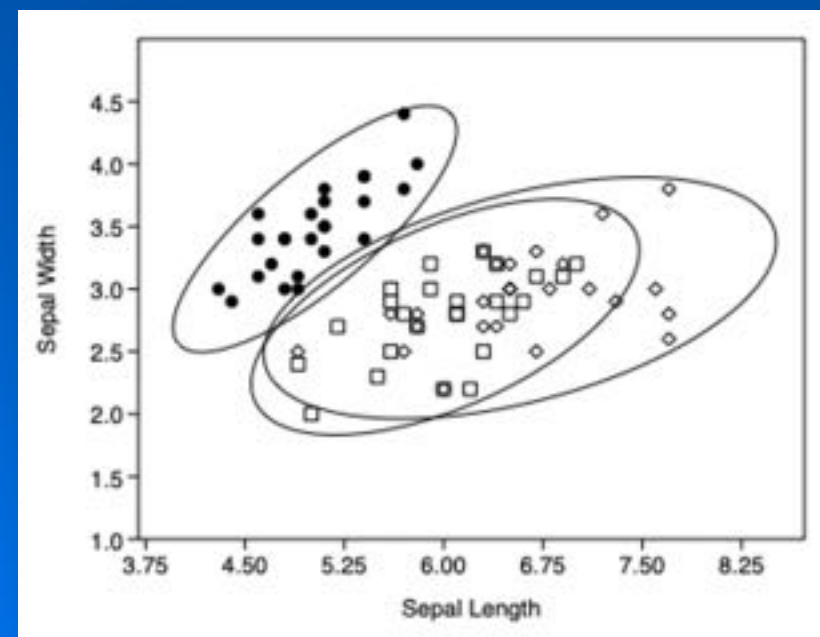
Croatia Radiation Data.dat

	40K	224Ra	228Ra	236U	137Cs	Natural	Total	H	I
2	13.7	41.9	24.4	0.1	2.8	80.2	83		
3	14	52.6	48.4	0.4	3.3	115.4	118.7		
4	12.3	40.6	27.7	0.2	1.6	80.8	82.3		
5	13.2	45.9	29.6	0.4	2.5	89.2	91.6		
6	11.3	40.6	21.6	0.1	1.6	73.6	75.2		
7	15.8	20	8.9	0.1	6	44.8	50.8		
8	14.3	45.3	25.4	0.2	1.1	85.2	86.3		
9	15.5	50.6	28.2	0.2	1.7	94.5	96.2		
10	13.3	59.2	30.6	0.2	1.8	103.3	105.1		
11	12.6	37.9	41.8	0.2	2.4	92.6	94.9		
12	11.7	28.6	34.3	0.2	5	74.9	79.9		
13	12.2	30.6	57.3	0.2	9.3	100.4	109.7		
14	16.2	53.2	36.2	0.2	2	105.9	107.9		
15	14.3	32.6	61.6	0.3	6.6	108.7	115.4		
16	15.5	16	8.5	0.1	0.7	40	40.6		
17	11.2	35.9	35.7	0.2	5.3	83	88.3		
18	11.7	39.9	42.8	0.2	11.7	94.6	106.3		
19	12.9	12.6	8	0.2	2.4	33.7	36		
20	15.9	21.3	11.3	0.1	3.9	48.6	52.5		
21	12.5	24	14.6	0.1	2	51.1	53.1		
22	18.7	20	9.4	0.1	16.9	48.2	65.1		
23	15	13.3	7.5	0	2.5	35.9	38.3		
24	18.3	38.6	62.5	0.5	8.2	119.9	128.1		



Iris 25.dat

	Species	Sepal Length	Sepal Width	Petal Length	Petal Width	F	G	H
1	I. setosa	5.1	3.5	1.4	0.2			
2	I. setosa	4.9	3	1.4	0.2			
3	I. setosa	4.7	3.2	1.3	0.2			
4	I. setosa	4.6	3.1	1.5	0.2			
5	I. setosa	5	3.6	1.4	0.2			
6	I. setosa	5.4	3.9	1.7	0.4			
7	I. setosa	4.6	3.4	1.4	0.3			
8	I. setosa	5	3.4	1.5	0.2			
9	I. setosa	4.4	2.9	1.4	0.2			
10	I. setosa	4.9	3.1	1.5	0.1			
11	I. setosa	5.4	3.7	1.5	0.2			
12	I. setosa	4.8	3.4	1.6	0.2			
13	I. setosa	4.8	3	1.4	0.1			
14	I. setosa	4.3	3	1.1	0.1			
15	I. setosa	5.8	4	1.2	0.2			
16	I. setosa	5.7	4.4	1.5	0.4			
17	I. setosa	5.4	3.9	1.3	0.4			
18	I. setosa	5.1	3.5	1.4	0.3			
19	I. setosa	5.7	3.8	1.7	0.3			
20	I. setosa	5.1	3.8	1.5	0.3			
21	I. setosa	5.4	3.4	1.7	0.2			
22	I. setosa	5.1	3.7	1.5	0.4			
23	I. setosa	4.6	3.6	1	0.2			



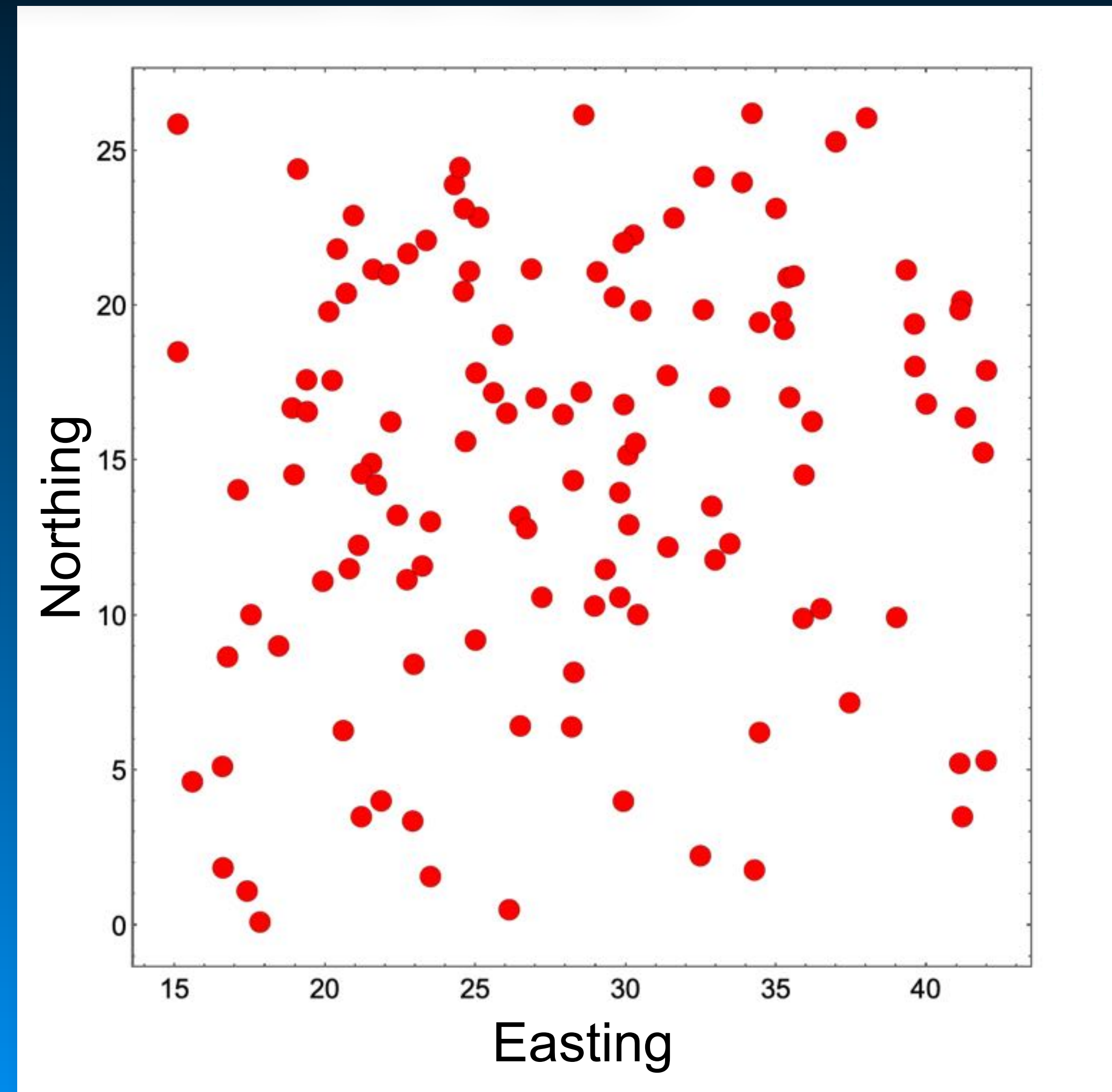
# Distribution of Points

## Test for Uniform Distribution of Points

Often one of the first questions to be confronted in an earth science context is what sort of spatial distribution the sampled localities in a dataset exhibit.

This is a plot of the locations of 123 wells drilled in the Arbuckle Group in central Kansas.

Do these data exhibit uniform density?



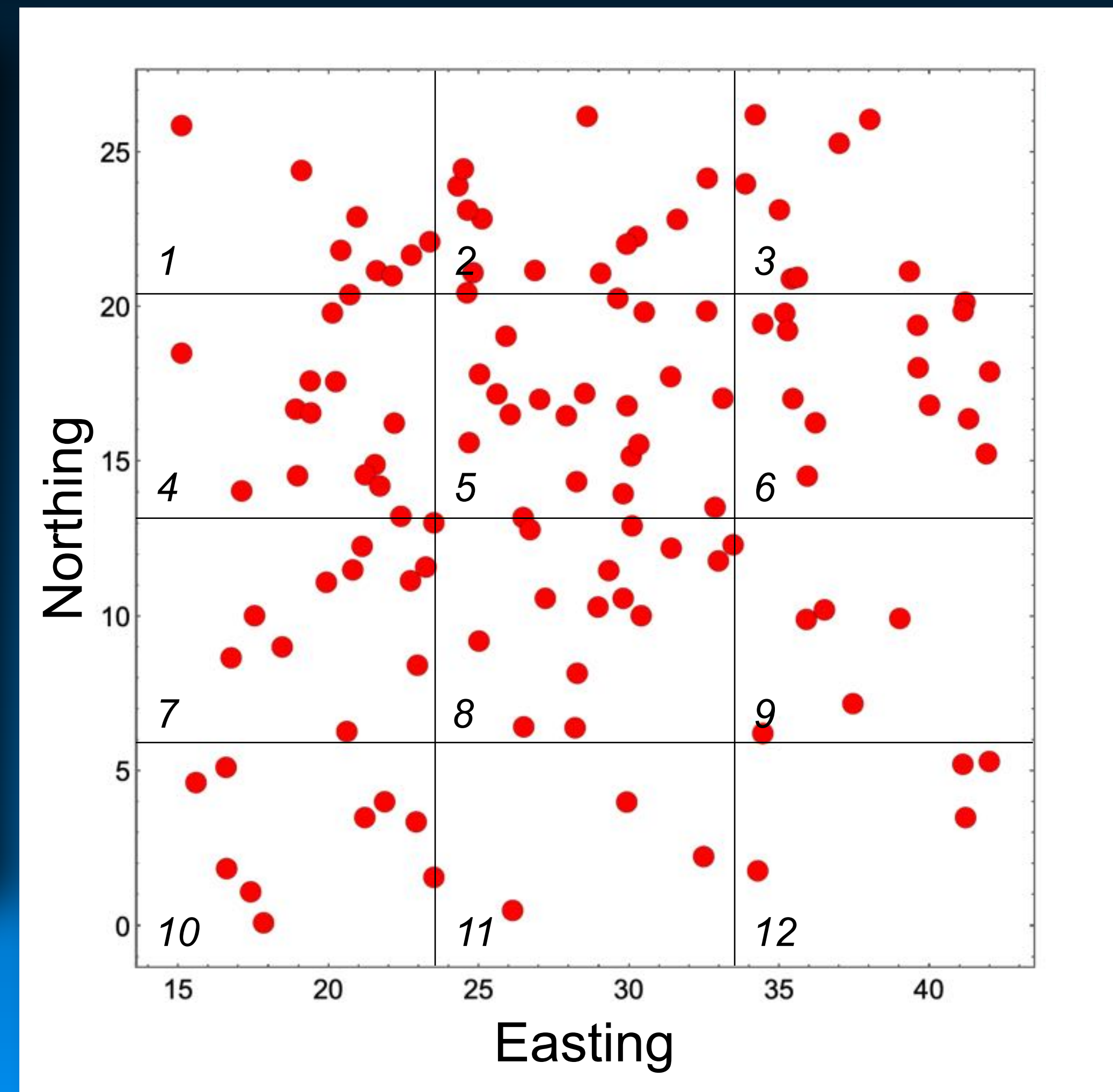
# Distribution of Points

## Test for Uniform Distribution of Points: Quadrat Analysis

One approach would be to partition the area into a series of equal-size quadrats and count the frequency of wells that fall into each partition.

If the wells are spaced uniformly there should be no statistically significant difference between the quadrat frequency counts.

Cell	Obs.
1	8
2	13
3	8
4	14
5	20
6	14
7	11
8	14
9	5
10	9
11	3
12	4
$\Sigma$	123

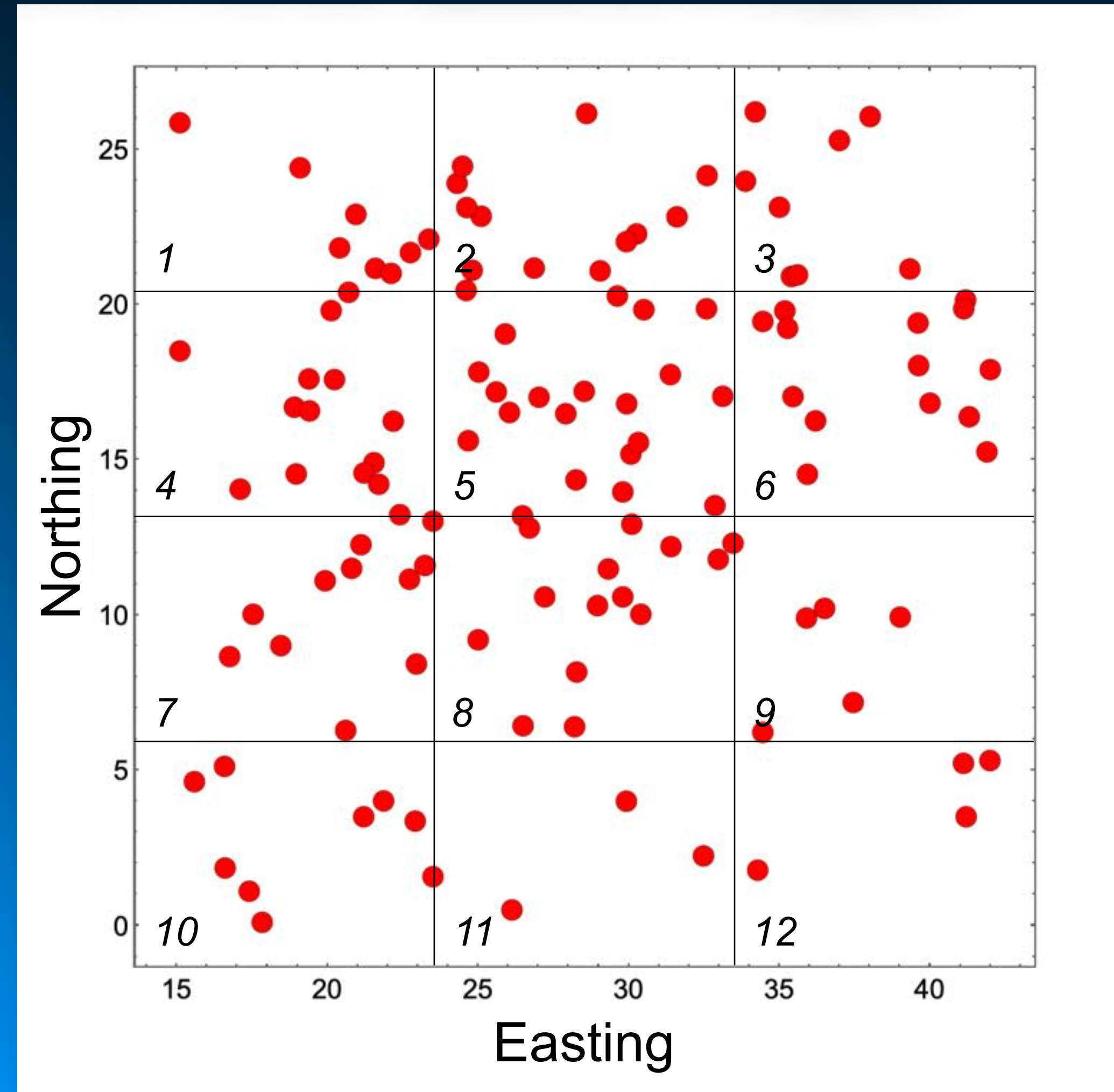


# Distribution of Points

## Test for Uniform Distribution of Points: Quadrat Analysis

### The Chi-Squared ( $\chi^2$ ) Test

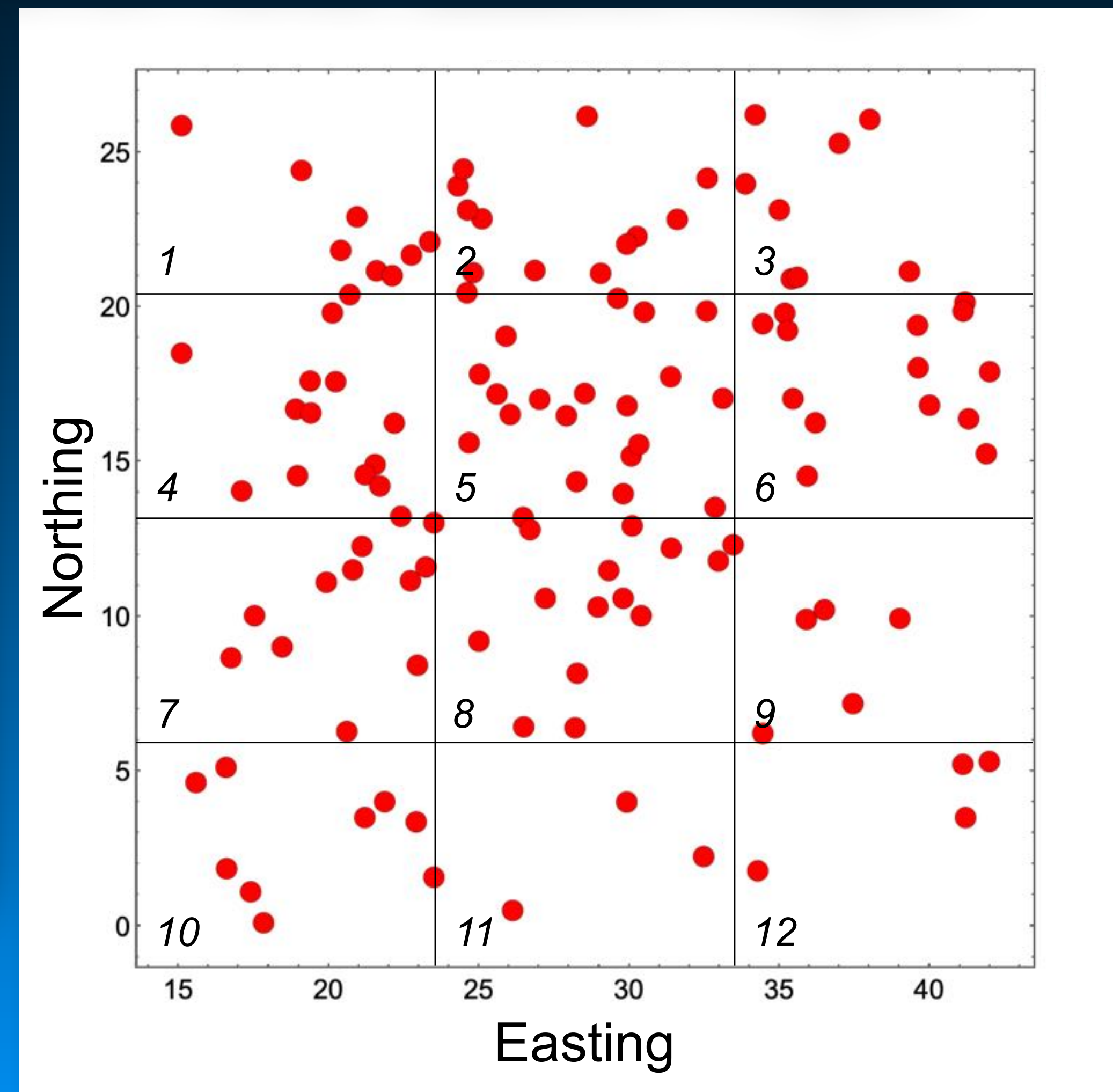
Statistical test to determine if there is a significant difference between observed and expected frequencies in categorical data. The  $\chi^2$  statistic can also be used to test for variable independence and whether the data fits a specific distribution (goodness-of-fit test).



# Distribution of Points

## Test for Uniform Distribution of Points: Quadrat Analysis

Cell	Obs.	Expect.	$(O-E)^2 / E$
1	8	10.25	0.49
2	13	10.25	0.74
3	8	10.25	0.49
4	14	10.25	1.37
5	20	10.25	9.27
6	14	10.25	1.37
7	11	10.25	0.05
8	14	10.25	1.37
9	5	10.25	2.69
10	9	10.25	0.15
11	3	10.25	5.13
12	4	10.25	3.81
$\Sigma$	123	123	26.95



# Distribution of Points

## Test for Uniform Distribution of Points: Quadrat Analysis

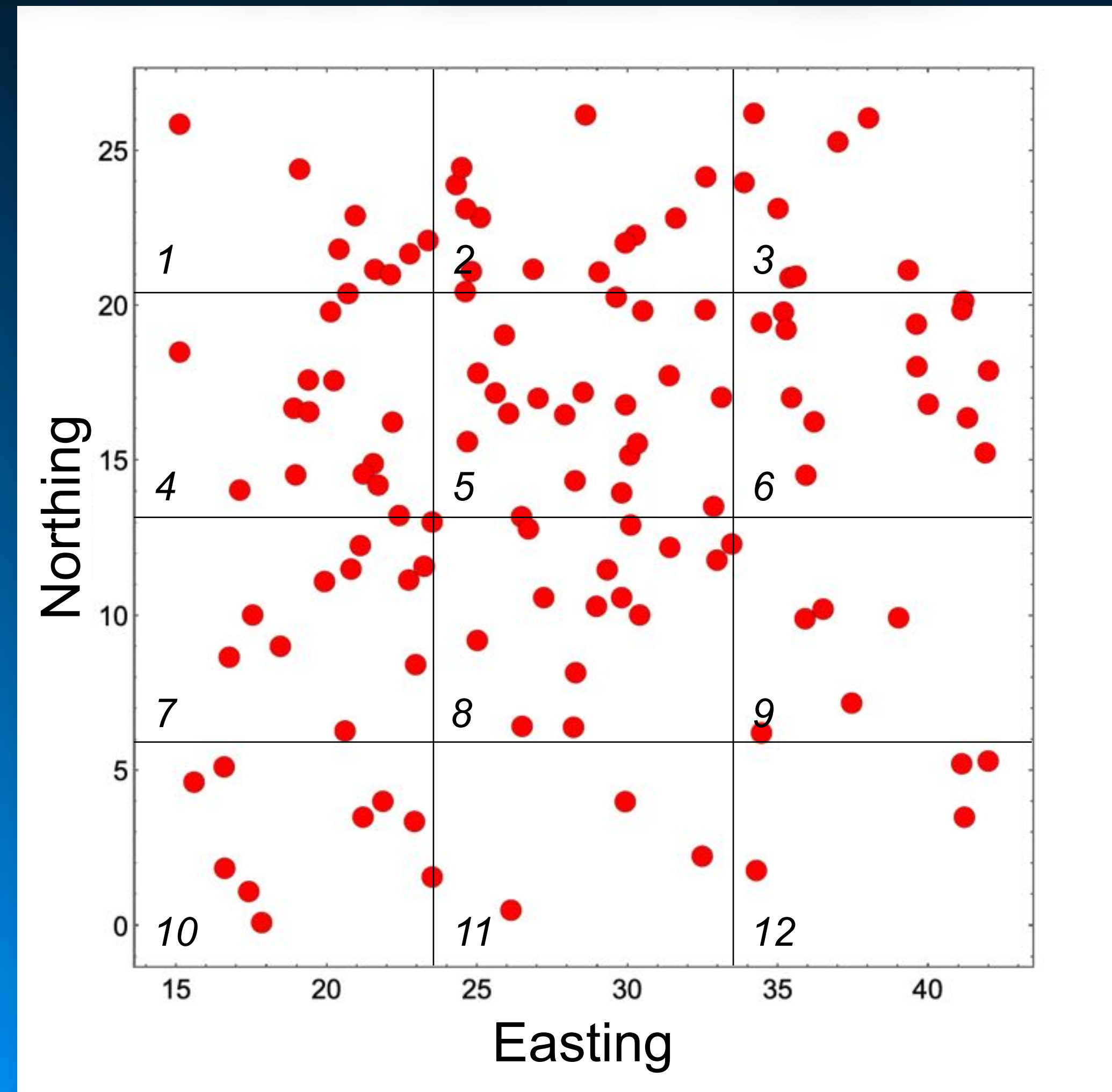
The Chi-Squared ( $\chi^2$ ) Test

$$\chi^2 = \sum_{i=1}^n \frac{(\text{Obs.} - \text{Exp.})^2}{\text{Exp.}}$$

$$\chi_{\alpha=0.05, \text{dof}=10}^2 = 18.31$$

$$\chi_{\text{obs.}}^2 = 26.95$$

Reject  $H_0$



# Distribution of Points

## Test for Uniform & Clustered Distribution of Points

### Morissita ( $I_\delta$ ) Test

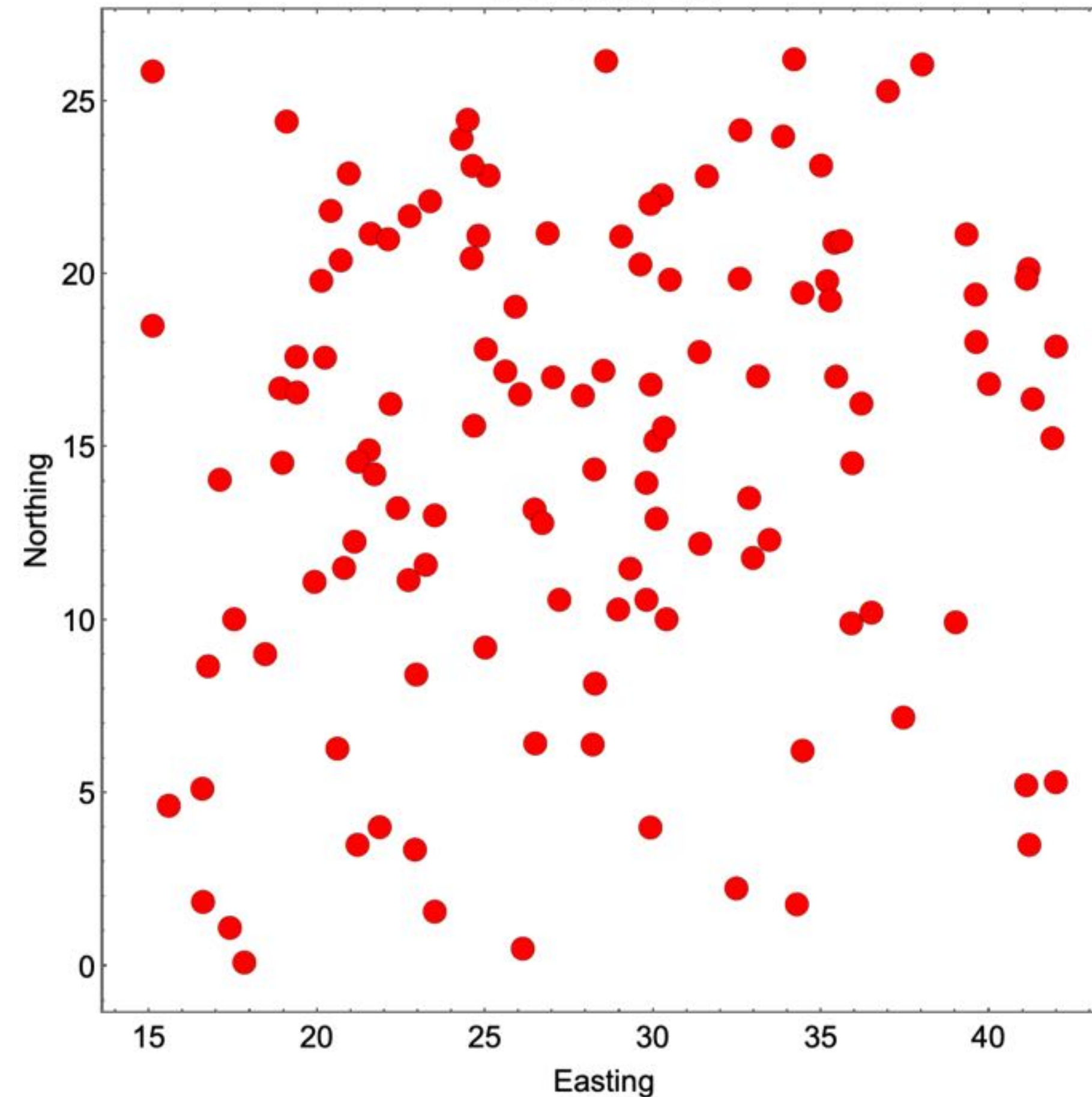
$$I_\delta = n \frac{\sum_{i=1}^n x^2 - \sum_{i=1}^n x}{(\sum_{i=1}^n x)^2 - \sum_{i=1}^n x}$$

$I_\delta < 1.0$  = Overdispersed Distribution

$I_\delta = 1.0$  = Random Distribution

$I_\delta > 1.0$  = Clustered Distribution

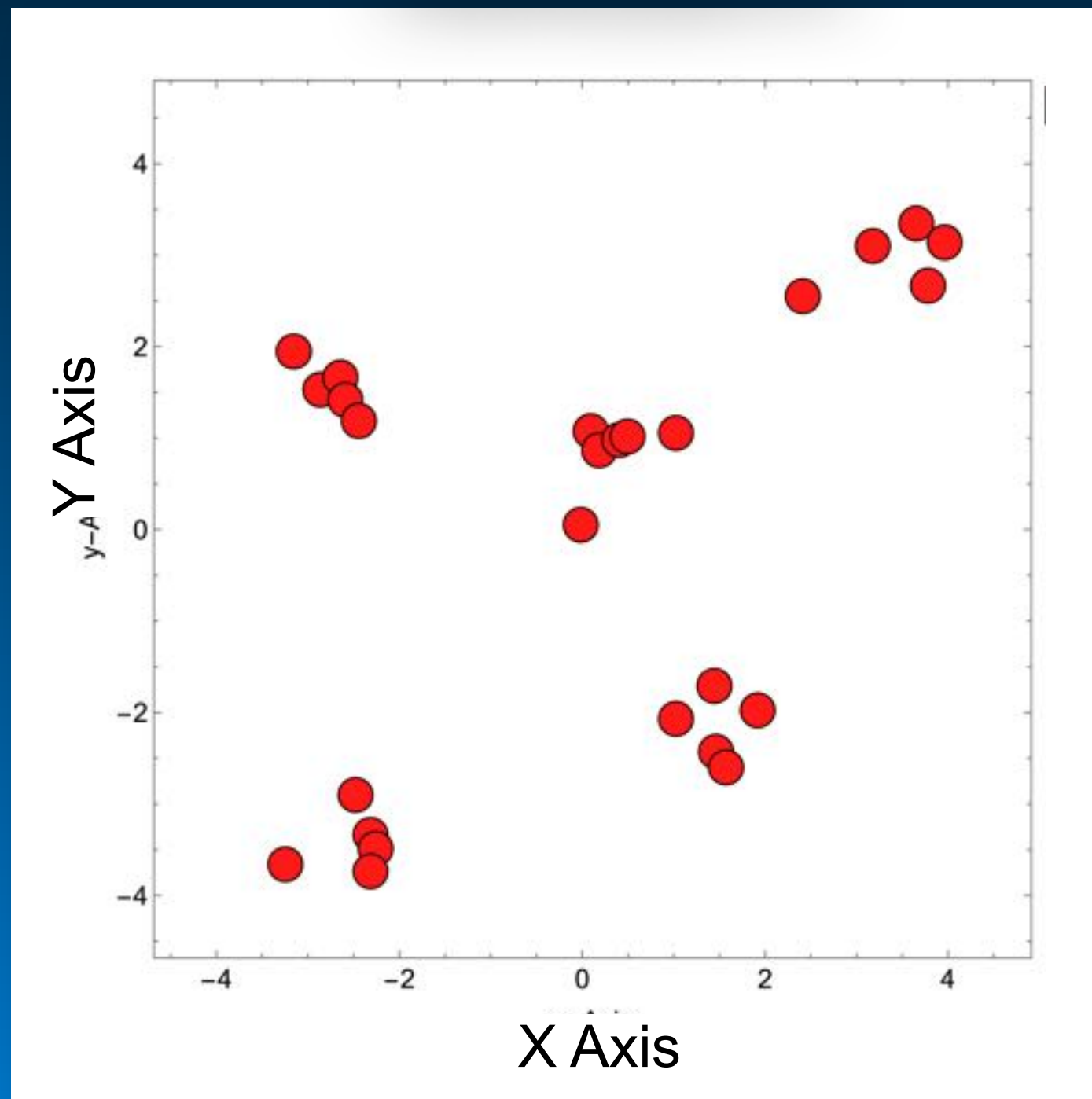
$$F_0 = \frac{I_\delta(\sum_{i=1}^n x - 1) + n - \sum_{i=1}^n x}{n - 1}$$



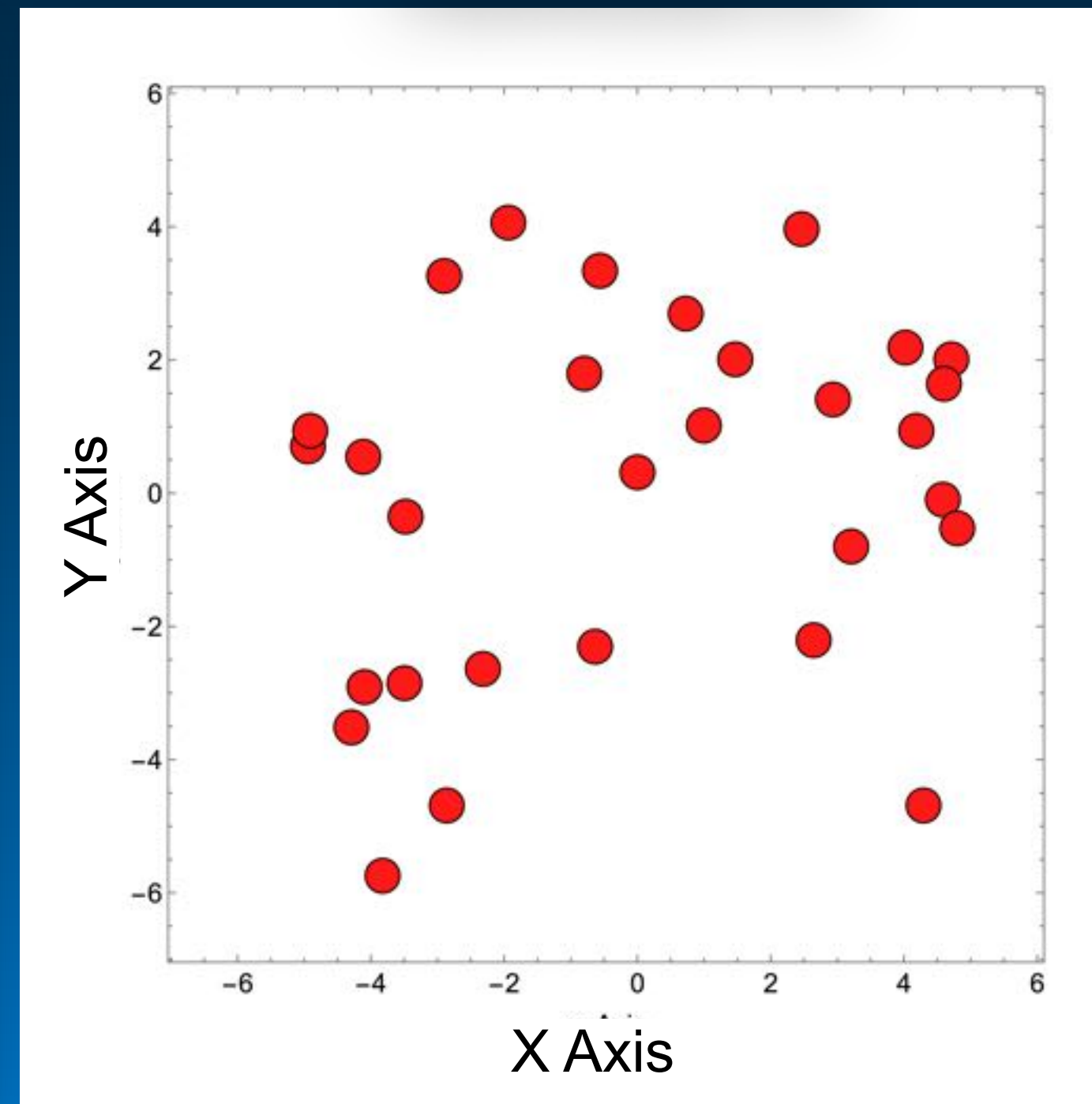
# Distribution of Points

## Test for a Clustered Distribution of Points: Nearest-Neighbor Analysis

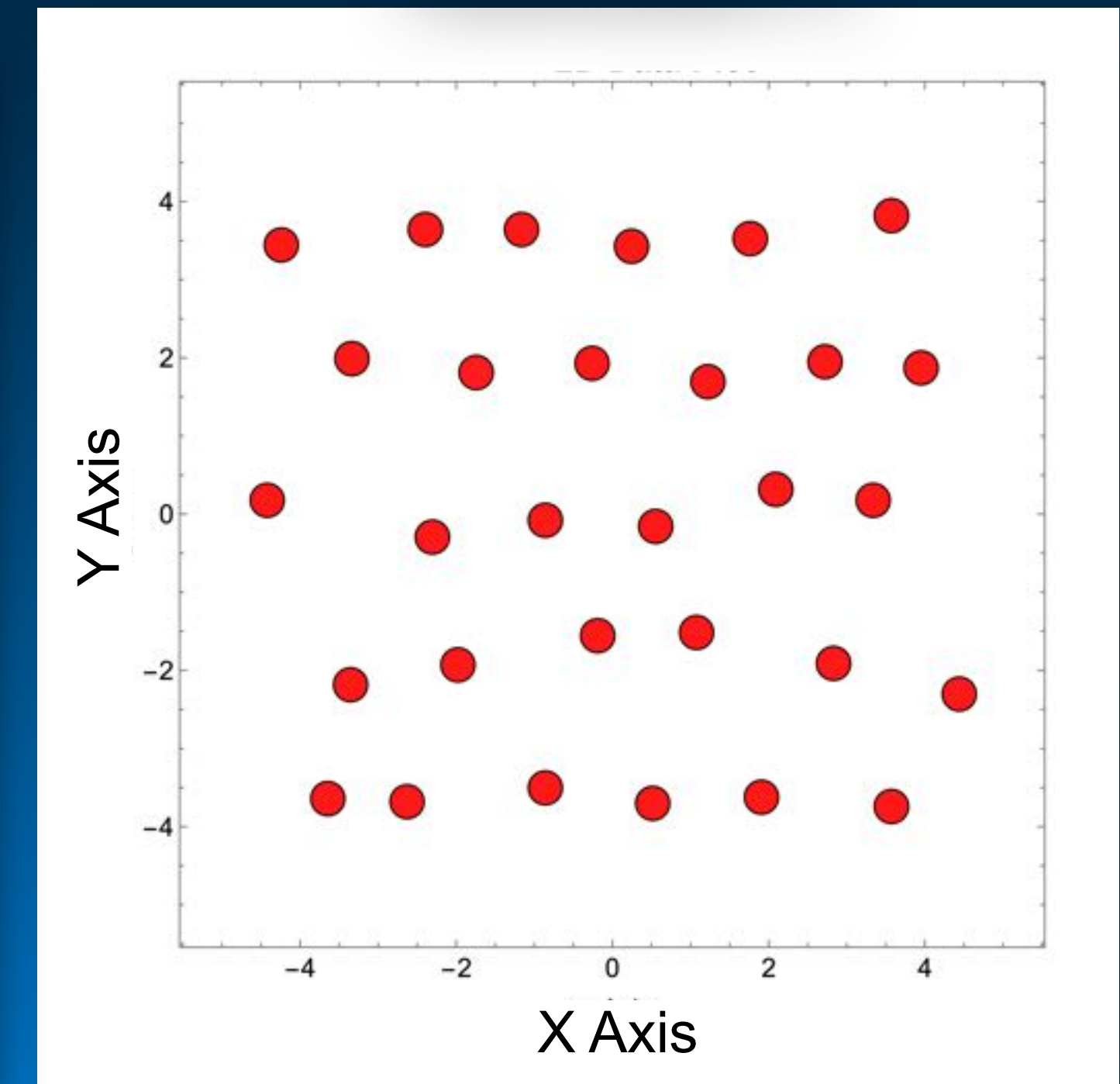
Distribution A



Distribution B



Distribution C



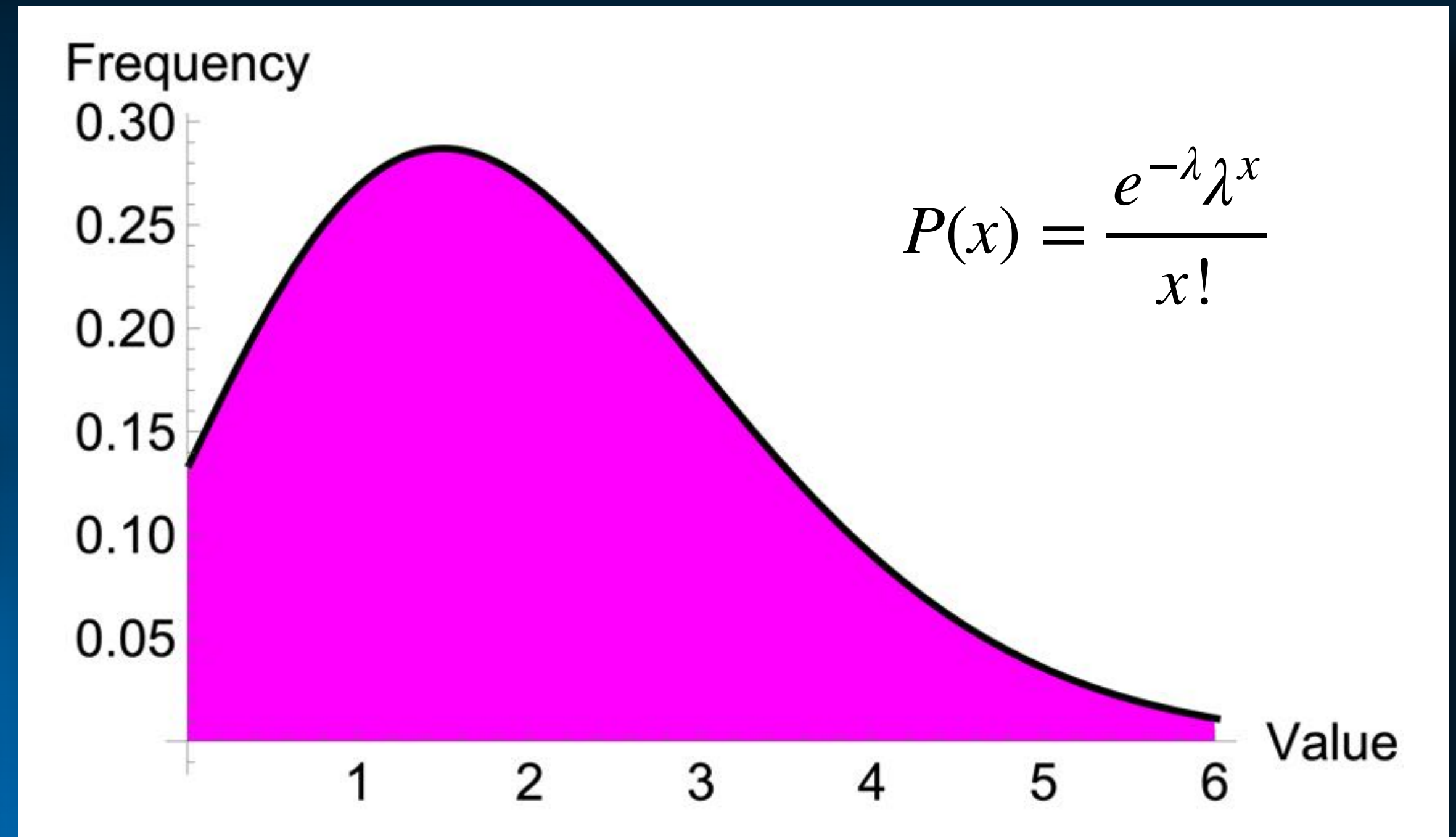
Tests also exist that forego the need to subdivide the space into quadrants. Let's compare the distributions of these three point sets and ask the question of the extent to which they exhibit clustering.

# Distribution of Points

## Poisson Distribution

The Poisson distribution tabulates the number of independent events ( $x$ ) that occur within a fixed interval given an average rate of occurrence ( $\lambda$ ). The Poisson distribution is useful for modeling distributions of points in space because it:

- assumes complete spatial independence (points don't attract or repel);
- places points at a constant rate (achieves homogeneity);
- works best for producing the occurrence of discrete events;
- effectively models the spatial distribution of rare occurrences.

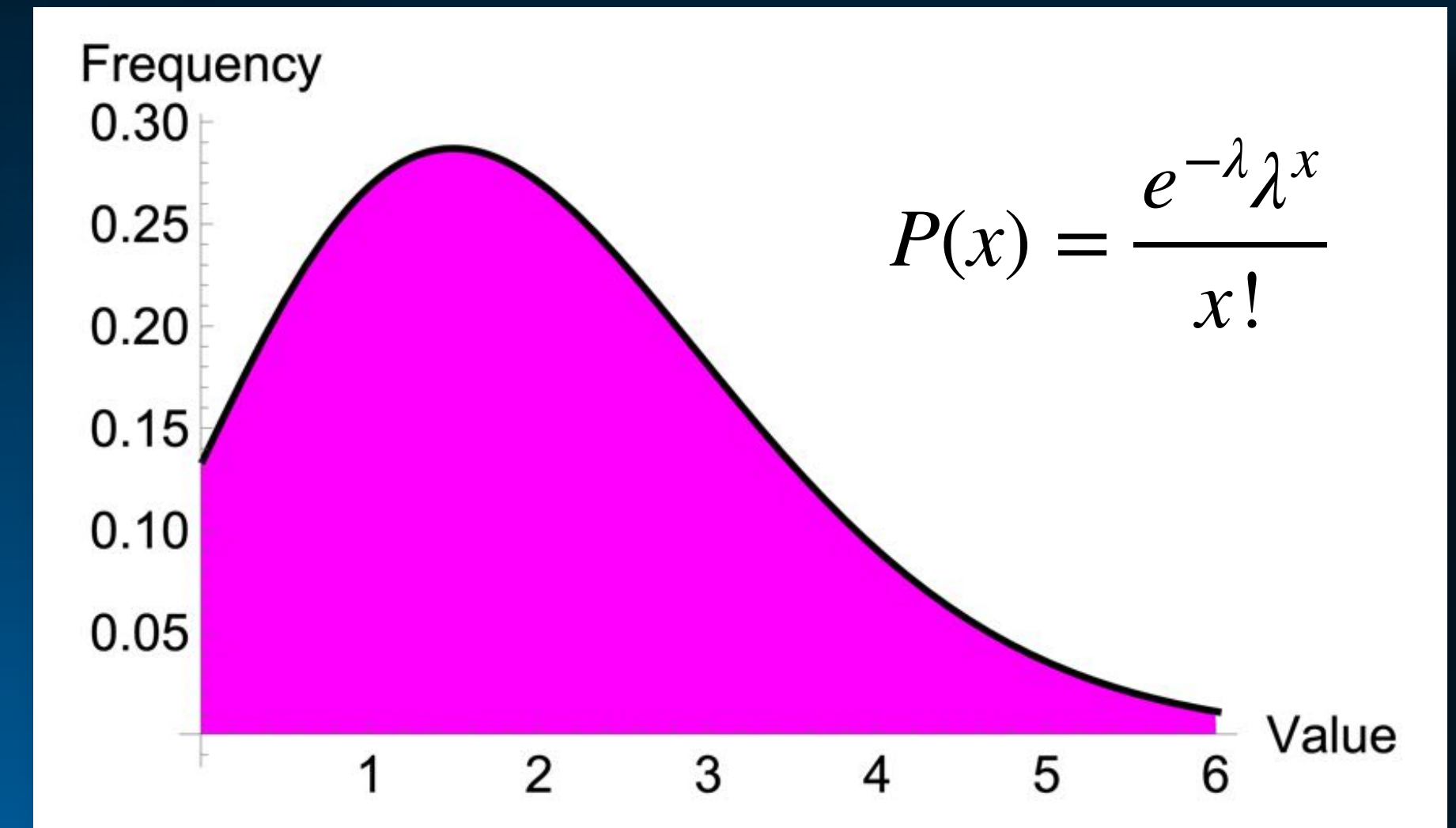


# Distribution of Points

## Nearest-Neighbor Analysis

The Poisson distribution supports nearest-neighbor analysis because, for any given area ( $A$ ) and sample size ( $n$ ) it allows estimation of the mean distance between any point and its nearest neighbor for a random sample.

$$\bar{\mu} = \frac{1}{2} \sqrt{\frac{A}{n}} \quad R = \frac{\bar{d}}{\bar{\mu}}$$



Once we have this estimate we can easily calculate the mean distance to the nearest neighbor ( $\bar{d}$ ) of all points in any distribution of points (in 2, 3, or  $m$  dimensions) and compare that value to this prediction. Clark and Evans (1954) expressed this as a ratio ( $R$ ).

# Distribution of Points

## Nearest-Neighbor Analysis

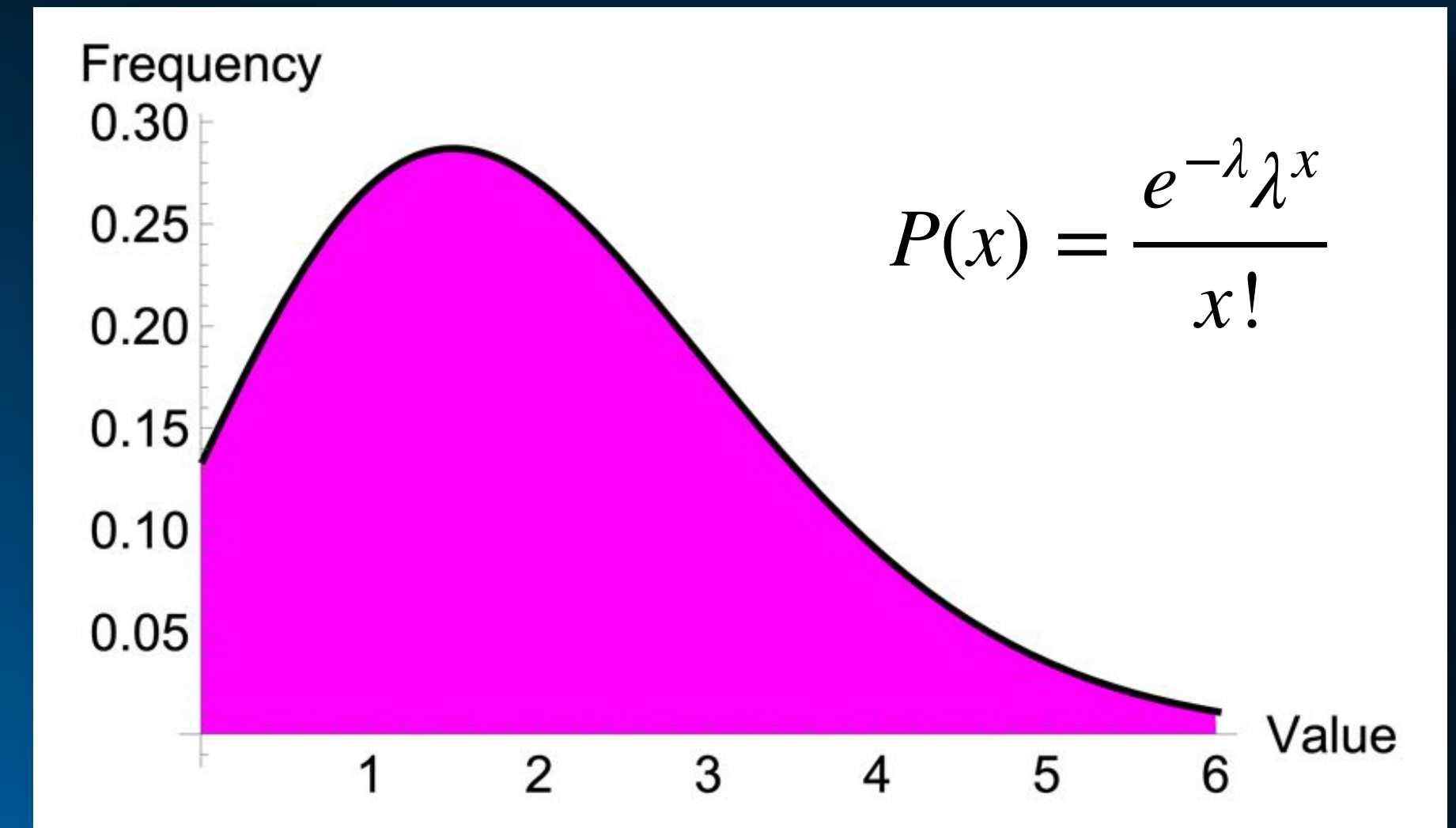
Clark and Evans'  $R$  varies between 0.0 (all points coincide) and c. 2.15 (all points spaced regularly in a hexagonal array).

If  $R < 0.0$  ,  $\bar{d} < \bar{u}$   $\rightarrow$  data are clustered.

If  $R = 0.0$  ,  $\bar{d} = \bar{u}$   $\rightarrow$  data are distributed randomly.

If  $R > 0.0$  ,  $\bar{d} > \bar{u}$   $\rightarrow$  data are dispersed.

Note, this test provides not only a means whereby we can identify when data exhibit a clustered character (as well as providing a definition of what clustered data are), it also provides a means whereby we can identify data that have a non-random dispersed character (as well as providing a definition of what dispersed data are).

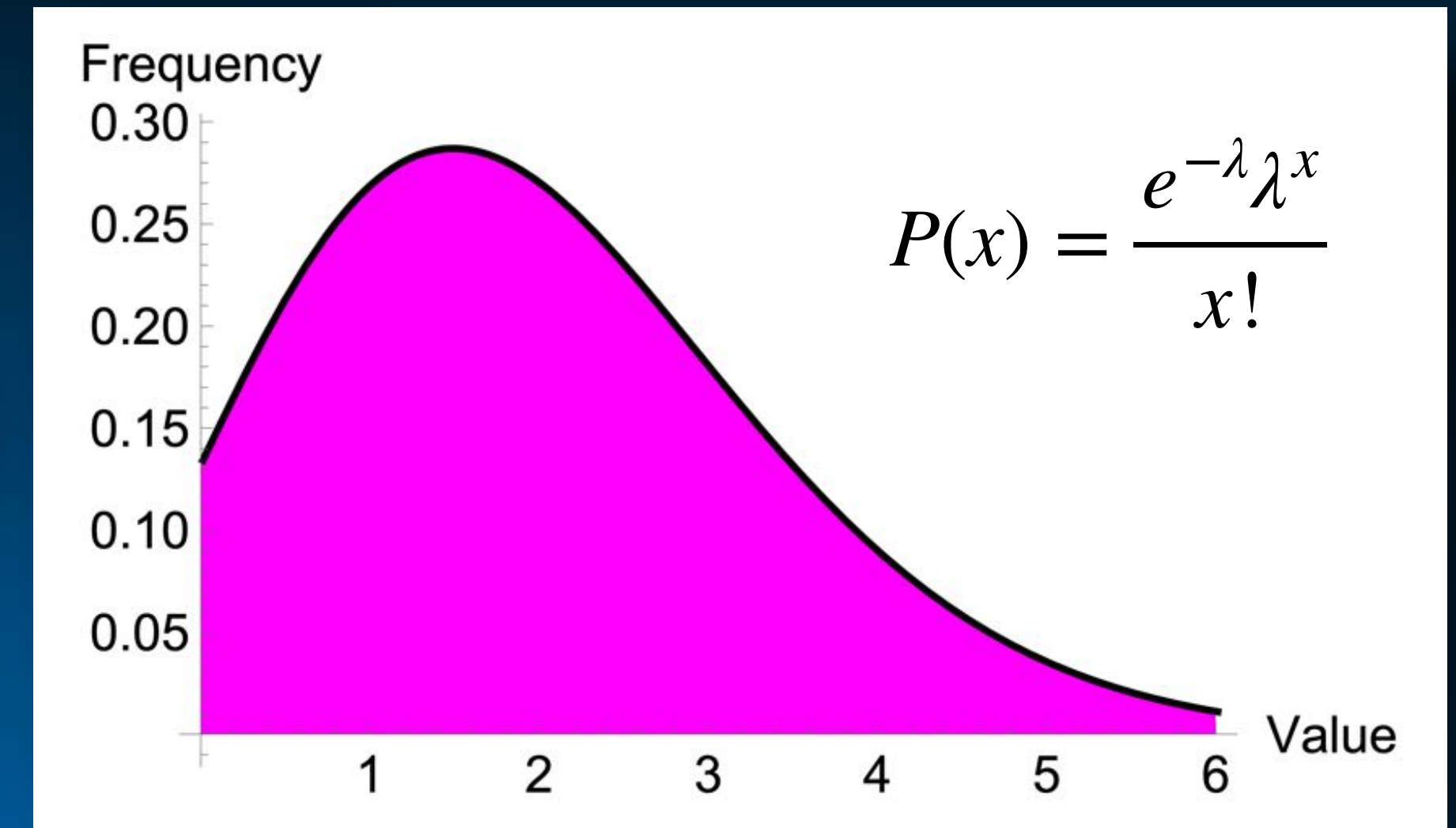


# Distribution of Points

## Nearest-Neighbor Analysis

The Poisson distribution also allows us to turn this relation into a parametric statistical test. To do this we need an estimate of the standard error for the estimate of the mean nearest-neighbor distance ( $s_e$ ).

$$s_e = \frac{\sqrt{(4 - \pi)A}}{2\sqrt{\pi n}} \quad R = \frac{\bar{d}}{\bar{u}}$$



Once we have this estimate we can easily calculate the associated probability ( $p$ ) value via reference to the standardized normal distribution ( $Z$  test). Note this test does not assume the data are normally distributed because (i.)  $\bar{u}$  is estimated from the Poisson distribution and (ii.)  $\bar{d}$  will be distributed normally via the CLT.

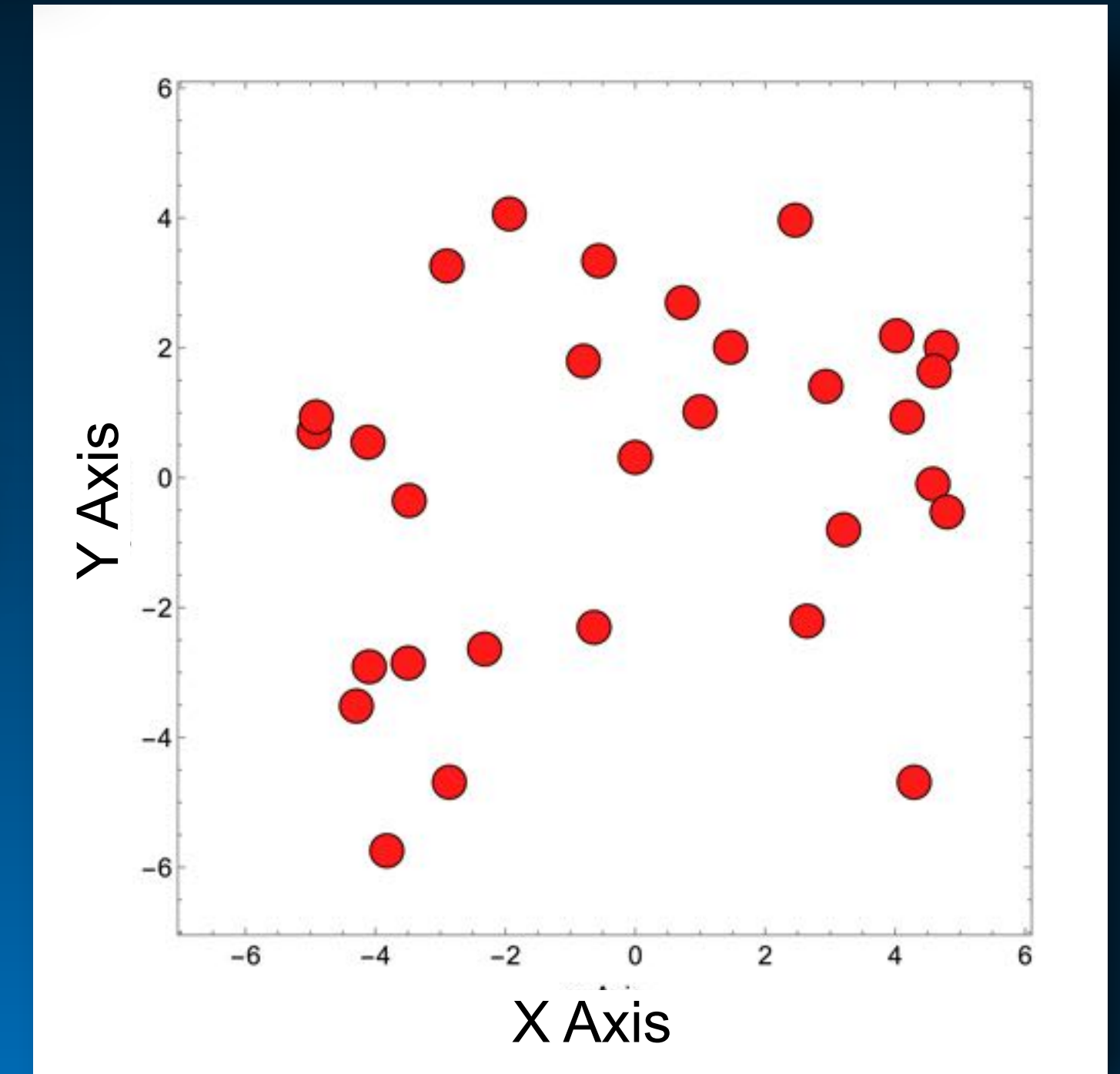
# Distribution of Points

## Nearest-Neighbor Analysis

One widely recognized problem with nearest-neighbor analysis is that points near the edge of the distribution have fewer neighbors than points close to the distribution's center. There are several potential solutions to this problem, the most commonly implemented of which is a set of correction factors for the estimate of the mean nearest-neighbor distance and its variance (see Donnelly, 1978) based on extensive simulations.

$$\bar{\delta} \approx \frac{1}{2} \sqrt{\frac{A}{n}} + \left(0.514 + \frac{0.412}{\sqrt{n}}\right) \frac{P}{n}$$

$$s_{\delta}^2 \approx 0.070 \frac{A}{n^2} + 0.035 P \frac{\sqrt{A}}{n^{\frac{5}{2}}}$$

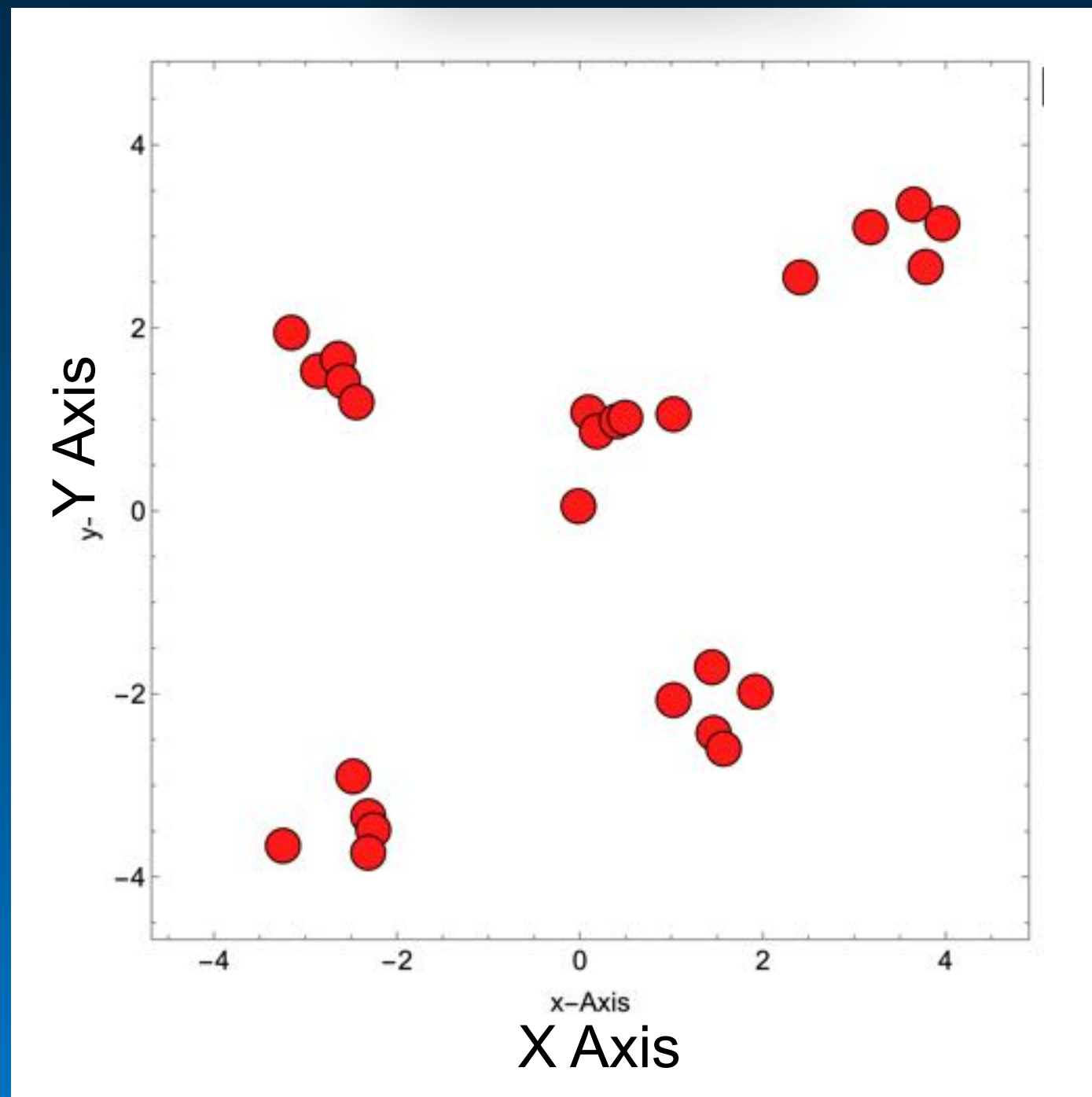


Note: in both these equations  $P$  is the perimeter of the boundary used to estimate  $A$ .

# Distribution of Points

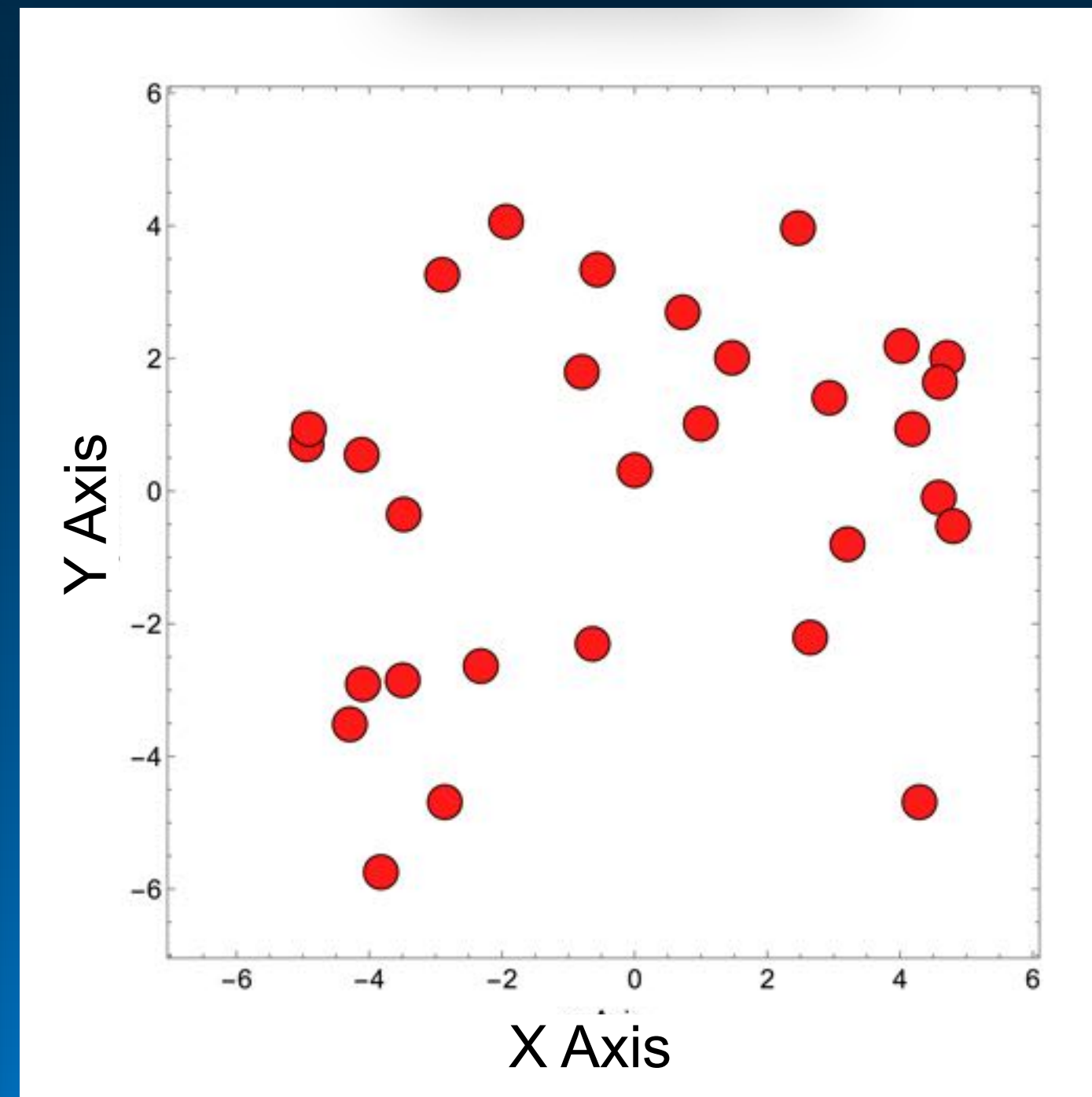
## Test for a Clustered Distribution of Points: Nearest-Neighbor Analysis

Distribution A



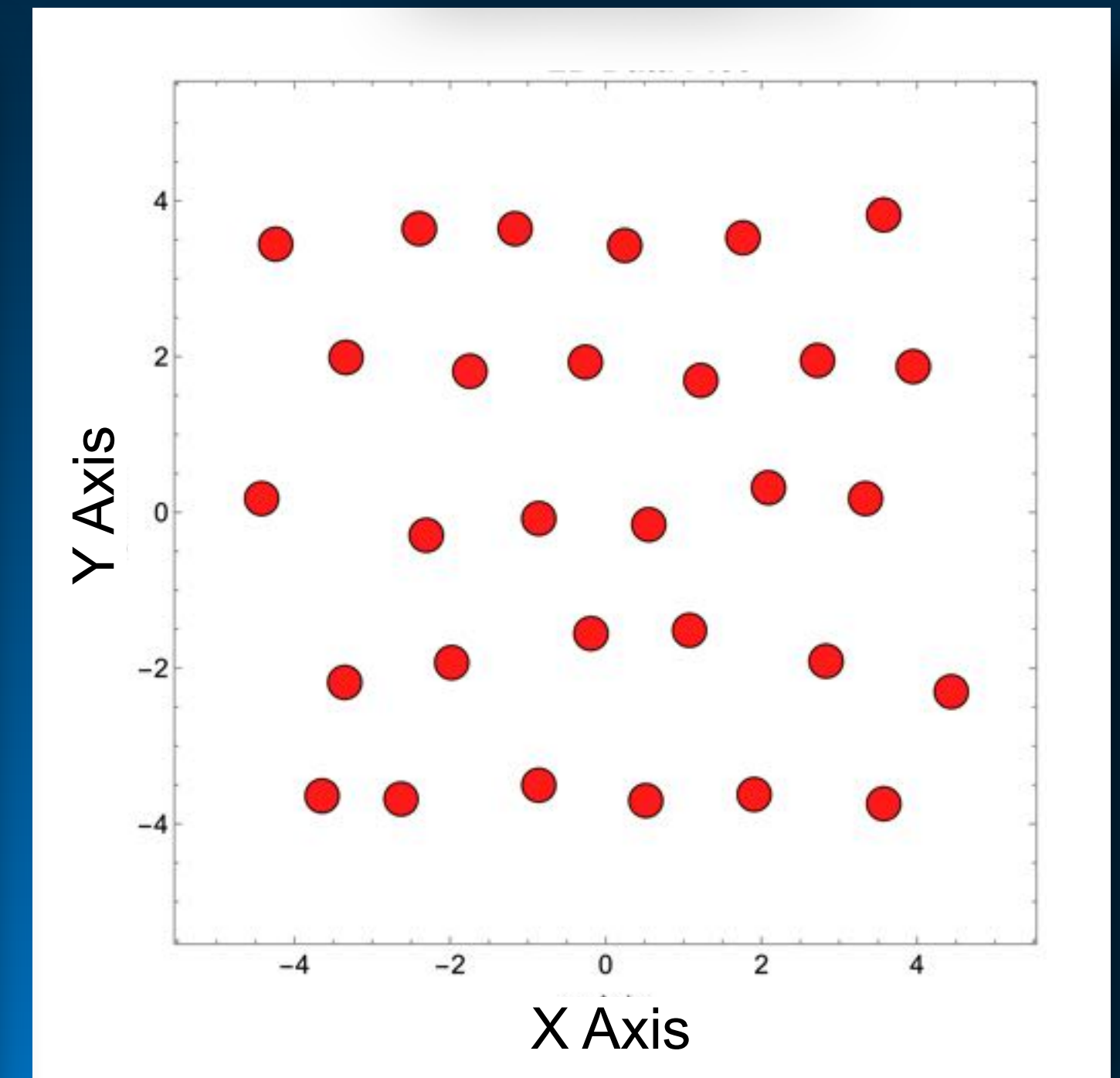
$$\begin{aligned}\bar{u} &= 0.574 & R &= 0.691 \\ \bar{d} &= 0.397 & z &= 3.017 \\ a &= 0.0013\end{aligned}$$

Distribution B



$$\begin{aligned}\bar{u} &= 0.811 & R &= 1.341 \\ \bar{d} &= 1.088 & z &= 3.570 \\ a &= 0.0001\end{aligned}$$

Distribution C



$$\begin{aligned}\bar{u} &= 0.712 & R &= 2.010 \\ \bar{d} &= 1.430 & z &= 10.581 \\ a &= 0.000000000\end{aligned}$$

# Analysis of Directional Data

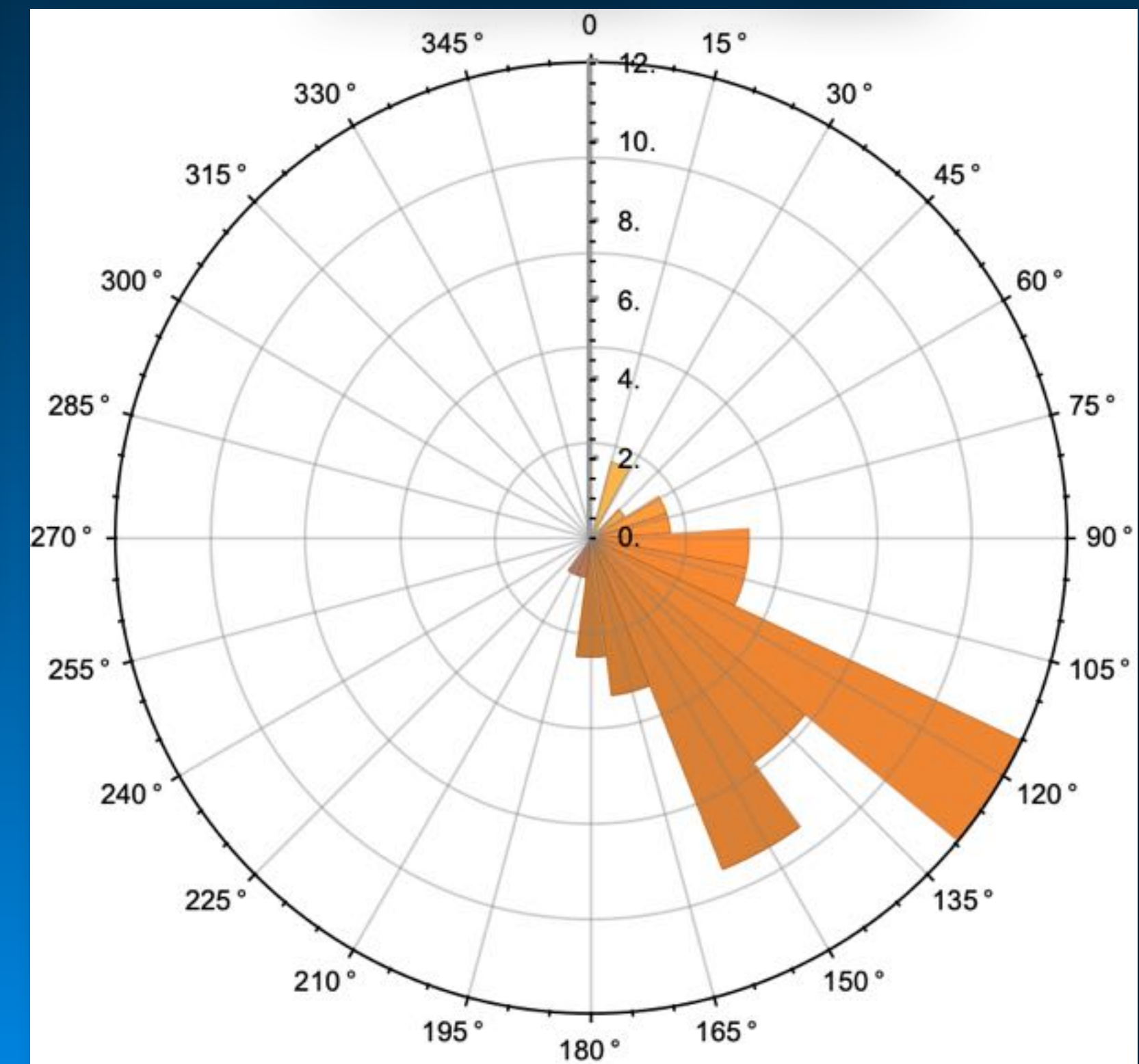
## Graphic Presentation of Directional Data

Striation	Angle (°)
1	23
2	27
3	53
4	58
5	64
6	83
7	85
8	88
9	93
10	99
11	100
12	105
13	113
14	113
15	114
16	117
17	121
18	123
19	125
20	126

Striation	Angle (°)
21	129
22	132
23	132
24	132
25	134
26	135
27	137
28	144
29	145
30	145
31	146
32	153
33	155
34	155
35	155
36	157
37	163
38	165
39	171
40	172

Striation	Angle (°)
41	129
42	132
43	132
44	132
45	134
46	135
47	137
48	144
49	145
50	145
51	146

Orientation of Glacial Striations in Southern Finland

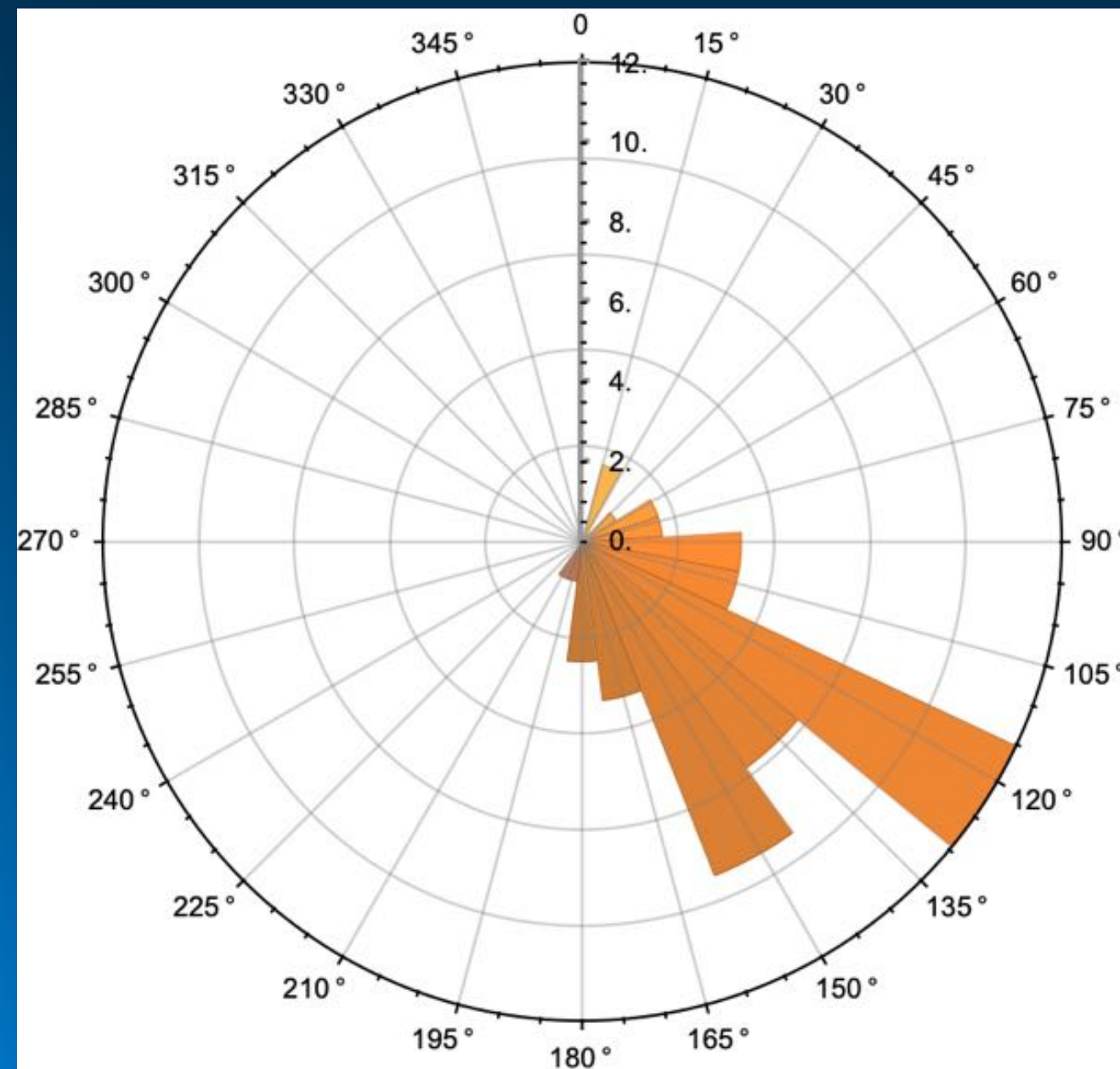


25 Bins

# Analysis of Directional Data

## Rayleigh's Test for a Preferred Trend

Orientation of Glacial Striations in Southern Finland



$$X_r = \sum_{i=1}^n \cos \theta_i \quad X_r = -25.7933$$

$$Y_r = \sum_{i=1}^n \sin \theta_i \quad Y_r = 31.6367$$

$$R = \sqrt{X_r^2 + Y_r^2} \quad R = 40.8188$$

$$\bar{R} = R/n \quad \bar{R} = 0.8004$$

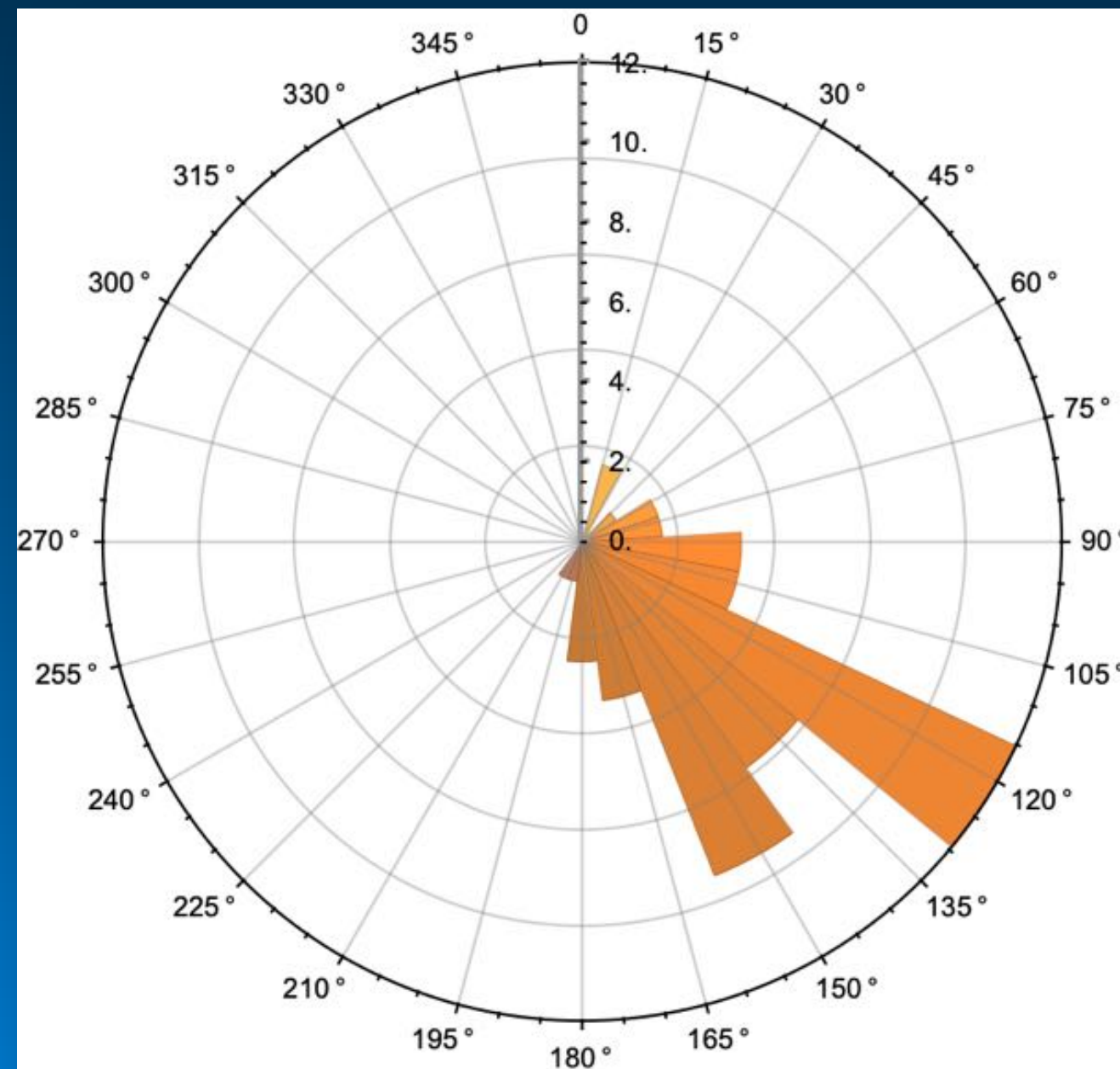
$$\bar{R}_{\alpha=0.05, n=51} = 0.2981$$

Reject  $H_0$  at  $\alpha = 0.05$ . The data exhibit a preferred orientation.

# Analysis of Directional Data

## Rayleigh's Test for Comparison to a Specific Trend

### Orientation of Glacial Striations in Southern Finland



This test can be made exact, but this requires the use of extensive charts to enable setting of the correct critical value (Stephens, 1969). An alternative, approximate approach is to calculate the confidence interval on the mean vector direction and use that as a standard to which any specific trend might be compared.

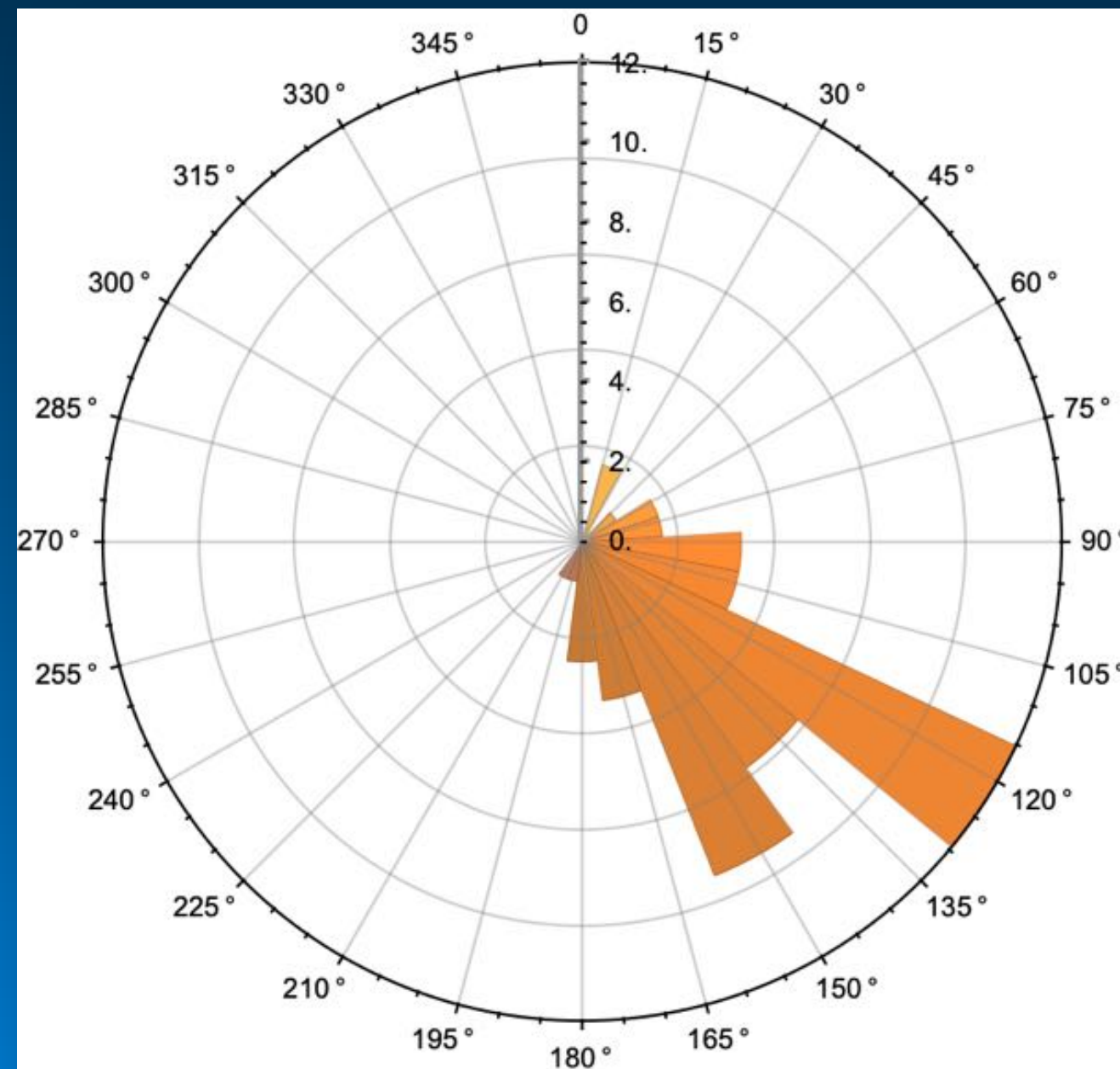
Mean Vector:  $\bar{\theta} = \tan^{-1}(Y_r/X_r)$

Standard Error:  $s_e = \frac{1}{\sqrt{2n\bar{R}\kappa}}$

# Analysis of Directional Data

## Rayleigh's Confidence-Interval Test for Comparison to a Specific Trend

### Orientation of Glacial Striations in Southern Finland



$$\bar{\theta} = \tan^{-1}(Y_r/X_r)$$

$$\bar{\theta} = 129.19^\circ$$

$$s_e = \frac{1}{\sqrt{2n\bar{R}\kappa}}$$

$$s_e = 5.2924^\circ$$

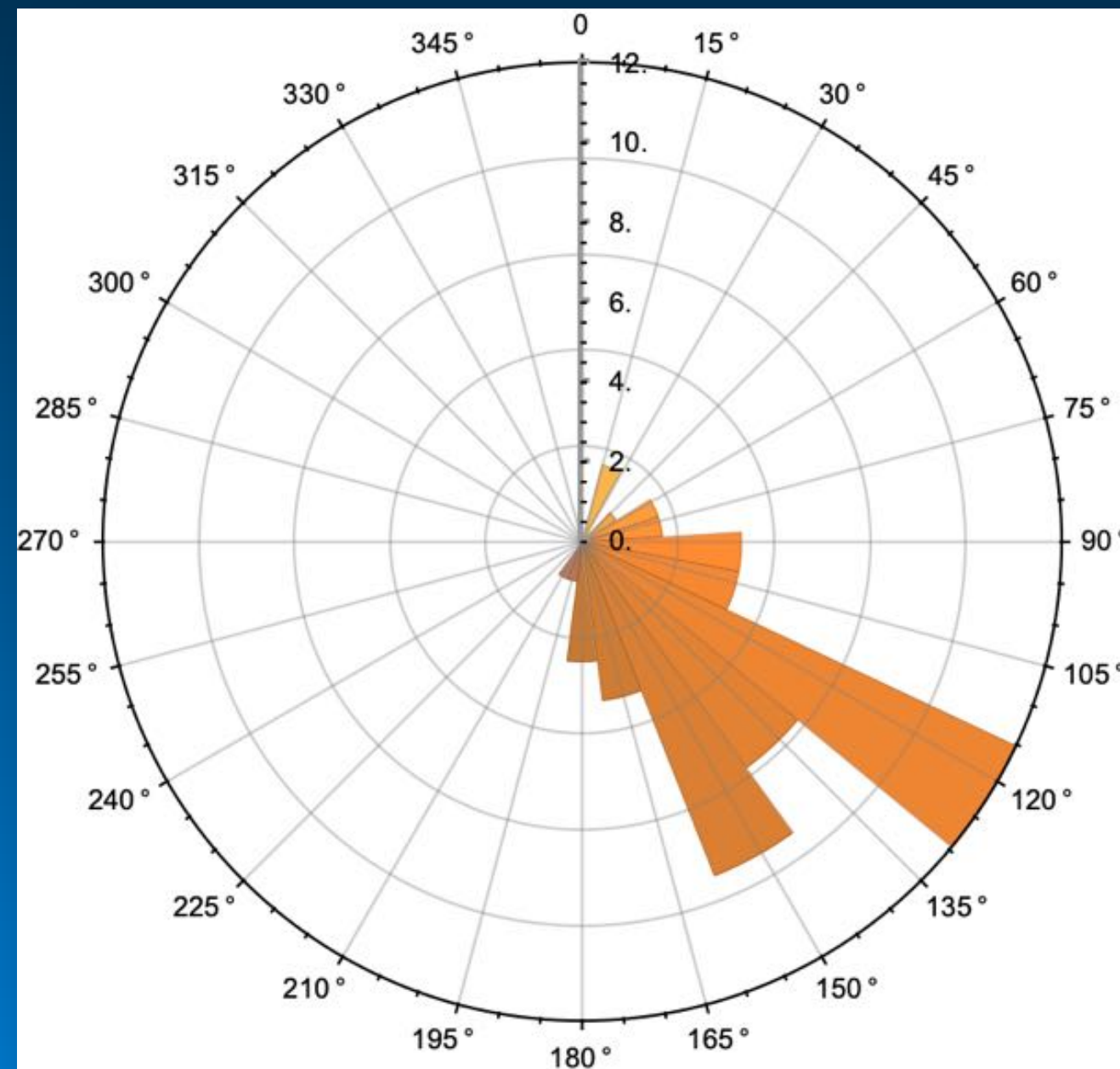
$$CI_{\alpha=0.05} = Z_{\alpha} s_e$$

$$CI_{\alpha=0.05} = 123.898^\circ - 134.483^\circ$$

# Analysis of Directional Data

## V Test for Comparison to a Specific Trend

Orientation of Glacial Striations in Southern Finland



$$V = \frac{1}{n} \sum_{i=0}^n \cos(\theta_i - \mu_0)$$

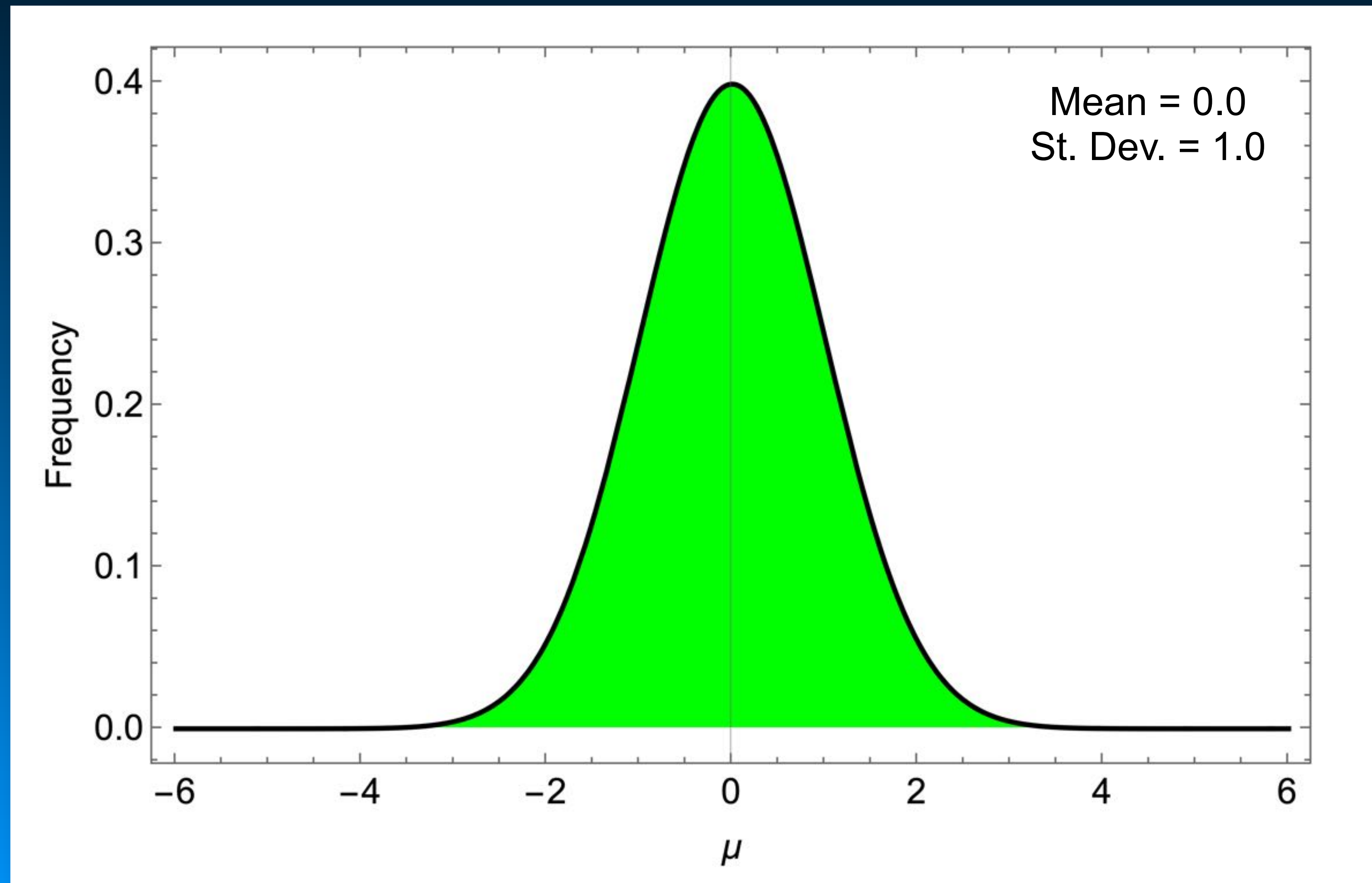
Where:  $\mu_0$  - specific trend angle.

$$\bar{R} = \sqrt{\left(\frac{1}{n} \sum_{i=1}^n \cos(\theta_i)\right)^2 + \left(\frac{1}{n} \sum_{i=1}^n \sin(\theta_i)\right)^2}$$

$$u = \bar{R} \cdot \sqrt{2n} \cdot \cos(\bar{\theta} - \mu_0)$$

# Analysis of Directional Data

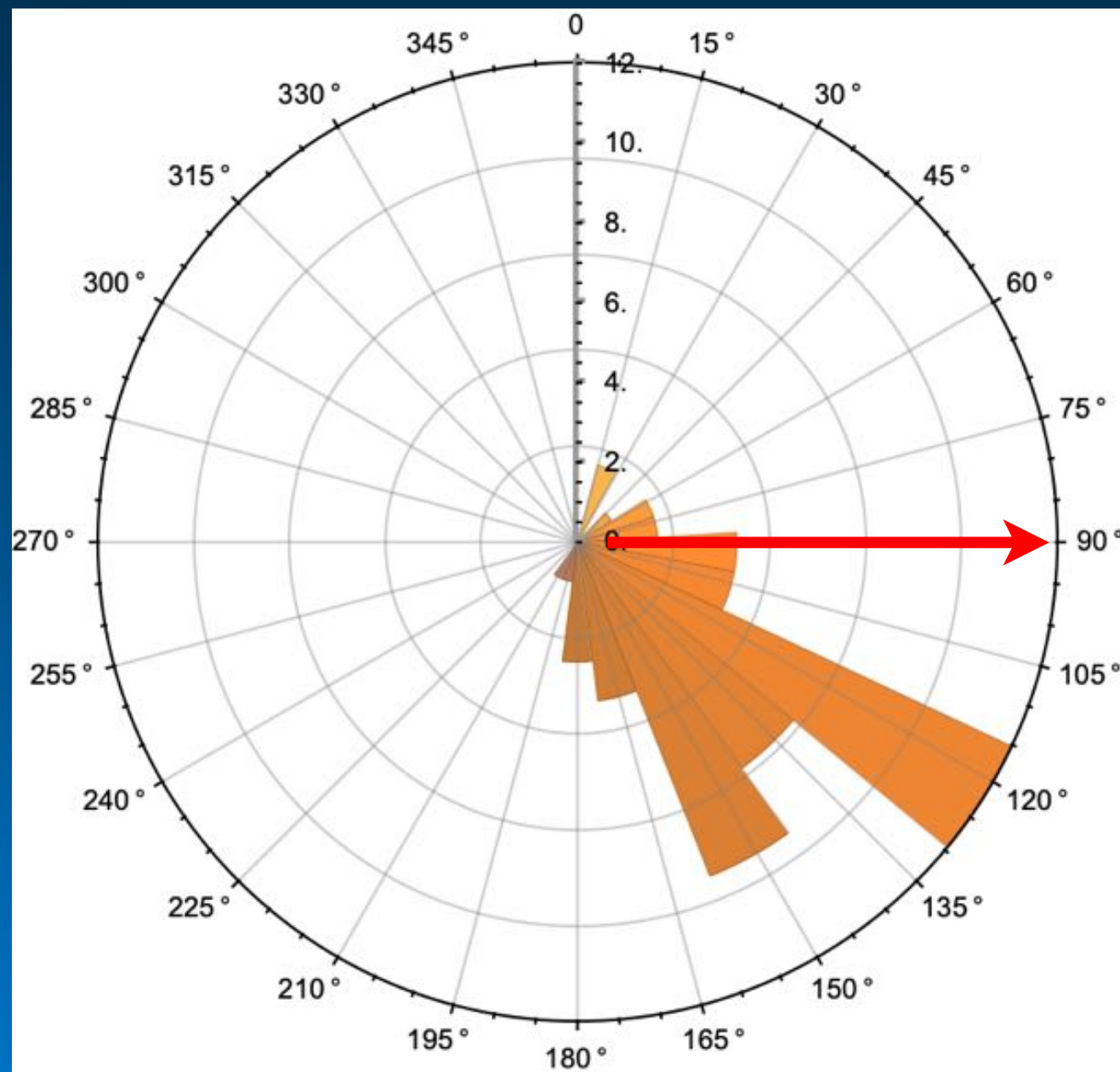
V Test is Referenced to the Standard Normal Distribution



# Analysis of Directional Data

## V Test for Comparison to a Specific Trend: Example

Orientation of Glacial  
Striations in Southern Finland



$$\mu_0 = 90^\circ$$

$$V = \frac{1}{n} \sum_{i=0}^n \cos(\theta_i - \mu_0)$$

$$V = 0.6203$$

$$\bar{R} = \sqrt{\left(\frac{1}{n} \sum_{i=1}^n \cos(\theta_i)\right)^2 + \left(\frac{1}{n} \sum_{i=1}^n \sin(\theta_i)\right)^2}$$

$$\bar{R} = 0.3385$$

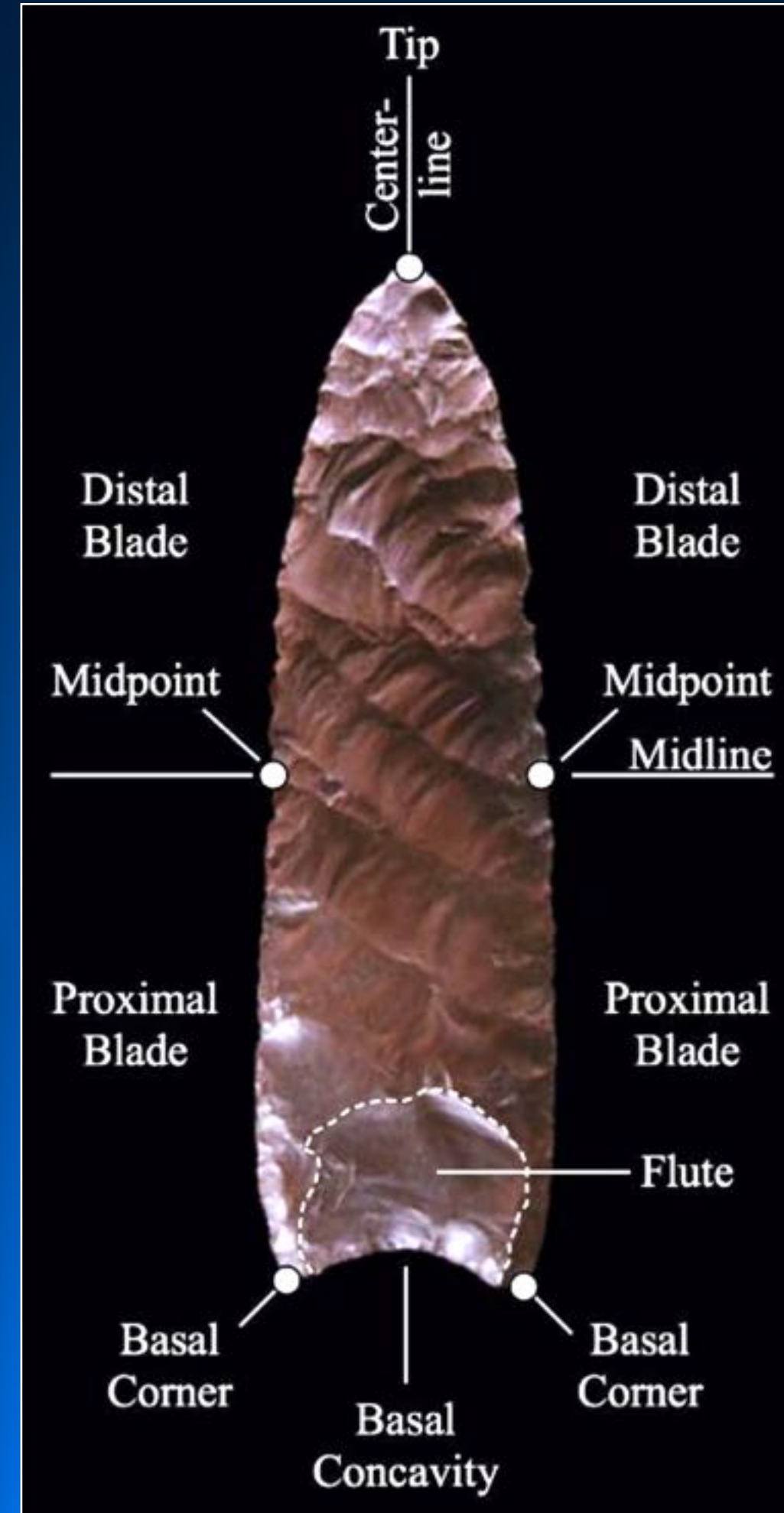
$$u = \bar{R} \cdot \sqrt{2n} \cdot \cos(\bar{\theta} - \mu_0)$$

$$u = 2.7761$$

$$\alpha = 0.9967$$

# Lab Practical Assignment V

## Morphometrics & Spatial Data Analysis

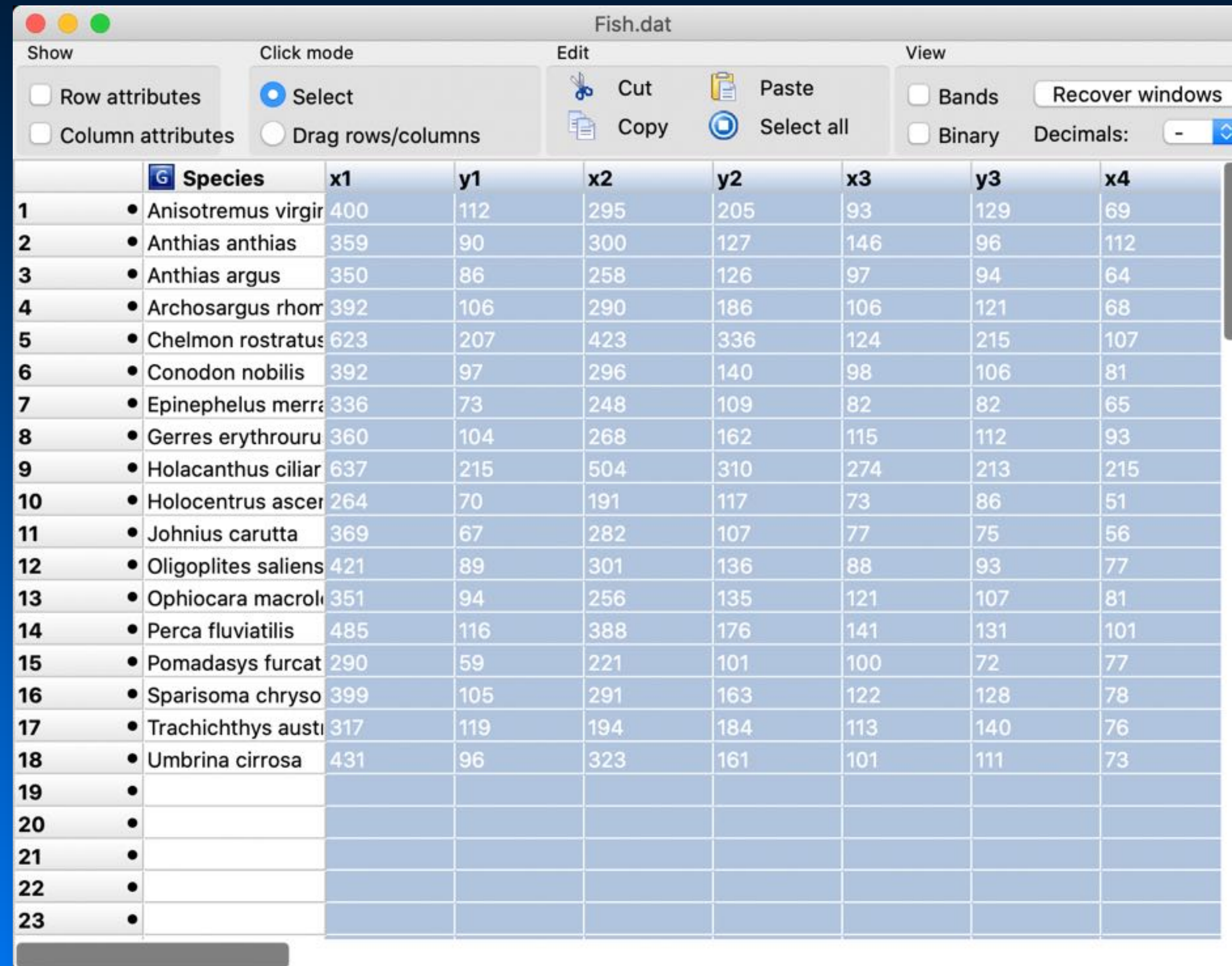


# Lab Practical Assignment V

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# Lab Practical Assignment IV

## Correspondence Analysis (CA) in PAST



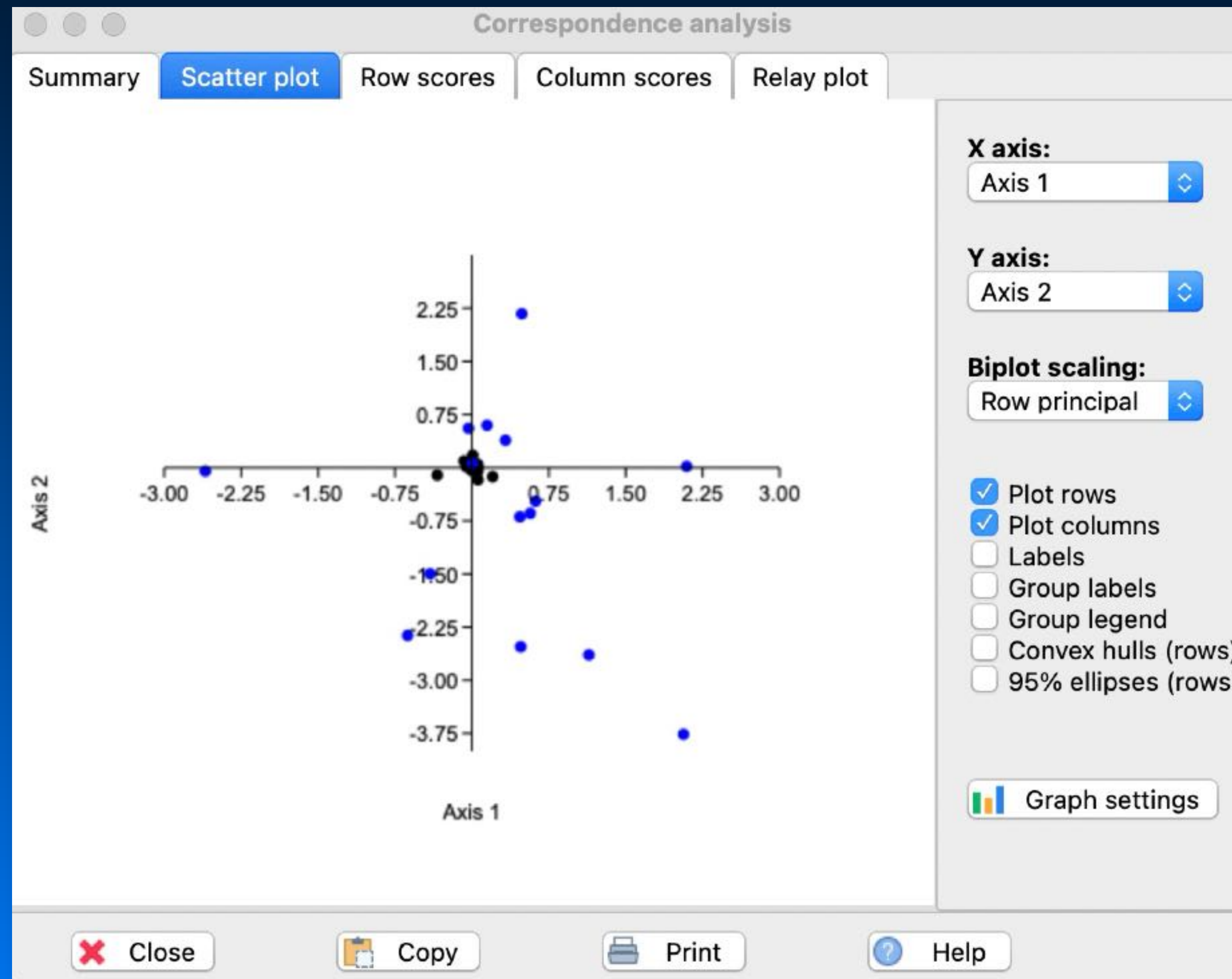
The screenshot shows the PAST software interface with a data table titled 'Fish.dat'. The table has 18 rows and 8 columns. The columns are labeled 'Species', 'x1', 'y1', 'x2', 'y2', 'x3', 'y3', and 'x4'. The rows contain species names and their corresponding values for each variable. The interface also includes a menu bar with options like 'Show', 'Click mode', 'Edit', and 'View', and a toolbar with icons for 'Cut', 'Copy', 'Paste', and 'Select all'.

	Species	x1	y1	x2	y2	x3	y3	x4
1	• Anisotremus virgatus	400	112	295	205	93	129	69
2	• Anthias anthias	359	90	300	127	146	96	112
3	• Anthias argus	350	86	258	126	97	94	64
4	• Archosargus rhomboidalis	392	106	290	186	106	121	68
5	• Chelmon rostratus	623	207	423	336	124	215	107
6	• Conodon nobilis	392	97	296	140	98	106	81
7	• Epinephelus merra	336	73	248	109	82	82	65
8	• Gerres erythroureus	360	104	268	162	115	112	93
9	• Holacanthus ciliaris	637	215	504	310	274	213	215
10	• Holocentrus asper	264	70	191	117	73	86	51
11	• Johnius carutta	369	67	282	107	77	75	56
12	• Oligoplites saliens	421	89	301	136	88	93	77
13	• Ophiocara macrolepis	351	94	256	135	121	107	81
14	• Perca fluviatilis	485	116	388	176	141	131	101
15	• Pomadasys furcatus	290	59	221	101	100	72	77
16	• Sparisoma chrysopterygion	399	105	291	163	122	128	78
17	• Trachichthys australis	317	119	194	184	113	140	76
18	• Umbrina cirrosa	431	96	323	161	101	111	73
19	•							
20	•							
21	•							
22	•							
23	•							



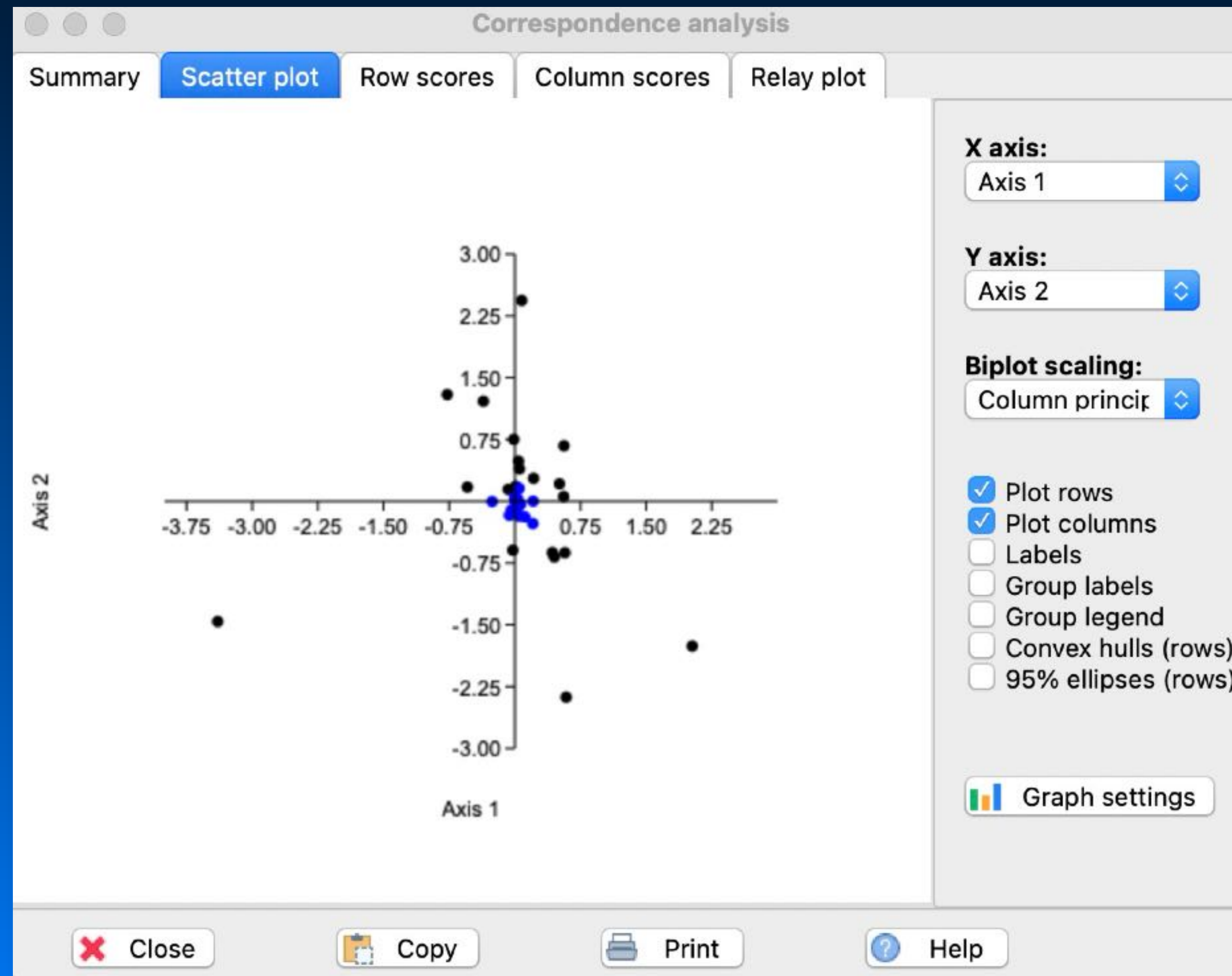
# Lab Practical Assignment IV

## Correspondence Analysis (CA) in PAST



# Lab Practical Assignment IV

## Correspondence Analysis (CA) in PAST



# Lab Practical Assignment IV

## Correspondence Analysis (CA) in PAST

Correspondence analysis

Summary Scatter plot Row scores Column scores Relay plot

	Axis 1	Axis 2	Axis 3	Axis 4	Axis 5	Axis 6	Axis 7
Anisotremu	0.428941	-0.623339	-1.18863	-0.691429	0.0640283	0.123041	0.206876
Anthias antl	-0.772099	1.29508	0.0745189	-0.763146	-0.555875	0.963312	-1.29872
Anthias arg	0.214153	0.277894	0.532644	0.290636	0.0946202	-0.85502	0.74243
Archosargu	-0.0231584	-0.594056	0.713386	-0.336355	0.744103	-0.852494	0.958767
Chelmon ro	0.585829	-2.37852	-2.44617	1.2247	2.22573	0.71357	-0.08096
Conodon no	-0.0750732	0.144131	0.322876	1.18735	0.0227208	-1.01525	-0.59383
Epinephelus	-0.0120463	0.750241	-0.185678	1.28241	0.644586	-2.37598	-0.77855
Gerres erytl	0.558052	0.0571966	-0.938088	-1.23159	0.955982	-0.0587613	0.168408
Holacanthu	-3.39368	-1.4601	0.14124	-0.769842	0.0770166	-0.254558	0.167149
Holocentrus	0.509518	0.211664	-1.05658	-0.513393	-0.650864	0.170772	-0.05765
Johnius car	-0.359458	1.2136	0.362347	1.21756	0.275235	-2.23329	-0.54889
Lonchurus l	0.0781638	2.43765	-1.51518	-1.20932	0.607941	0.0184996	-0.24819
Oligoplites	0.0415191	0.486424	2.00956	0.842686	2.39464	1.37649	-0.38717
Ophiocara n	0.561366	0.673332	1.57496	-0.333736	0.233144	1.53931	2.40185
Perca fluvia	0.010096	0.180316	0.530167	0.679371	-1.47605	-0.35476	1.48998
Pomacentru	-0.541987	0.171298	0.831647	-0.591197	0.314744	0.866411	-1.51888
Pomadasys	0.451729	-0.676219	-0.0171987	0.92956	-1.19529	0.909109	-1.07592
Sparisoma c	0.57168	-0.625106	-0.775374	0.57192	0.601923	0.303605	1.14385
Trachichthy	2.02615	-1.75782	1.92227	-2.77288	-0.184818	-1.53884	-1.12847

Close Copy Print Help

# Lab Practical Assignment IV

## Correspondence Analysis (CA) in PAST

Correspondence analysis

Summary Scatter plot Row scores **Column scores** Relay plot

	Axis 1	Axis 2	Axis 3	Axis 4	Axis 5	Axis 6	Axis 7
Pre-Orbit Le	0.0474775	-0.182296	-0.156216	0.0742287	0.123059	0.0293501	0.0221414
Head Length	0.0466845	-0.0500687	-0.0244075	0.00938765	-0.0569188	0.0288396	0.0239833
Pre-Dorsal L	0.208871	0.00123279	0.0562029	-0.0129859	0.0696972	-0.0204981	-0.0173962
Pre-Pectoral L	0.0567217	-0.0465127	-0.0600497	0.0259171	-0.0042464	0.0201656	-0.0285902
Pre-Pelvic L	0.0618946	-0.0341045	-0.0666588	0.0607289	-0.0621742	0.0341176	-0.0176317
Pre-Anal Le	0.00066602	0.00364572	-0.0260186	0.0167667	-0.0617167	-0.062964	0.00833159
Standard Le	0.0326823	0.0279091	0.02848	0.033805	0.0147693	0.00134247	0.00913006
Fork Length	-0.0032994	0.0400337	0.0110395	0.0090198	0.0199935	-0.0190263	0.0202197
Total Length	0.0146826	0.0430804	0.0262531	-0.0032032	-0.0043100	0.023796	-0.023757
Snout Length	0.113773	-0.190597	-0.113549	0.0285136	0.0661375	0.0054673	0.00477027
Eye Diameter	0.205812	-0.271462	0.127121	-0.18161	-0.107625	-0.0536325	-0.111289
Pectoral Fin	0.048535	0.156604	-0.118454	-0.176557	0.00016446	0.0228703	0.0183163
Dorsal Fin L	-0.259323	-0.0035478	-0.0055230	0.0030982	0.0151355	0.00194268	-0.0199572
Peduncle Le	-0.0405785	-0.108016	0.141516	-0.0232726	-0.0844916	0.107742	0.0975062
Body Depth	-0.0626009	-0.170866	0.0243383	-0.0887391	0.025862	-0.0152384	0.0157711

Close Copy Print Help

# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST

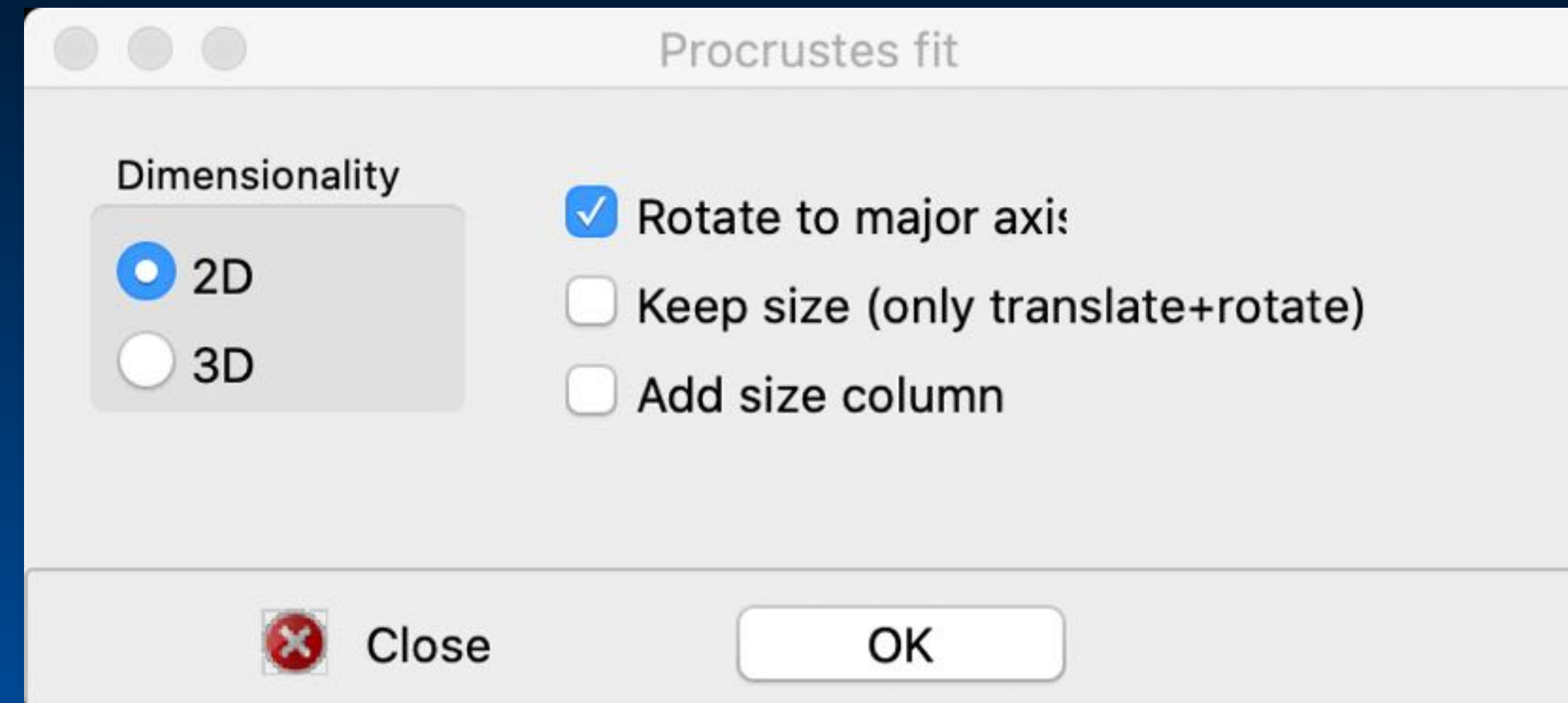
The screenshot shows the PAST software interface with a data table titled 'Fish.dat'. The table contains 23 rows of data. The first column is labeled 'Species' and the subsequent columns are labeled 'x1', 'y1', 'x2', 'y2', 'x3', 'y3', and 'x4'. The data is as follows:

	Species	x1	y1	x2	y2	x3	y3	x4
1	• Anisotremus virgatus	400	112	295	205	93	129	69
2	• Anthias anthias	359	90	300	127	146	96	112
3	• Anthias argus	350	86	258	126	97	94	64
4	• Archosargus rhomboidalis	392	106	290	186	106	121	68
5	• Chelmon rostratus	623	207	423	336	124	215	107
6	• Conodon nobilis	392	97	296	140	98	106	81
7	• Epinephelus merrilli	336	73	248	109	82	82	65
8	• Gerres erythroureus	360	104	268	162	115	112	93
9	• Holacanthus ciliaris	637	215	504	310	274	213	215
10	• Holocentrus asper	264	70	191	117	73	86	51
11	• Johnius carutta	369	67	282	107	77	75	56
12	• Oligoplites saliens	421	89	301	136	88	93	77
13	• Ophiocara macrolepis	351	94	256	135	121	107	81
14	• Perca fluviatilis	485	116	388	176	141	131	101
15	• Pomadasys furcatus	290	59	221	101	100	72	77
16	• Sparisoma chrysoptera	399	105	291	163	122	128	78
17	• Trachichthys australis	317	119	194	184	113	140	76
18	• Umbrina cirrosa	431	96	323	161	101	111	73
19	•							
20	•							
21	•							
22	•							
23	•							



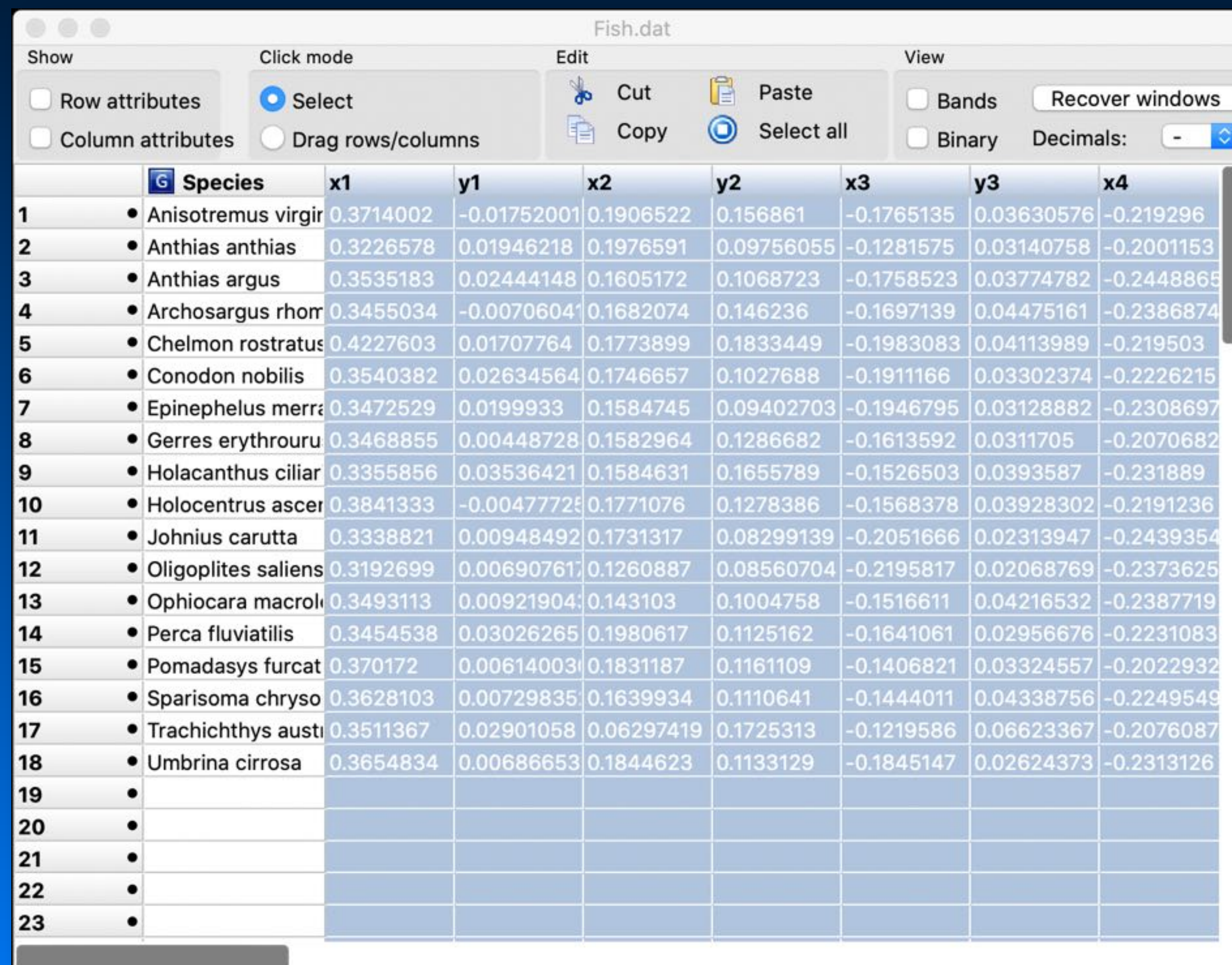
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST

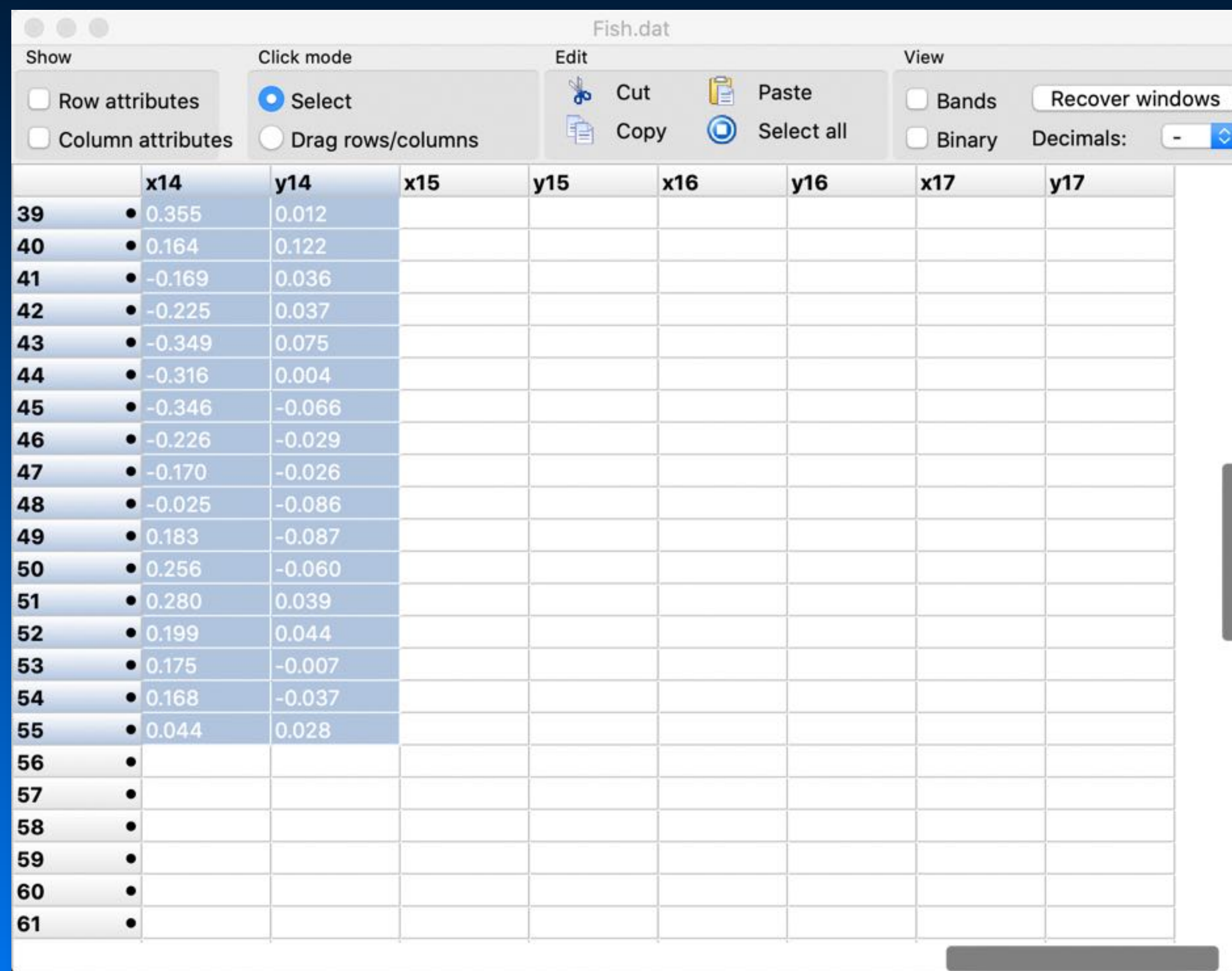


The screenshot displays the PAST software interface for a file named 'Fish.dat'. The interface includes a menu bar with 'Show', 'Click mode', 'Edit', and 'View' sections. The 'Click mode' section has 'Select' selected. The 'Edit' section includes 'Cut', 'Copy', 'Paste', and 'Select all'. The 'View' section includes 'Bands', 'Binary', 'Recover windows', and 'Decimals'. The main data table has the following columns: Species, x1, y1, x2, y2, x3, y3, and x4. The data rows are numbered 1 through 23, with the last three rows (19-23) being empty.

	Species	x1	y1	x2	y2	x3	y3	x4
1	• Anisotremus virgatus	0.3714002	-0.01752001	0.1906522	0.156861	-0.1765135	0.03630576	-0.219296
2	• Anthias anthias	0.3226578	0.01946218	0.1976591	0.09756055	-0.1281575	0.03140758	-0.2001153
3	• Anthias argus	0.3535183	0.02444148	0.1605172	0.1068723	-0.1758523	0.03774782	-0.2448865
4	• Archosargus rhomboidalis	0.3455034	-0.0070604	0.1682074	0.146236	-0.1697139	0.04475161	-0.2386874
5	• Chelmon rostratus	0.4227603	0.01707764	0.1773899	0.1833449	-0.1983083	0.04113989	-0.219503
6	• Conodon nobilis	0.3540382	0.02634564	0.1746657	0.1027688	-0.1911166	0.03302374	-0.2226215
7	• Epinephelus merrilli	0.3472529	0.0199933	0.1584745	0.09402703	-0.1946795	0.03128882	-0.2308697
8	• Gerres erythroureus	0.3468855	0.00448728	0.1582964	0.1286682	-0.1613592	0.0311705	-0.2070682
9	• Holacanthus ciliaris	0.3355856	0.03536421	0.1584631	0.1655789	-0.1526503	0.0393587	-0.231889
10	• Holocentrus asper	0.3841333	-0.00477725	0.1771076	0.1278386	-0.1568378	0.03928302	-0.2191236
11	• Johnius carutta	0.3338821	0.00948492	0.1731317	0.08299139	-0.2051666	0.02313947	-0.2439354
12	• Oligoplites saliens	0.3192699	0.00690761	0.1260887	0.08560704	-0.2195817	0.02068769	-0.2373625
13	• Ophiocara macrolepis	0.3493113	0.00921904	0.143103	0.1004758	-0.1516611	0.04216532	-0.2387719
14	• Perca fluviatilis	0.3454538	0.03026265	0.1980617	0.1125162	-0.1641061	0.02956676	-0.2231083
15	• Pomadasys furcatus	0.370172	0.00614003	0.1831187	0.1161109	-0.1406821	0.03324557	-0.2022932
16	• Sparisoma chrysolepis	0.3628103	0.00729835	0.1639934	0.1110641	-0.1444011	0.04338756	-0.2249549
17	• Trachichthys australis	0.3511367	0.02901058	0.06297419	0.1725313	-0.1219586	0.06623367	-0.2076087
18	• Umbrina cirrosa	0.3654834	0.00686653	0.1844623	0.1133129	-0.1845147	0.02624373	-0.2313126
19	•							
20	•							
21	•							
22	•							
23	•							

# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST

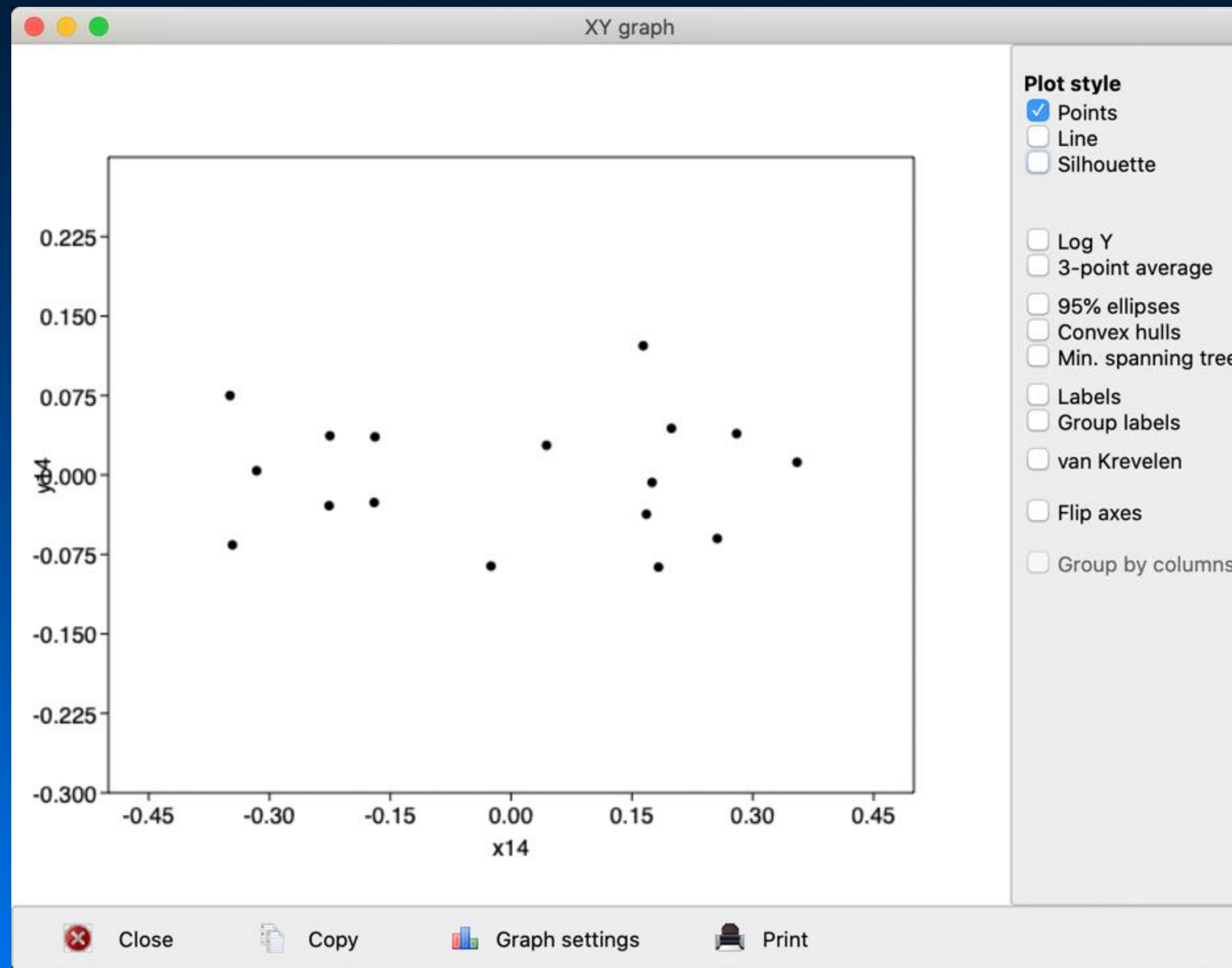


The screenshot shows the PAST software interface with a data table titled 'Fish.dat'. The table has 8 columns: x14, y14, x15, y15, x16, y16, x17, and y17. Rows 39 through 55 are highlighted in blue. The interface includes a menu bar with 'Show', 'Click mode', 'Edit', and 'View' options. The 'Click mode' is set to 'Select'. The 'View' options include 'Bands', 'Binary', and 'Decimals'.

	x14	y14	x15	y15	x16	y16	x17	y17
39	• 0.355	0.012						
40	• 0.164	0.122						
41	• -0.169	0.036						
42	• -0.225	0.037						
43	• -0.349	0.075						
44	• -0.316	0.004						
45	• -0.346	-0.066						
46	• -0.226	-0.029						
47	• -0.170	-0.026						
48	• -0.025	-0.086						
49	• 0.183	-0.087						
50	• 0.256	-0.060						
51	• 0.280	0.039						
52	• 0.199	0.044						
53	• 0.175	-0.007						
54	• 0.168	-0.037						
55	• 0.044	0.028						
56	•							
57	•							
58	•							
59	•							
60	•							
61	•							

# Lab Practical Assignment IV

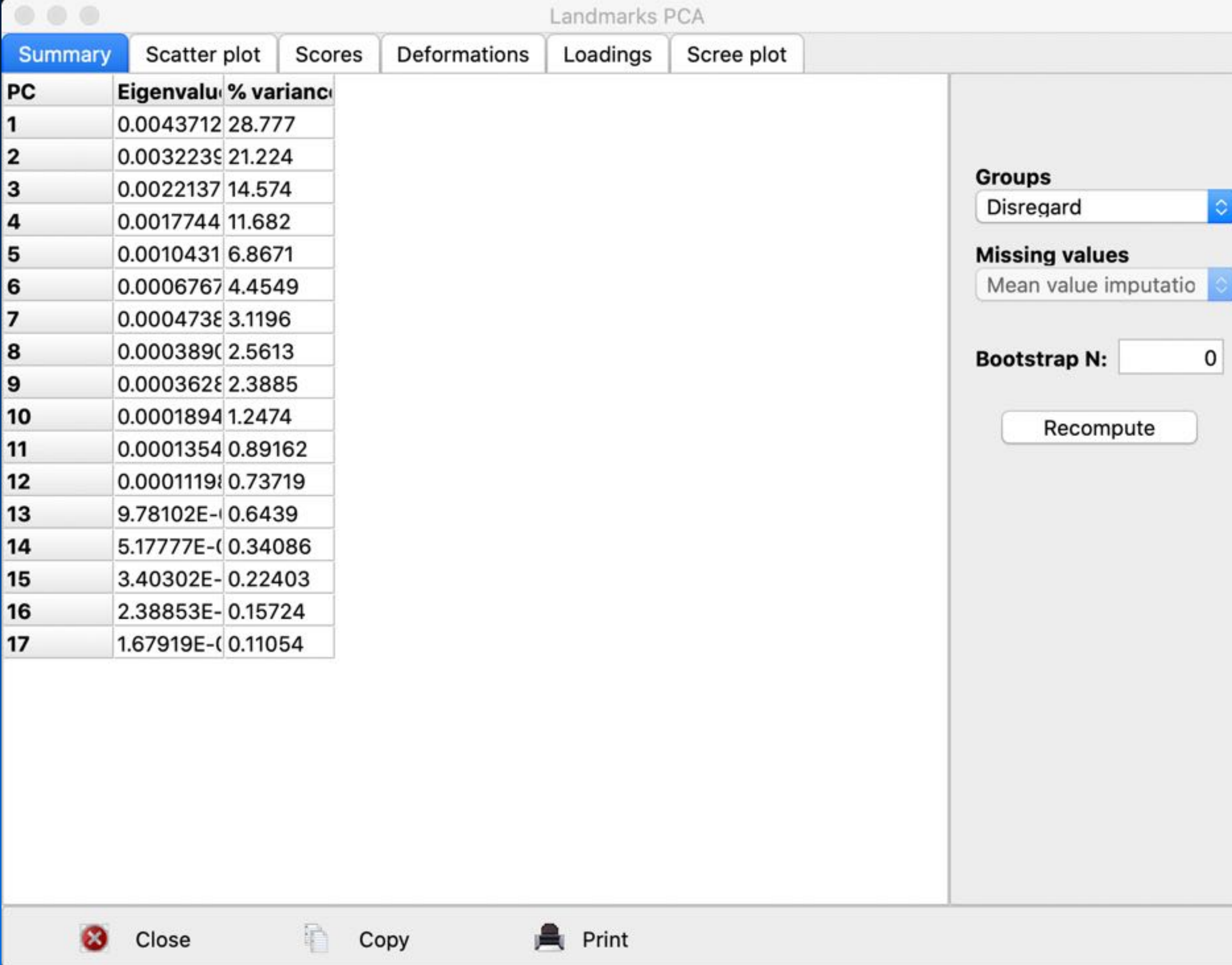
## Geometric Morphometrics (GM) in PAST





# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST

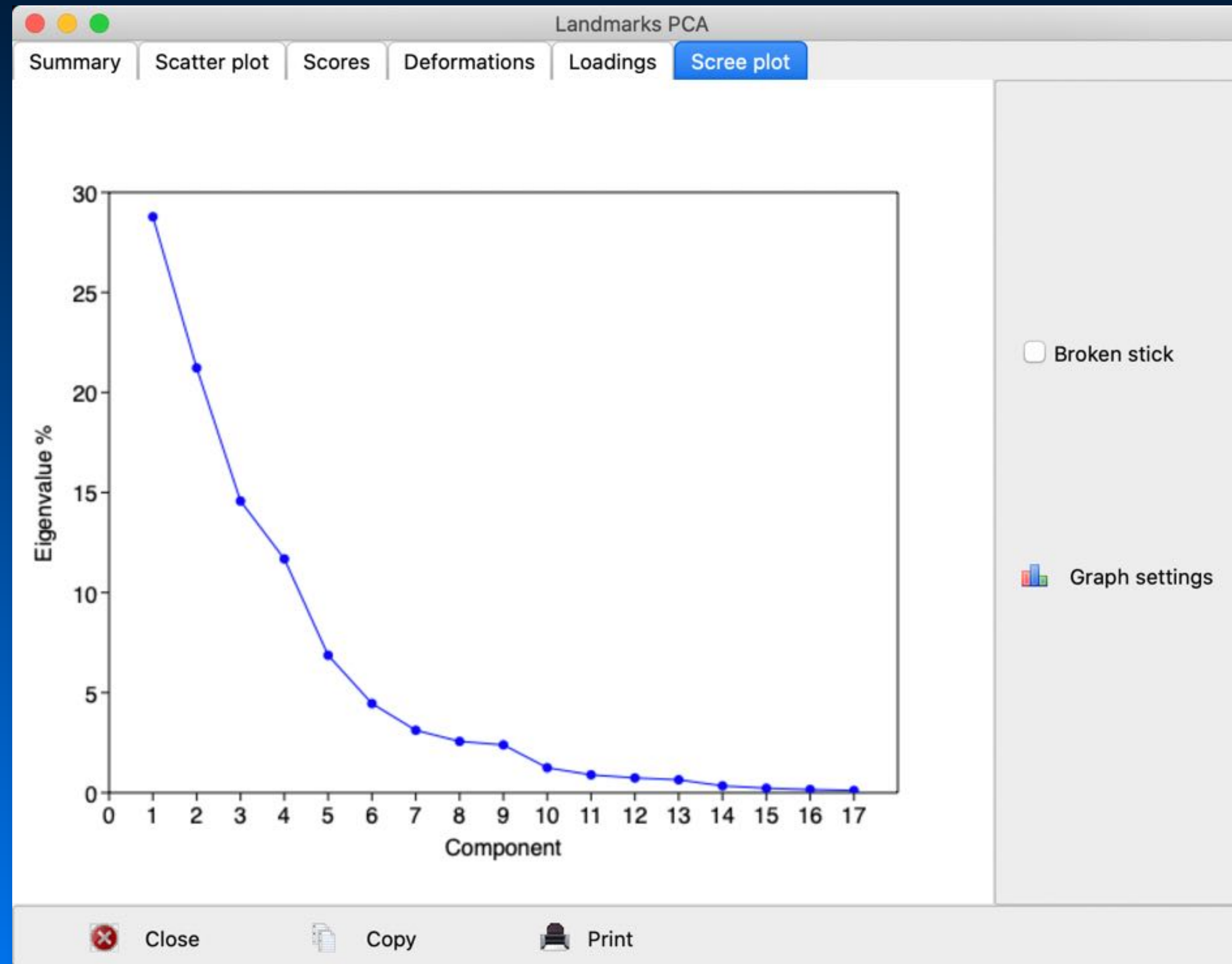


The screenshot displays the 'Landmarks PCA' software interface. The 'Summary' tab is active, showing a table of principal components (PC) and their corresponding eigenvalues and variance percentages. The table lists 17 principal components, with the first three accounting for the majority of the variance (28.777%, 21.224%, and 14.574% respectively). The interface also includes a 'Groups' dropdown menu set to 'Disregard', a 'Missing values' dropdown menu set to 'Mean value imputation', and a 'Bootstrap N' field set to 0. A 'Recompute' button is located below these settings. At the bottom of the window, there are standard macOS window controls: 'Close', 'Copy', and 'Print'.

PC	Eigenvalue	% variance
1	0.0043712	28.777
2	0.0032239	21.224
3	0.0022137	14.574
4	0.0017744	11.682
5	0.0010431	6.8671
6	0.0006767	4.4549
7	0.0004738	3.1196
8	0.0003890	2.5613
9	0.0003628	2.3885
10	0.0001894	1.2474
11	0.0001354	0.89162
12	0.0001119	0.73719
13	9.78102E-05	0.6439
14	5.17777E-05	0.34086
15	3.40302E-05	0.22403
16	2.38853E-05	0.15724
17	1.67919E-05	0.11054

# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST

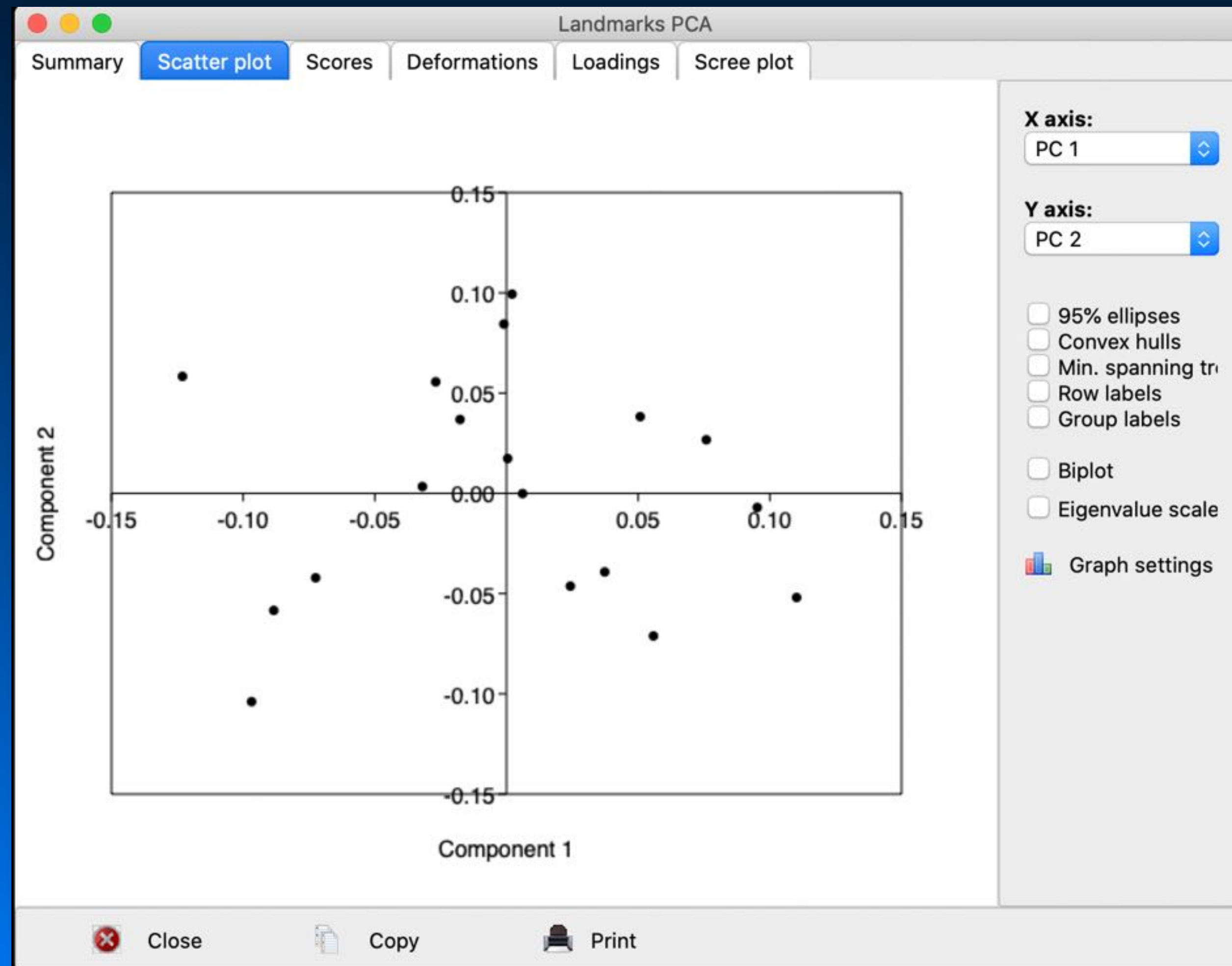
Landmarks PCA

Summary	Scatter plot	Scores	Deformations	Loadings	Scree plot				
	PC 1	PC 2	PC 3	PC 4	PC 5	PC 6	PC 7	PC 8	PC 9
1	-0.026866	0.055598	0.064949	0.034384	-0.0052946	-0.038127	0.024969	0.0044809	-0.0028
2	-0.096798	-0.10391	0.014196	0.002074	0.0099012	0.023677	-0.01501	-0.047535	-0.0049
3	0.075882	0.026719	0.0025628	-0.0218	0.013279	0.0038961	-0.0087203	-0.0042867	-0.0004
4	0.00046148	0.017351	-0.0026588	-0.027496	-0.0096916	-0.013857	0.027016	-0.0060346	-0.0004
5	0.0021173	0.099357	-0.015516	0.071542	-0.070375	0.01795	-0.01992	-0.010401	-0.0270
6	0.037309	-0.039206	0.00029195	-0.017909	-0.026682	-0.0059226	-0.009217	0.01259	-0.0029
7	0.095227	-0.0070486	0.0080838	-0.042492	-0.0084688	-0.001915	-0.039572	-0.0048142	0.01398
8	-0.072476	-0.042134	0.0023352	0.0043647	0.0010973	-0.044499	0.0098308	-0.019652	-0.0003
9	-0.0010021	0.084432	-0.025135	-0.061329	-0.021528	0.033059	0.031023	-0.023742	0.03677
10	-0.017634	0.036834	0.074168	0.04124	0.028255	-0.0025066	-0.032101	0.0052659	0.01786
11	0.11017	-0.051959	0.011192	-0.026966	-4.3234E-05	-0.020161	-0.006372	0.010329	0.00126
12	0.055808	-0.071131	-0.1166	0.084449	-0.0093282	-0.011623	0.014538	0.0033672	0.01742
13	0.050784	0.038244	-0.020593	0.036904	0.092095	0.038505	0.011856	-0.0025093	-0.0174
14	0.024266	-0.046282	0.017214	-0.045933	-0.01877	0.018353	0.015427	0.0034881	-0.0470
15	-0.088379	-0.058395	0.026723	0.013353	-0.022848	0.051104	0.0015778	0.0434	0.01980
16	-0.031932	0.0033687	0.010114	-0.017149	0.015153	-0.0091573	0.023813	0.025731	-0.0087
17	-0.12306	0.058297	-0.097009	-0.05136	0.024113	-0.023517	-0.032447	0.016925	-0.0077
18	0.0061146	-0.00013142	0.045686	0.024124	0.0091374	-0.015259	0.003307	-0.0066036	0.01308

Close Copy Print

# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST

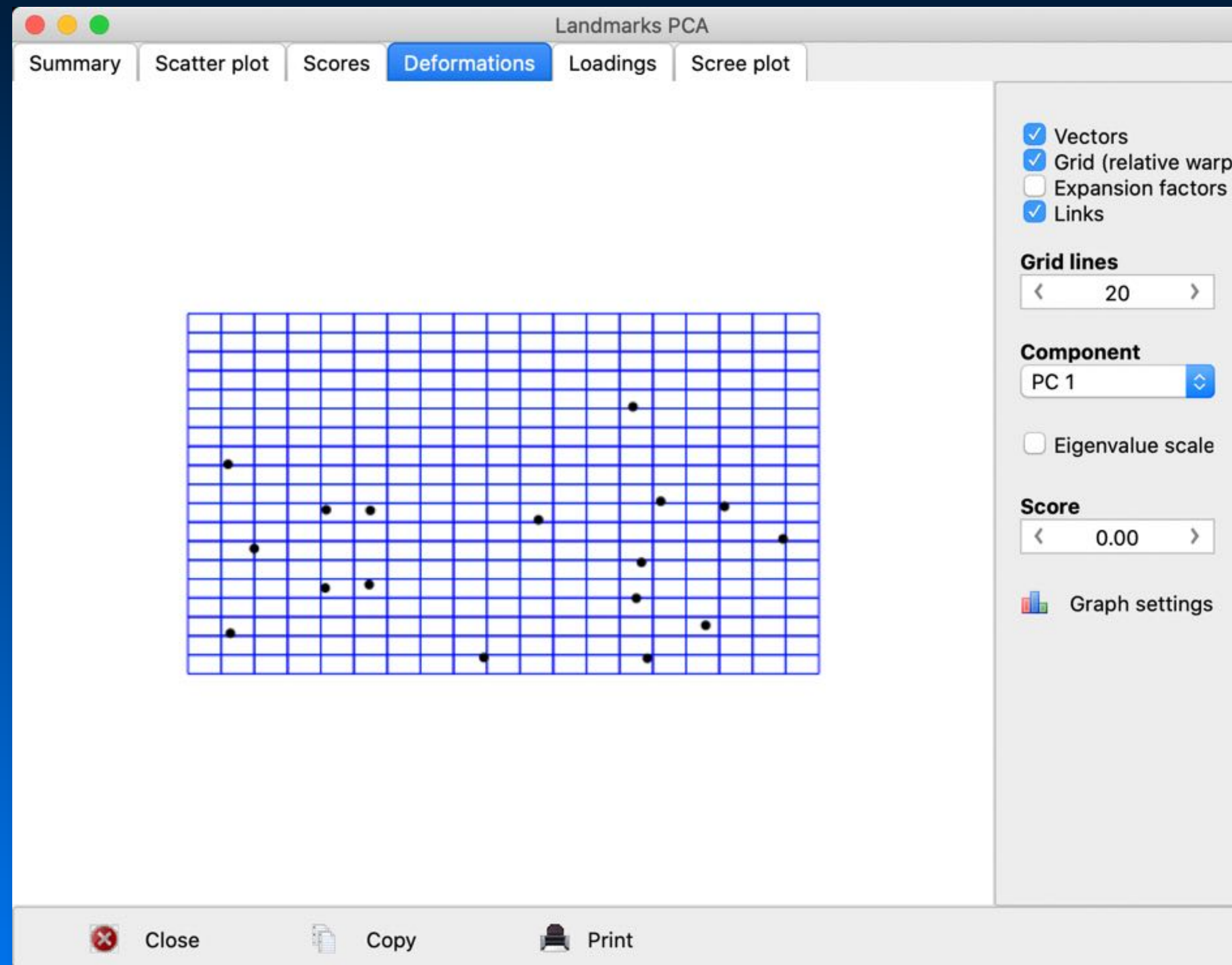
Landmarks PCA

	PC 1	PC 2	PC 3	PC 4	PC 5	PC 6	PC 7	PC 8	PC 9
x1	-0.051878	0.24533	0.19567	0.22017	-0.22647	0.060788	-0.27682	0.32297	-0.22
y1	0.01903	3.6792E-05	-0.12594	-0.18021	-0.075472	0.21856	-0.16535	-0.12962	-0.10
x2	0.072325	-0.1458	0.52673	0.098044	-0.30949	0.26532	0.31696	-0.30757	-0.18
y2	-0.22396	0.41307	-0.039758	-0.024722	-0.31301	-0.082983	0.08642	-0.11684	-0.10
x3	-0.31448	0.034169	0.047283	-0.22532	0.33423	0.30317	0.0080109	-0.011405	-0.00
y3	-0.07501	0.11316	-0.053376	-0.070381	0.073915	-0.0010597	-0.080432	0.082845	-0.00
x4	-0.18233	-0.04974	0.037345	0.017543	-0.074772	0.036204	-0.16065	-0.0029835	-0.00
y4	-0.061423	0.1469	-0.064126	-0.057168	0.12965	-0.047305	0.024969	-0.014099	-0.00
x5	0.32526	0.32679	0.027132	0.011879	0.0039667	0.011311	0.10147	-0.037506	0.00
y5	-0.21677	0.022459	-0.12687	-0.040685	0.0070389	0.38458	0.17193	0.022077	0.19
x6	-0.38838	-0.30899	-0.05965	0.049521	-0.38226	-0.37412	0.079226	0.051364	0.10
y6	0.0075227	0.024421	-0.061813	-0.030648	-0.012194	-0.0076015	0.13408	-0.080005	-0.00
x7	0.37603	0.39107	0.010097	-0.010071	0.011978	0.0016313	-0.096007	0.031928	0.08
y7	0.20235	-0.016093	-0.0024302	-0.022977	-0.043551	-0.26252	-0.082326	-0.12071	-0.30
x8	-0.17314	-0.056002	0.034868	0.076455	-0.11563	0.014281	-0.28457	0.026265	0.05
y8	0.045274	-0.048046	-0.087346	0.071526	-0.11557	-0.014548	-0.21082	-0.030634	0.23
x9	-0.28829	0.045191	0.027333	-0.14176	0.27675	0.14742	-0.1139	-0.10894	-0.00
y9	0.046799	-0.035472	-0.11734	0.063339	-0.11269	-0.009626	-0.14077	0.0053558	0.24
x10	-0.028914	0.00033638	-0.46692	0.72951	0.13845	0.10452	0.099983	-0.053188	-0.11
y10	0.11678	-0.29743	0.14021	0.017291	0.15237	-0.11111	-0.371	0.21064	-0.16
x11	0.023804	0.0090602	-0.24665	-0.14582	0.13741	-0.24439	-0.061083	-0.26974	0.00
y11	0.17812	-0.30658	0.092541	0.054315	0.039894	0.16517	-0.085667	-0.022317	0.05
x12	-0.02522	0.14629	0.09445	-0.19982	-0.034535	-0.16868	0.091622	0.24691	0.35
y12	0.14337	-0.11337	-0.0048105	-0.032384	-0.15883	0.10782	-0.035824	-0.039814	0.11

Close Copy Print

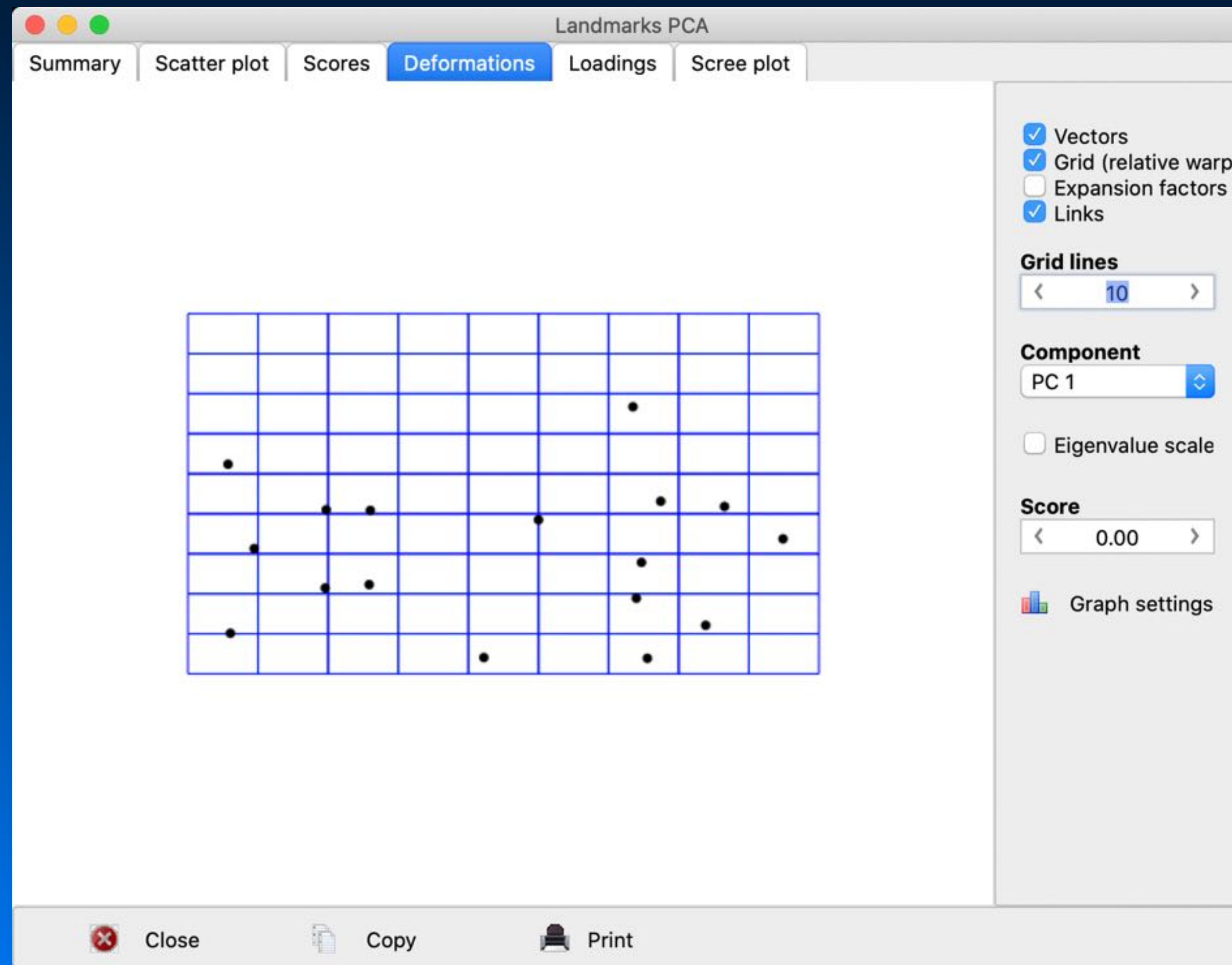
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



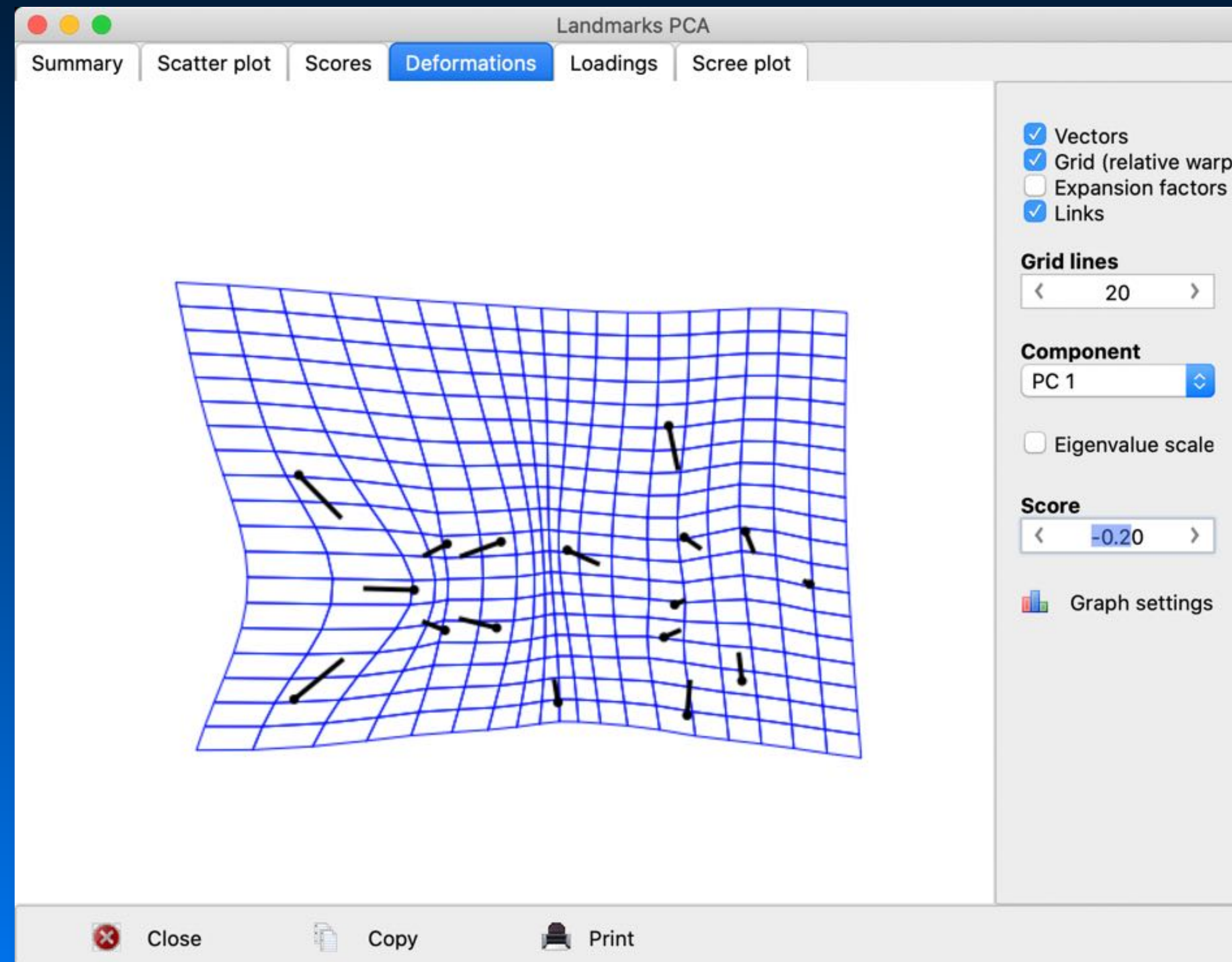
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



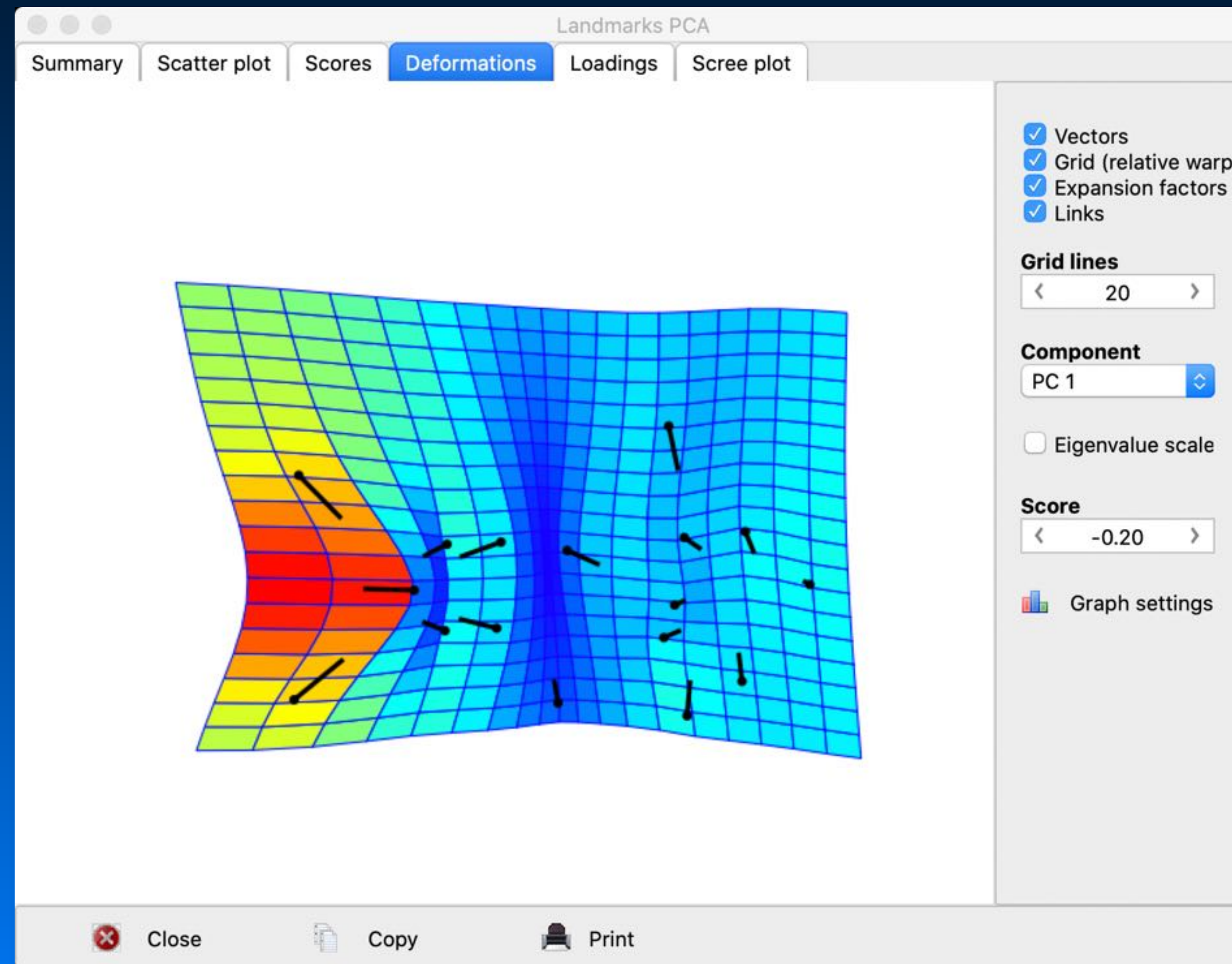
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



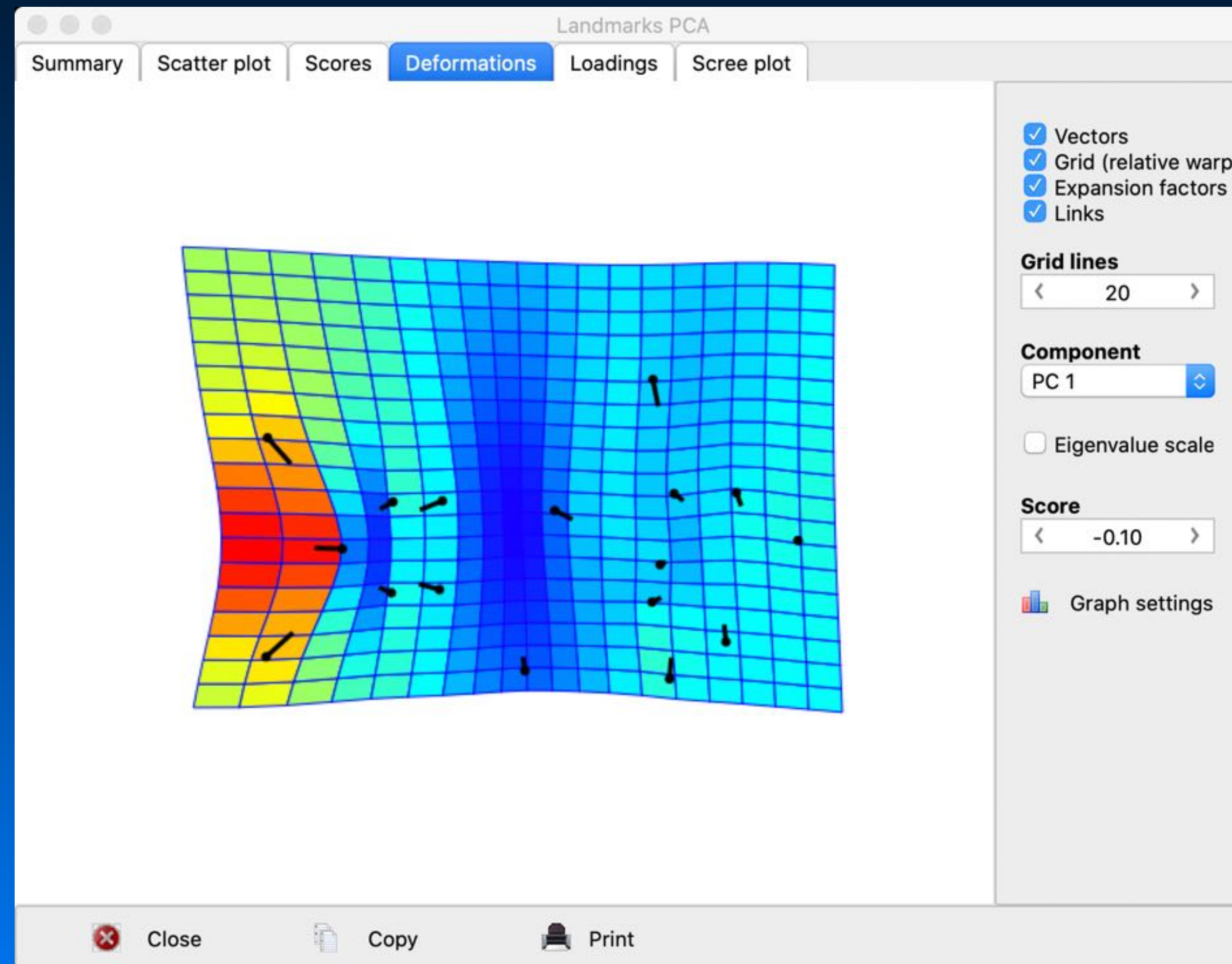
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



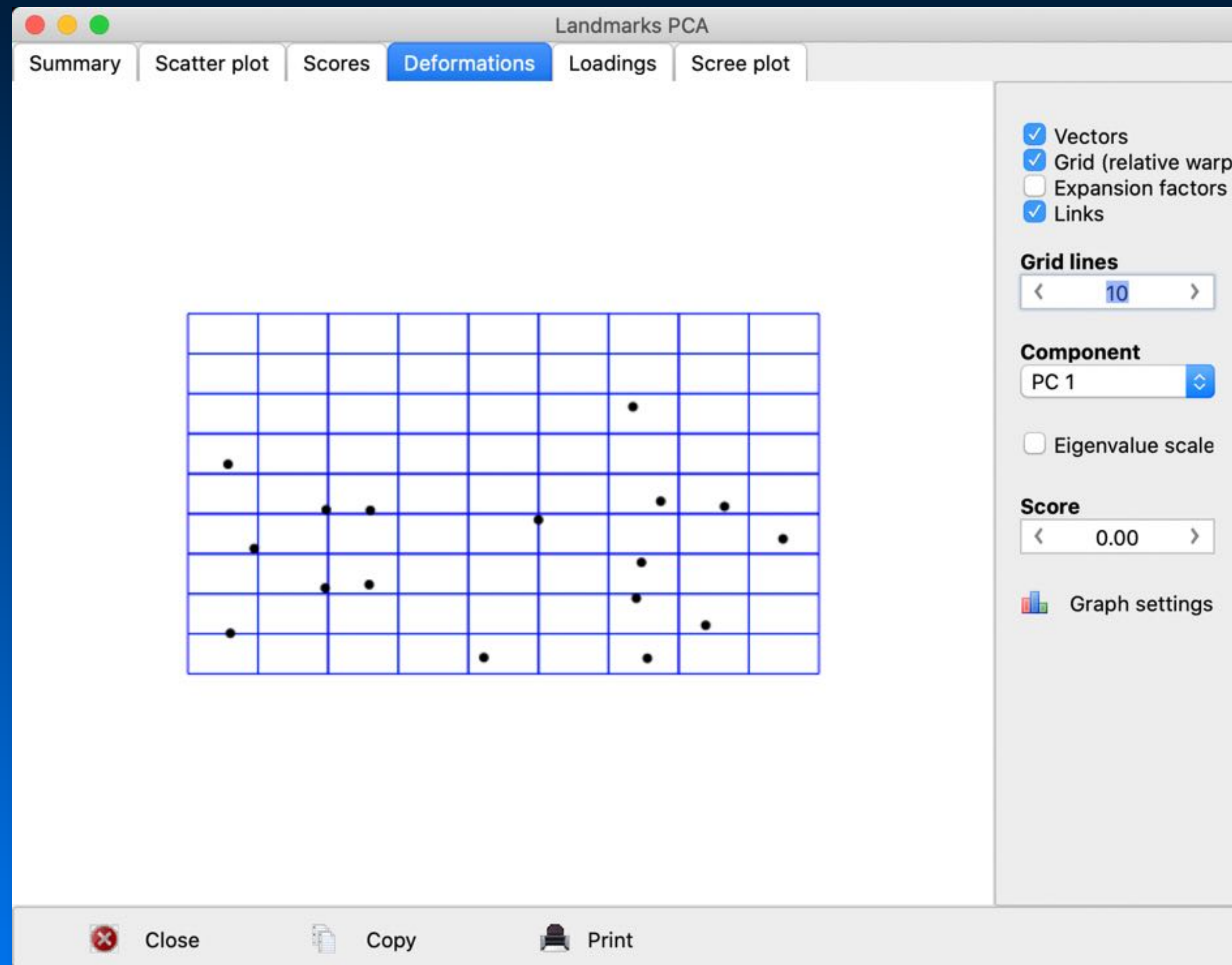
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



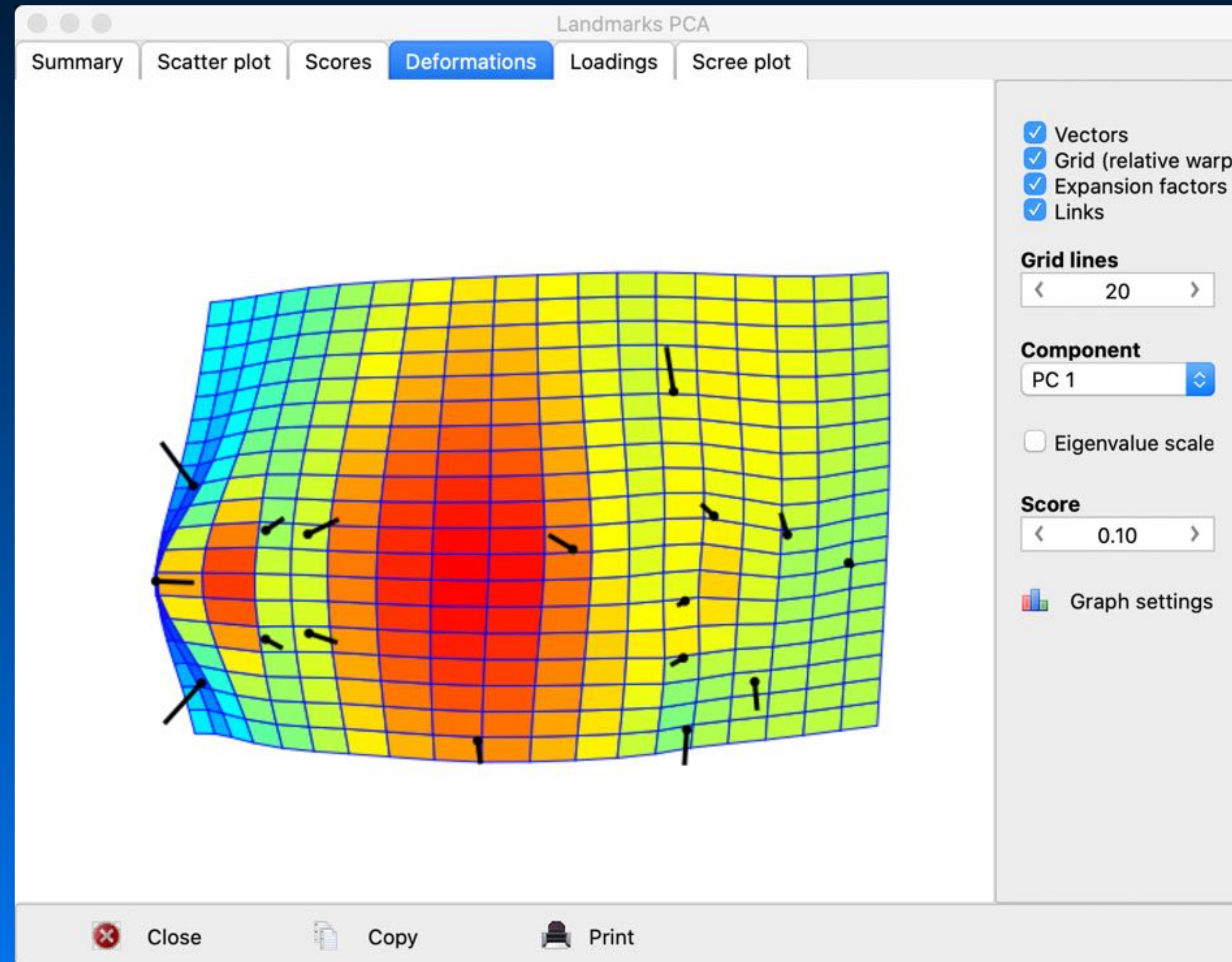
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



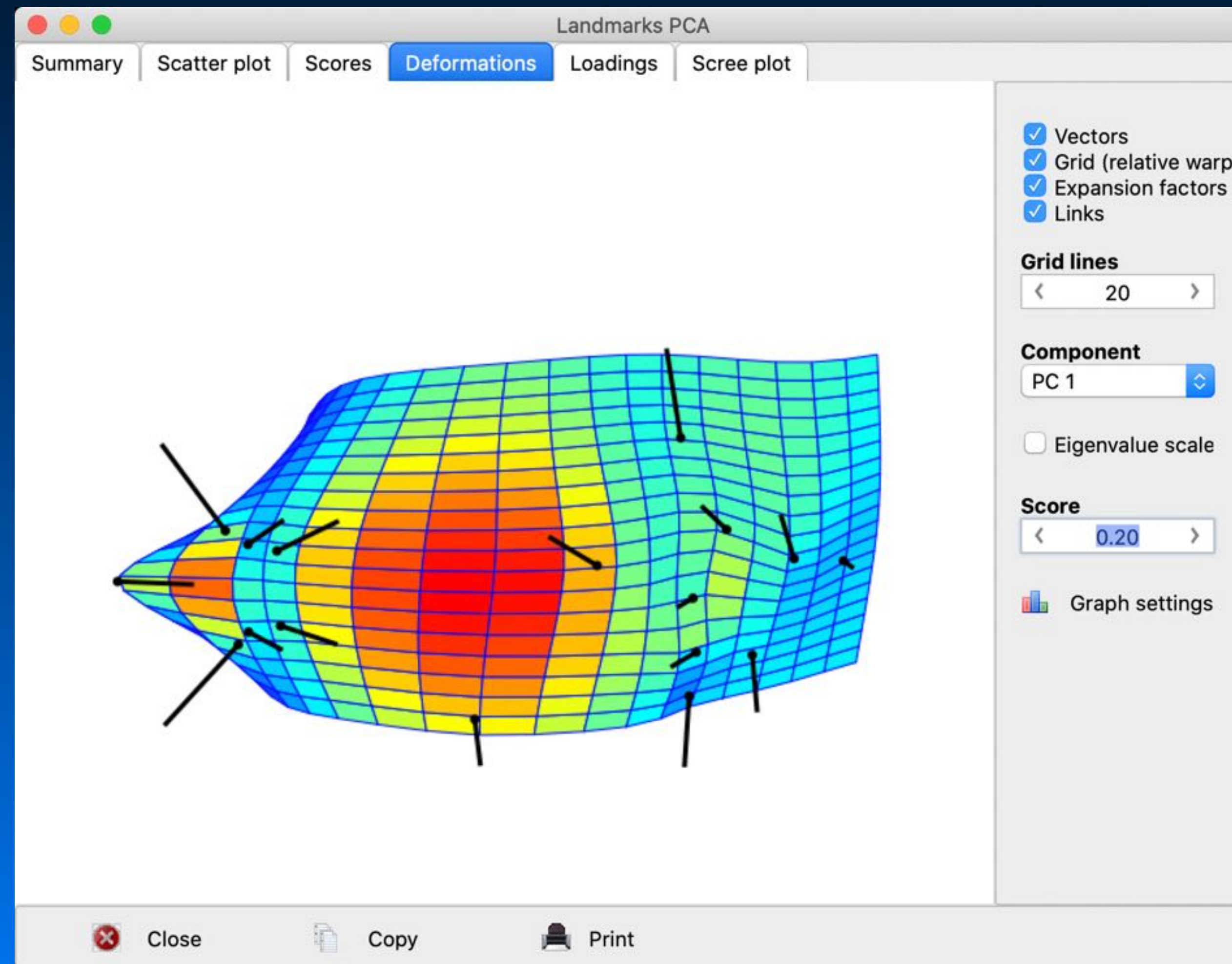
# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



# Lab Practical Assignment IV

## Geometric Morphometrics (GM) in PAST



# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST

《南京大学国际化课程建设项目申报书》 - Extinctions: Past, Present and Future.docx

Row attributes  Column attributes  Drag rows/columns

Edit: Cut, Copy, Paste, Select all

View: Bands  Binary  Recover windows, Decimals: -

	Long Axis	Inter. Axis	Short Axis	Long Diagor	Lg/Sm Sphe	Long+Inter.	Area/Volum H
1	• 3.76	3.66	0.54	5.275	9.768	13.741	4.782
2	• 8.59	4.99	1.34	10.022	7.5	10.162	2.13
3	• 6.22	6.14	4.52	9.842	2.175	2.732	1.089
4	• 7.57	7.28	7.07	12.662	1.791	2.101	0.822
5	• 9.03	7.08	2.59	11.762	4.539	6.217	1.276
6	• 5.51	3.98	1.3	6.924	5.326	7.304	2.403
7	• 3.27	0.62	0.44	3.357	7.629	8.838	8.389
8	• 8.74	7	3.31	11.675	3.529	4.757	1.119
9	• 9.64	9.49	1.03	13.567	13.133	18.519	2.354
10	• 9.73	1.33	1	9.871	9.871	11.064	3.704
11	• 8.59	2.98	1.17	9.17	7.851	9.908	2.616
12	• 7.12	5.49	3.68	9.716	2.642	3.43	1.189
13	• 4.69	3.101	2.17	5.983	2.76	3.554	2.013
14	• 5.51	1.34	1.27	5.808	4.566	5.382	3.427
15	• 1.66	1.61	1.57	2.799	1.783	2.087	3.716
16	• 5.9	5.76	1.55	8.388	5.395	7.497	1.973
17	• 9.84	9.27	1.51	13.604	9.017	12.668	1.745
18	• 8.39	4.92	2.54	10.053	3.956	5.237	1.432
19	• 4.94	4.38	1.03	6.678	6.494	9.059	2.807
20	• 7.23	2.3	1.77	7.79	4.393	5.374	2.274
21	• 9.46	7.31	1.04	11.999	11.579	16.182	2.415
22	• 9.55	5.35	4.25	11.742	2.766	3.509	1.054
23	• 4.94	4.52	4.5	8.046	1.793	2.103	1.292

# Lab Practical Assignment IV

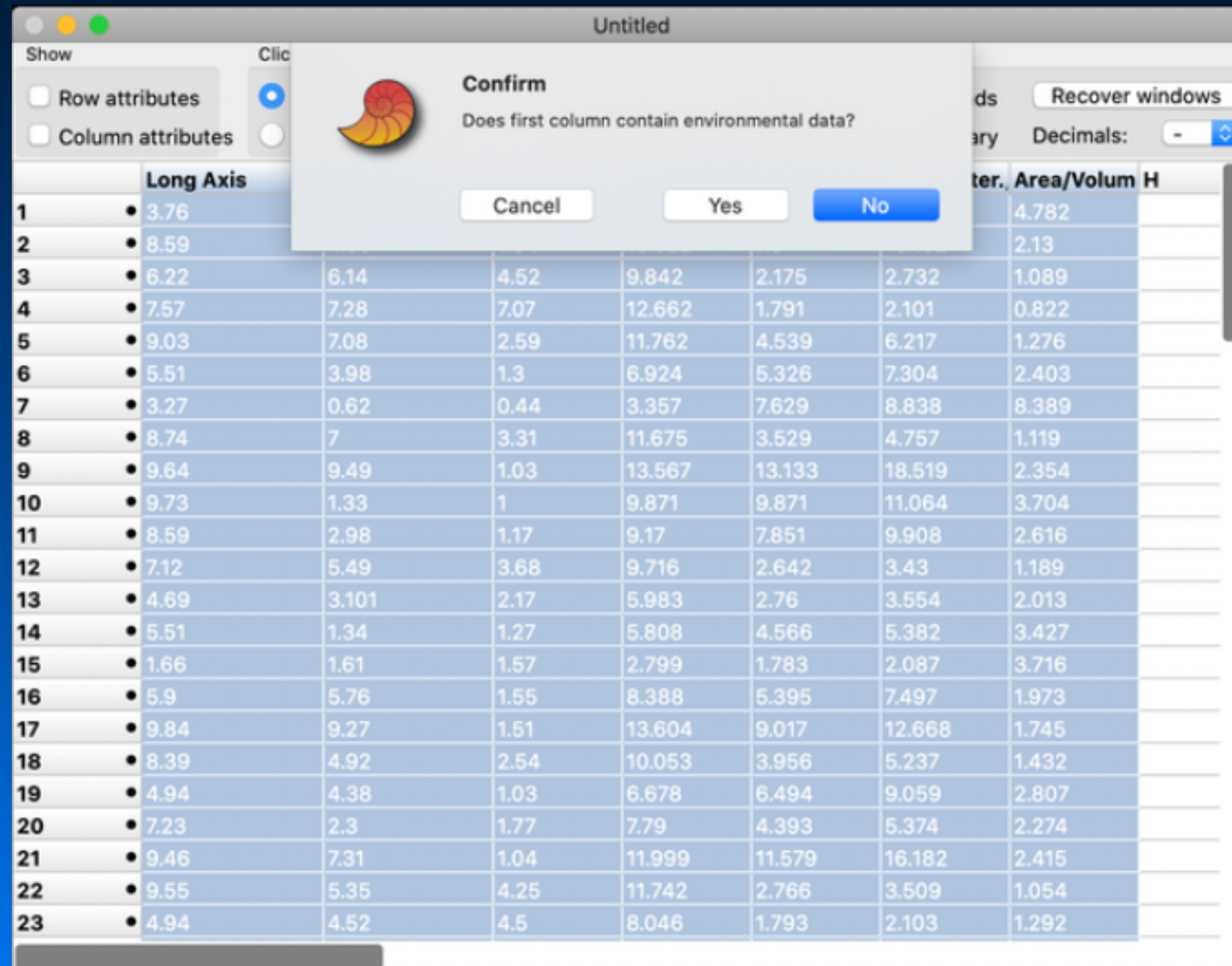
## Factor Analysis (*Q*-Mode) in PAST

The screenshot displays the PAST software interface. The 'Multivariate' menu is open, showing options for Ordination, Clustering, Tests, Calibration, Similarity and distance indices, and Genetic sequence stats. The 'Factor analysis (CABFAC)' option is selected, and a corresponding window is open. This window contains a table with 23 rows and 8 columns, representing the results of a factor analysis. The columns are labeled: Long Axis, Inter. Axis, Short Axis, Long Diagon, Lg/Sm Sphe, Long+Inter., and Area/Volum H. The first column contains row numbers from 1 to 23. The first cell of the first row (1, 1) is highlighted with a dashed border.

	Long Axis	Inter. Axis	Short Axis	Long Diagon	Lg/Sm Sphe	Long+Inter.	Area/Volum H
1	• 3.76	3.66	0.54	5.275	9.768	13.741	4.782
2	• 8.59	4.99	1.34	10.022	7.5	10.162	2.13
3	• 6.22	6.14	4.52	9.842	2.175	2.732	1.089
4	• 7.57	7.28	7.07	12.662	1.791	2.101	0.822
5	• 9.03	7.08	2.59	11.762	4.539	6.217	1.276
6	• 5.51	3.98	1.3	6.924	5.326	7.304	2.403
7	• 3.27	0.62	0.44	3.357	7.629	8.838	8.389
8	• 8.74	7	3.31	11.675	3.529	4.757	1.119
9	• 9.64	9.49	1.03	13.567	13.133	18.519	2.354
10	• 9.73	1.33	1	9.871	9.871	11.064	3.704
11	• 8.59	2.98	1.17	9.17	7.851	9.908	2.616
12	• 7.12	5.49	3.68	9.716	2.642	3.43	1.189
13	• 4.69	3.101	2.17	5.983	2.76	3.554	2.013
14	• 5.51	1.34	1.27	5.808	4.566	5.382	3.427
15	• 1.66	1.61	1.57	2.799	1.783	2.087	3.716
16	• 5.9	5.76	1.55	8.388	5.395	7.497	1.973
17	• 9.84	9.27	1.51	13.604	9.017	12.668	1.745
18	• 8.39	4.92	2.54	10.053	3.956	5.237	1.432
19	• 4.94	4.38	1.03	6.678	6.494	9.059	2.807
20	• 7.23	2.3	1.77	7.79	4.393	5.374	2.274
21	• 9.46	7.31	1.04	11.999	11.579	16.182	2.415
22	• 9.55	5.35	4.25	11.742	2.766	3.509	1.054
23	• 4.94	4.52	4.5	8.046	1.793	2.103	1.292

# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST



The screenshot shows the PAST software interface with a data table and a 'Confirm' dialog box. The dialog box asks, 'Does first column contain environmental data?' and has 'Cancel', 'Yes', and 'No' buttons. The 'No' button is highlighted in blue.

	Long Axis							
1	• 3.76							4.782
2	• 8.59							2.13
3	• 6.22	6.14	4.52	9.842	2.175	2.732		1.089
4	• 7.57	7.28	7.07	12.662	1.791	2.101		0.822
5	• 9.03	7.08	2.59	11.762	4.539	6.217		1.276
6	• 5.51	3.98	1.3	6.924	5.326	7.304		2.403
7	• 3.27	0.62	0.44	3.357	7.629	8.838		8.389
8	• 8.74	7	3.31	11.675	3.529	4.757		1.119
9	• 9.64	9.49	1.03	13.567	13.133	18.519		2.354
10	• 9.73	1.33	1	9.871	9.871	11.064		3.704
11	• 8.59	2.98	1.17	9.17	7.851	9.908		2.616
12	• 7.12	5.49	3.68	9.716	2.642	3.43		1.189
13	• 4.69	3.101	2.17	5.983	2.76	3.554		2.013
14	• 5.51	1.34	1.27	5.808	4.566	5.382		3.427
15	• 1.66	1.61	1.57	2.799	1.783	2.087		3.716
16	• 5.9	5.76	1.55	8.388	5.395	7.497		1.973
17	• 9.84	9.27	1.51	13.604	9.017	12.668		1.745
18	• 8.39	4.92	2.54	10.053	3.956	5.237		1.432
19	• 4.94	4.38	1.03	6.678	6.494	9.059		2.807
20	• 7.23	2.3	1.77	7.79	4.393	5.374		2.274
21	• 9.46	7.31	1.04	11.999	11.579	16.182		2.415
22	• 9.55	5.35	4.25	11.742	2.766	3.509		1.054
23	• 4.94	4.52	4.5	8.046	1.793	2.103		1.292

# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST

The screenshot displays the 'CABFAC factor analysis' software interface. The 'Summary' tab is active, showing a table of principal components (PC) with their corresponding eigenvalues and the percentage of variance explained. The table is as follows:

PC	Eigenvalue	% variance
1	22.302	89.21
2	1.9884	7.95
3	0.45436	1.82
4	0.21918	0.88
5	0.032385	0.13
6	0.0028774	0.01
7	0.00044272	0.00

Below the table, the 'Varimax factors' are set to 3, and a 'Save transfer function' button is visible. The interface also includes standard window controls (Close, Copy, Print) at the bottom.

# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST



# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST



# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST



# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST

CABFAC factor analysis

Summary Scatter plot **Factors** Score plot Scores Reconstruction plot Recon < >

	Factor 1	Factor 2	Factor 3
1	0.25166	-0.94507	0.15775
2	0.62315	-0.78003	0.052032
3	0.92145	-0.35465	0.12875
4	0.9525	-0.2476	0.13774
5	0.82637	-0.55727	0.047103
6	0.60796	-0.78393	0.11991
7	0.14461	-0.87368	0.46354
8	0.8762	-0.4742	0.064172
9	0.5177	-0.84818	-0.00032143
10	0.50215	-0.83378	0.12374
11	0.56908	-0.81055	0.085776
12	0.89672	-0.42828	0.10997
13	0.78002	-0.59128	0.20412
14	0.57347	-0.76178	0.25946
15	0.53135	-0.58507	0.60377
16	0.67547	-0.72527	0.077413

Close Copy Print

# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST

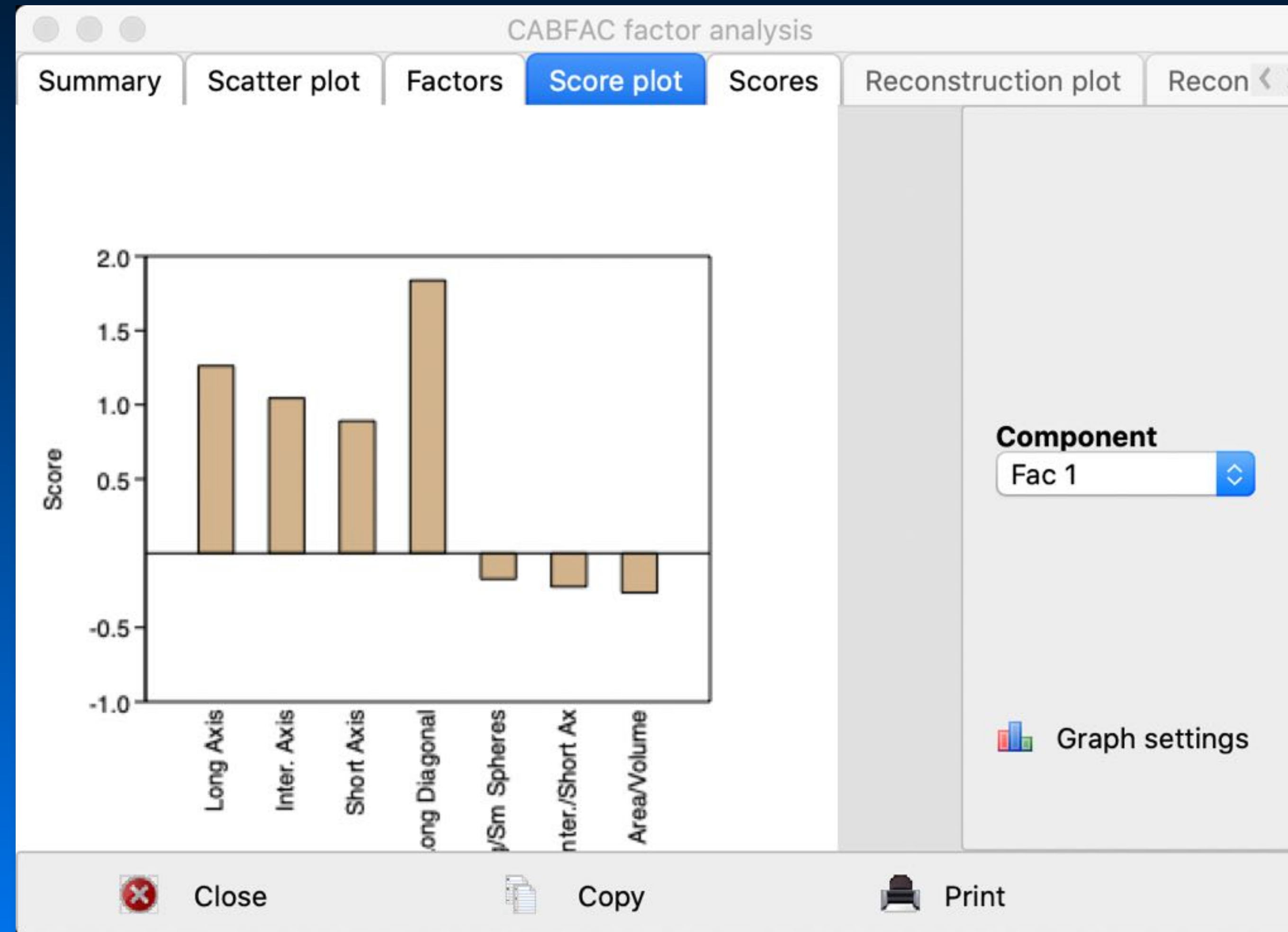
CABFAC factor analysis

Summary	Scatter plot	Factors	Score plot	Scores	Reconstruction plot	Recon < >
		<b>Factor 1</b>	<b>Factor 2</b>	<b>Factor 3</b>		
<b>Long Axis</b>	1.2614	-0.46931	-0.14766			
<b>Inter. Axis</b>	1.0446	-0.11176	-0.23943			
<b>Short Axis</b>	0.89014	0.51091	0.92102			
<b>Long Diagon</b>	1.8369	-0.30847	0.11411			
<b>Lg/Sm Sphe</b>	-0.17366	-1.479	0.086597			
<b>Long+Inter.</b>	-0.22492	-2.0119	-0.30829			
<b>Area/Volum</b>	-0.26524	-0.41938	2.4407			

Close Copy Print

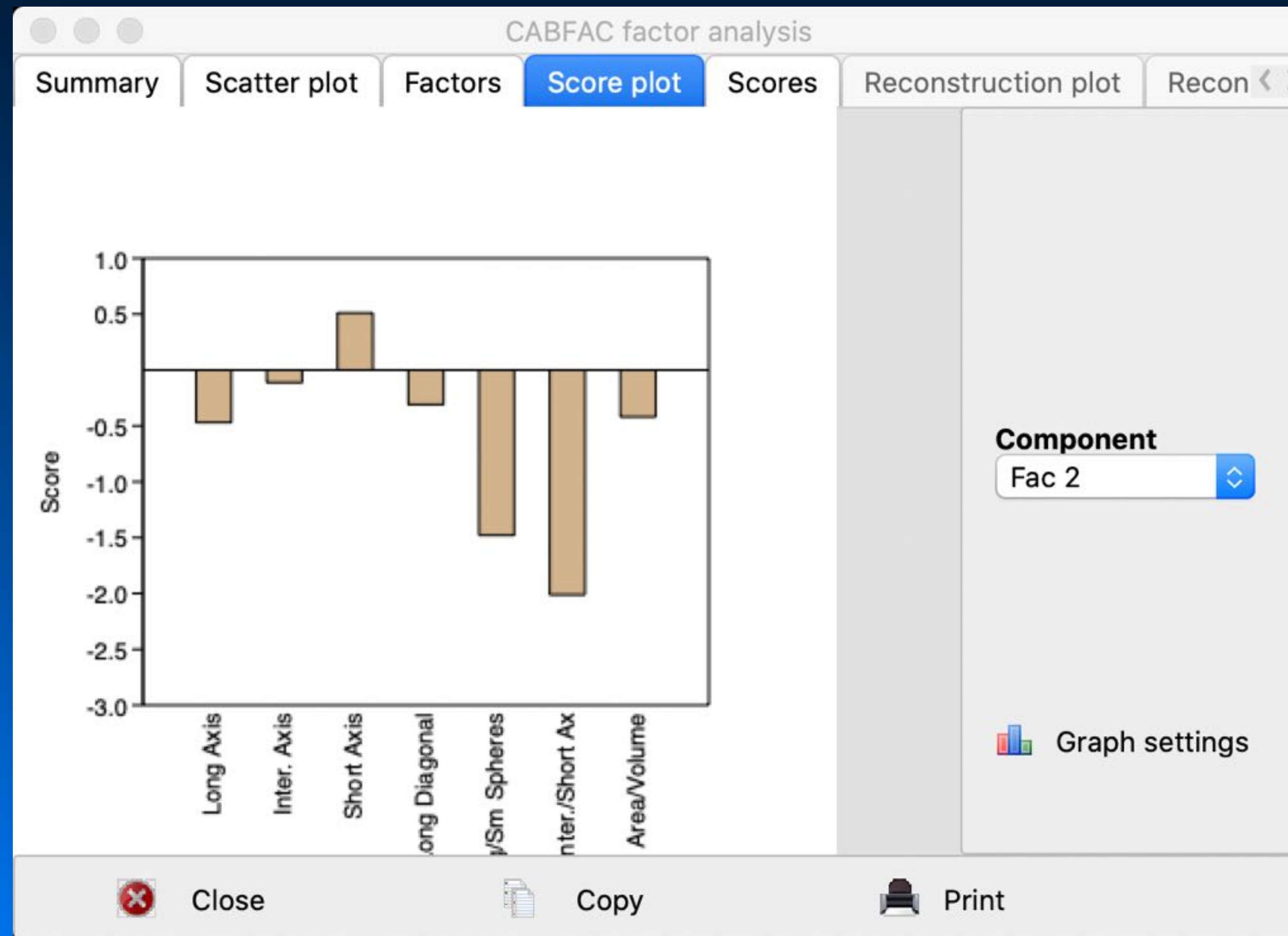
# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST



# Lab Practical Assignment IV

## Factor Analysis (*Q*-Mode) in PAST

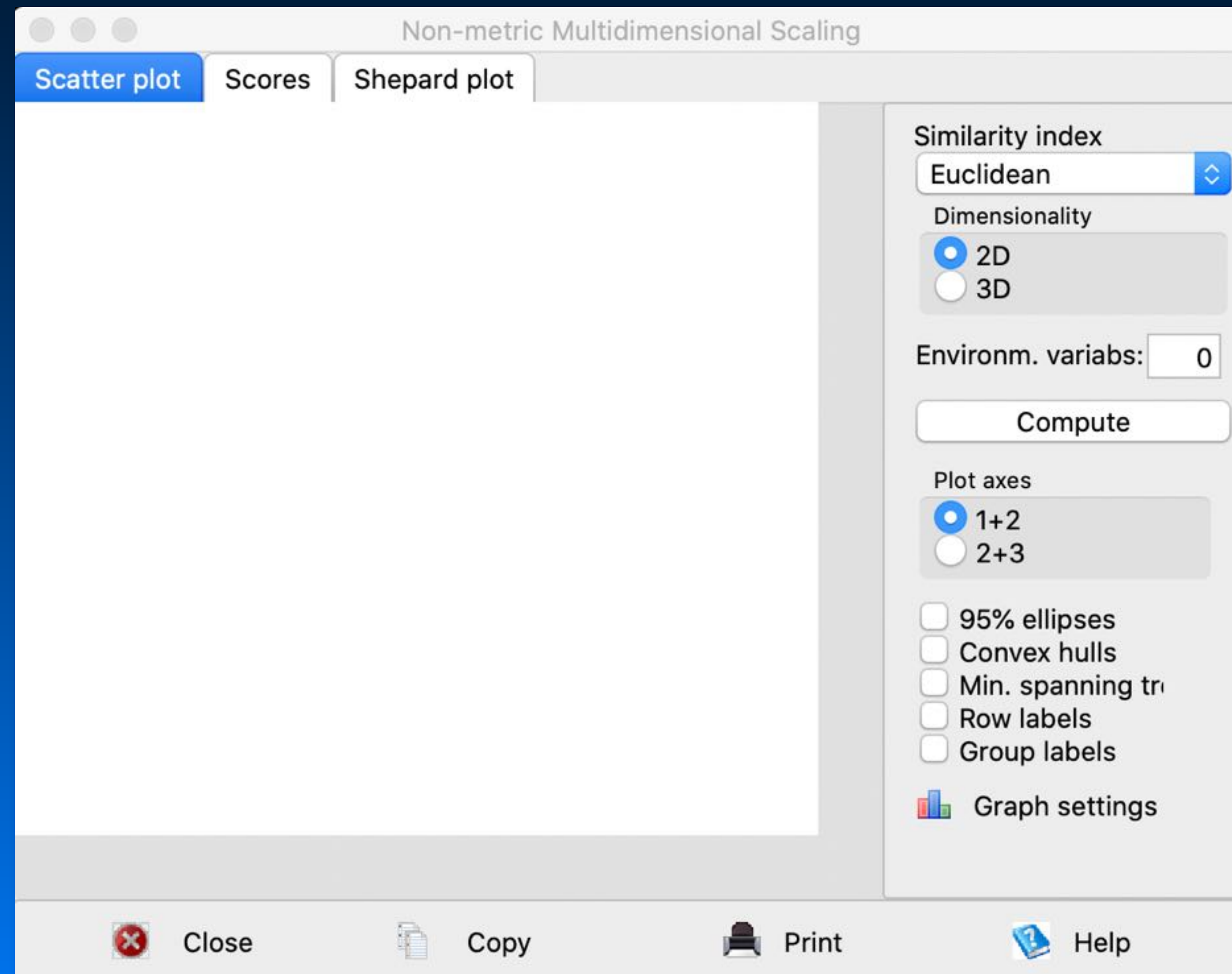






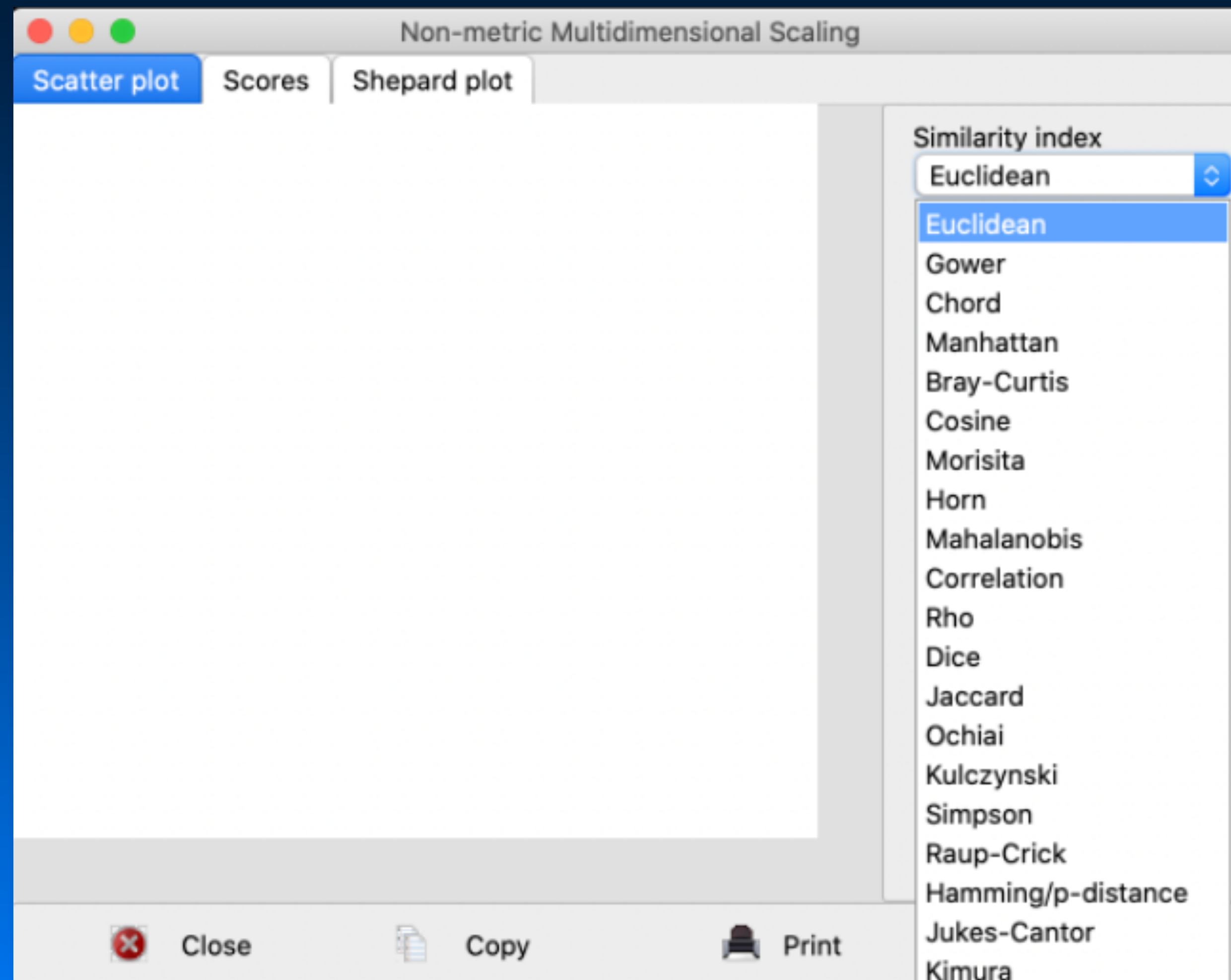
# Lab Practical Assignment IV

## Multidimensional Scaling (MDS) in PAST



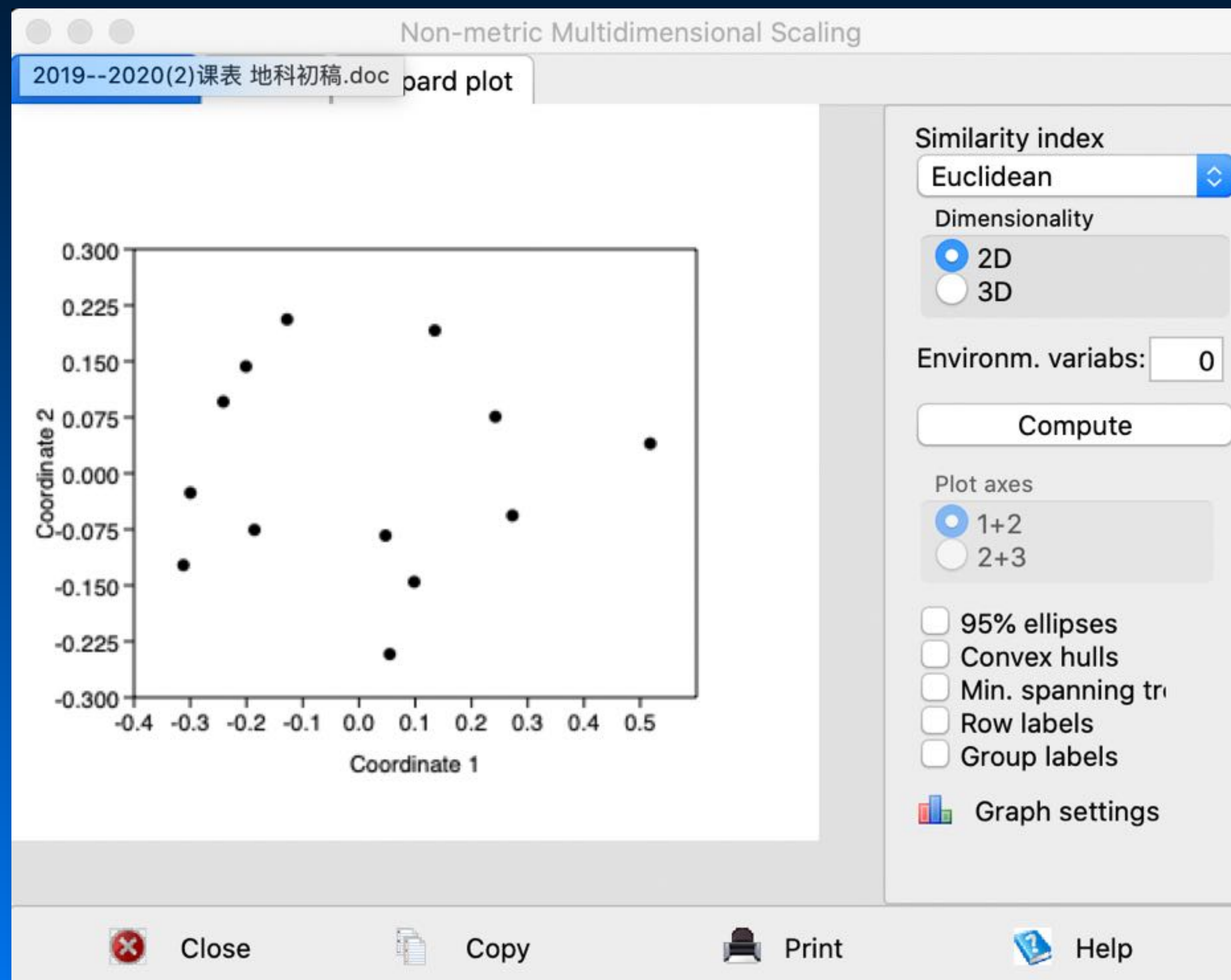
# Lab Practical Assignment IV

## Multidimensional Scaling (MDS) in PAST



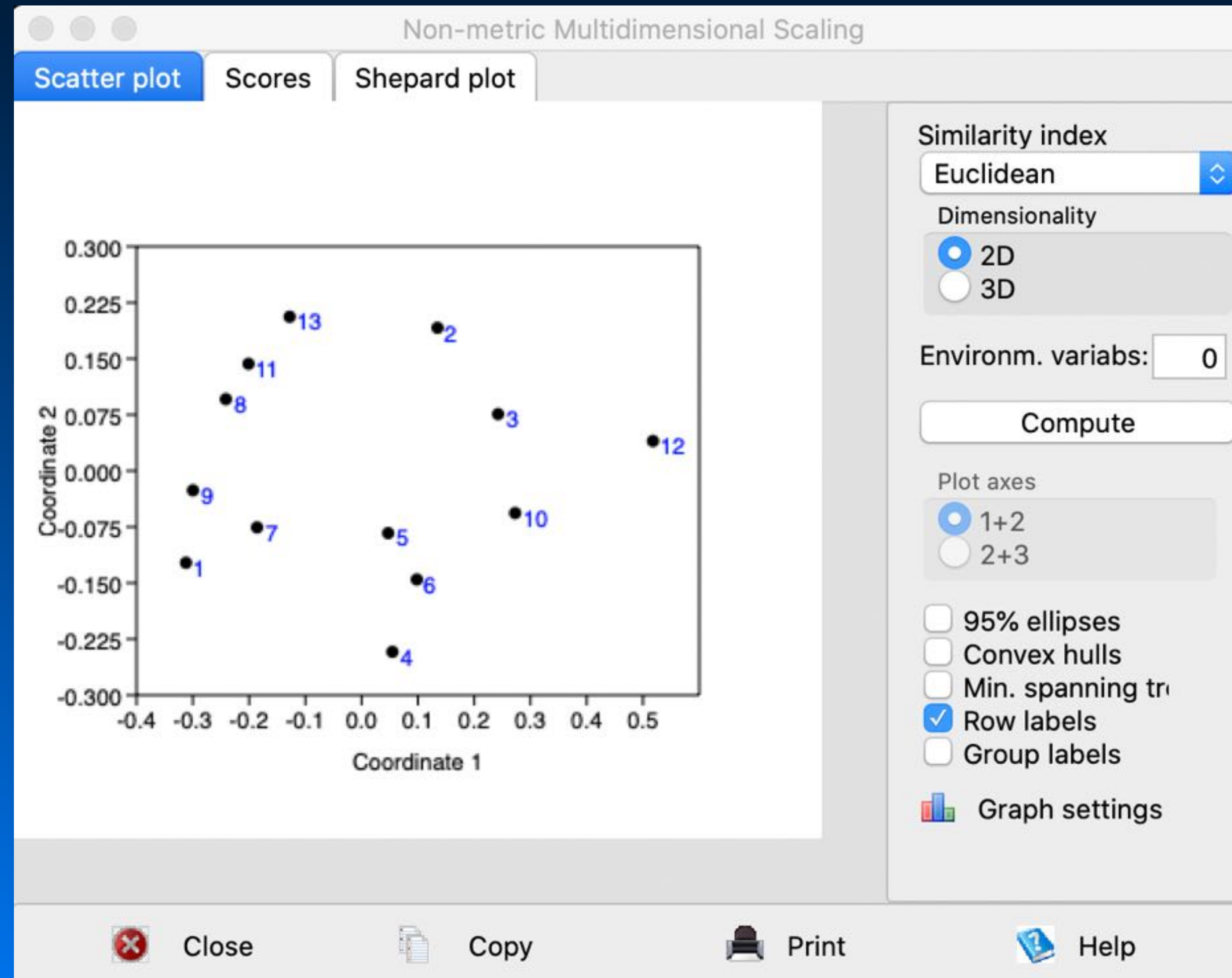
# Lab Practical Assignment IV

## Multidimensional Scaling (MDS) in PAST



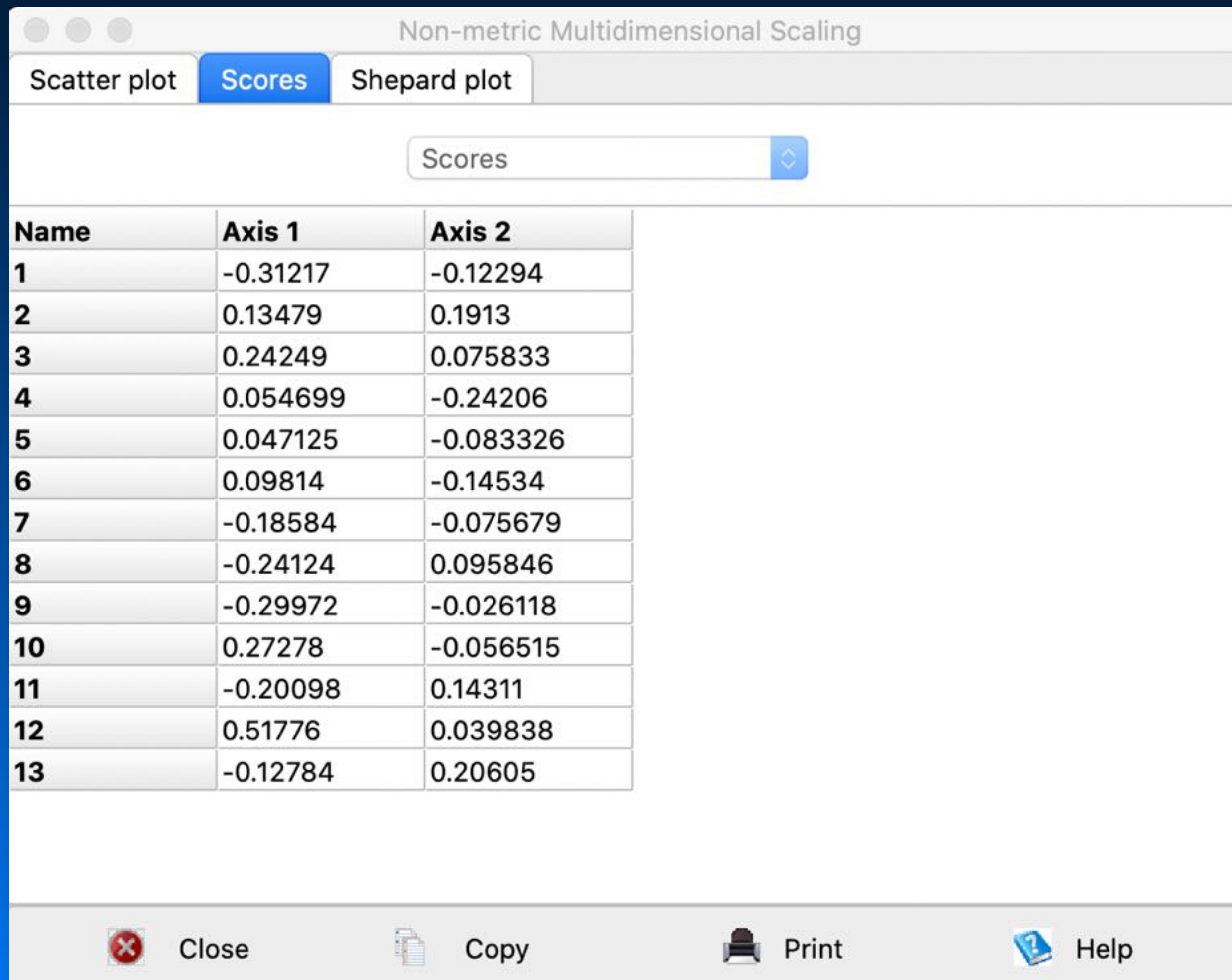
# Lab Practical Assignment IV

## Multidimensional Scaling (MDS) in PAST



# Lab Practical Assignment IV

## Multidimensional Scaling (MDS) in PAST

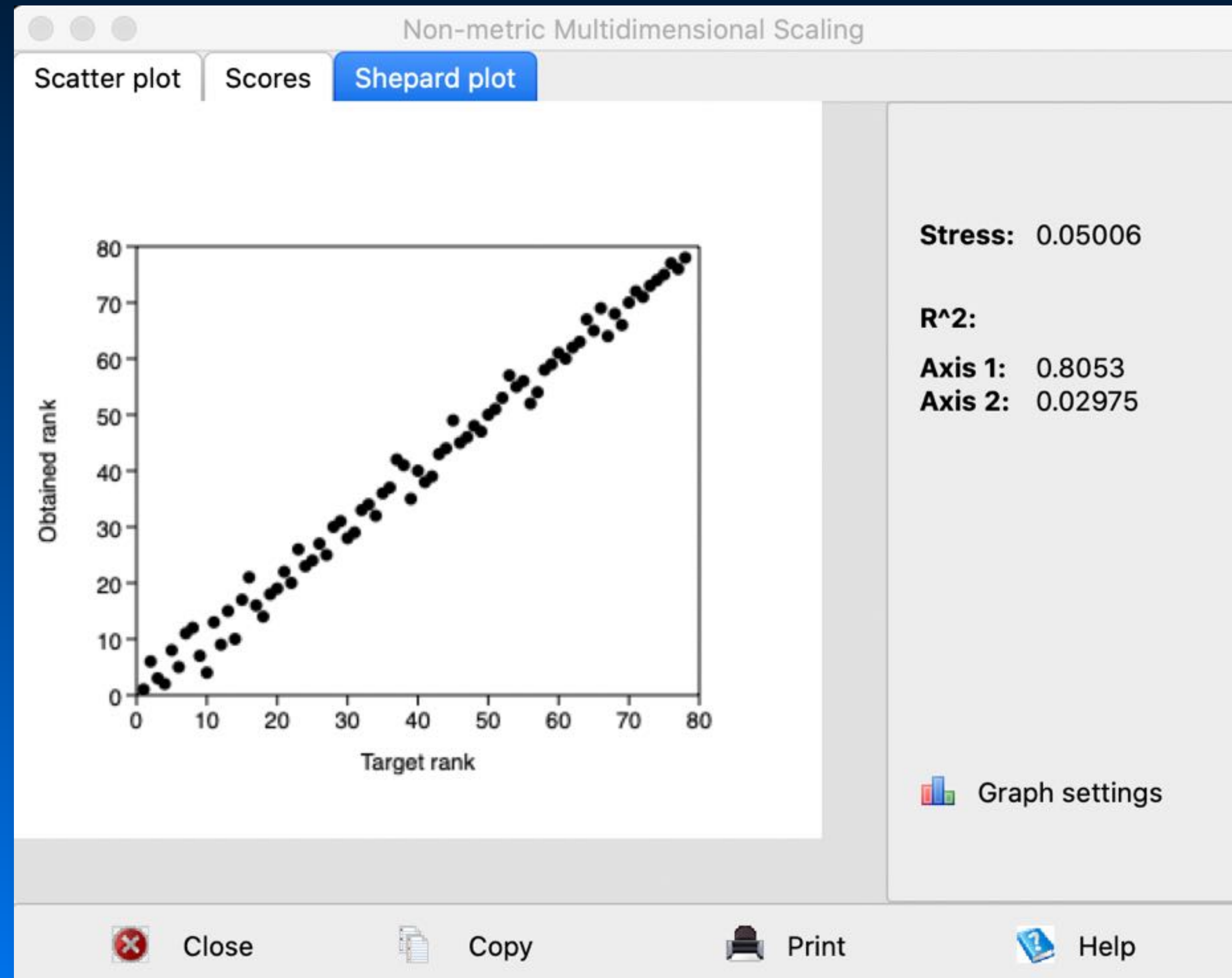


The screenshot shows a software window titled "Non-metric Multidimensional Scaling". It has three tabs: "Scatter plot", "Scores" (which is selected), and "Shepard plot". Below the tabs is a dropdown menu labeled "Scores". The main area contains a table with three columns: "Name", "Axis 1", and "Axis 2". The table lists 13 samples with their corresponding coordinates on the two axes. At the bottom of the window, there are four icons: a red 'X' for "Close", a document icon for "Copy", a printer icon for "Print", and a question mark icon for "Help".

Name	Axis 1	Axis 2
1	-0.31217	-0.12294
2	0.13479	0.1913
3	0.24249	0.075833
4	0.054699	-0.24206
5	0.047125	-0.083326
6	0.09814	-0.14534
7	-0.18584	-0.075679
8	-0.24124	0.095846
9	-0.29972	-0.026118
10	0.27278	-0.056515
11	-0.20098	0.14311
12	0.51776	0.039838
13	-0.12784	0.20605

# Lab Practical Assignment IV

## Multidimensional Scaling (MDS) in PAST



# Lab Practical Assignment IV

## Multivariate Data Analysis, Morphometrics & Diversity

